

Nanomagnetism

Part 4 — Learn from loops



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- ⇒ **Extract loop and moments**
- ⇒ Extract magnetic anisotropy
- ⇒ Extract interactions and distributions
- ⇒ Understand magnetization processes
- ⇒ Analyse thermal effects



Manipulation of magnetic materials:

➡ Application of a magnetic field

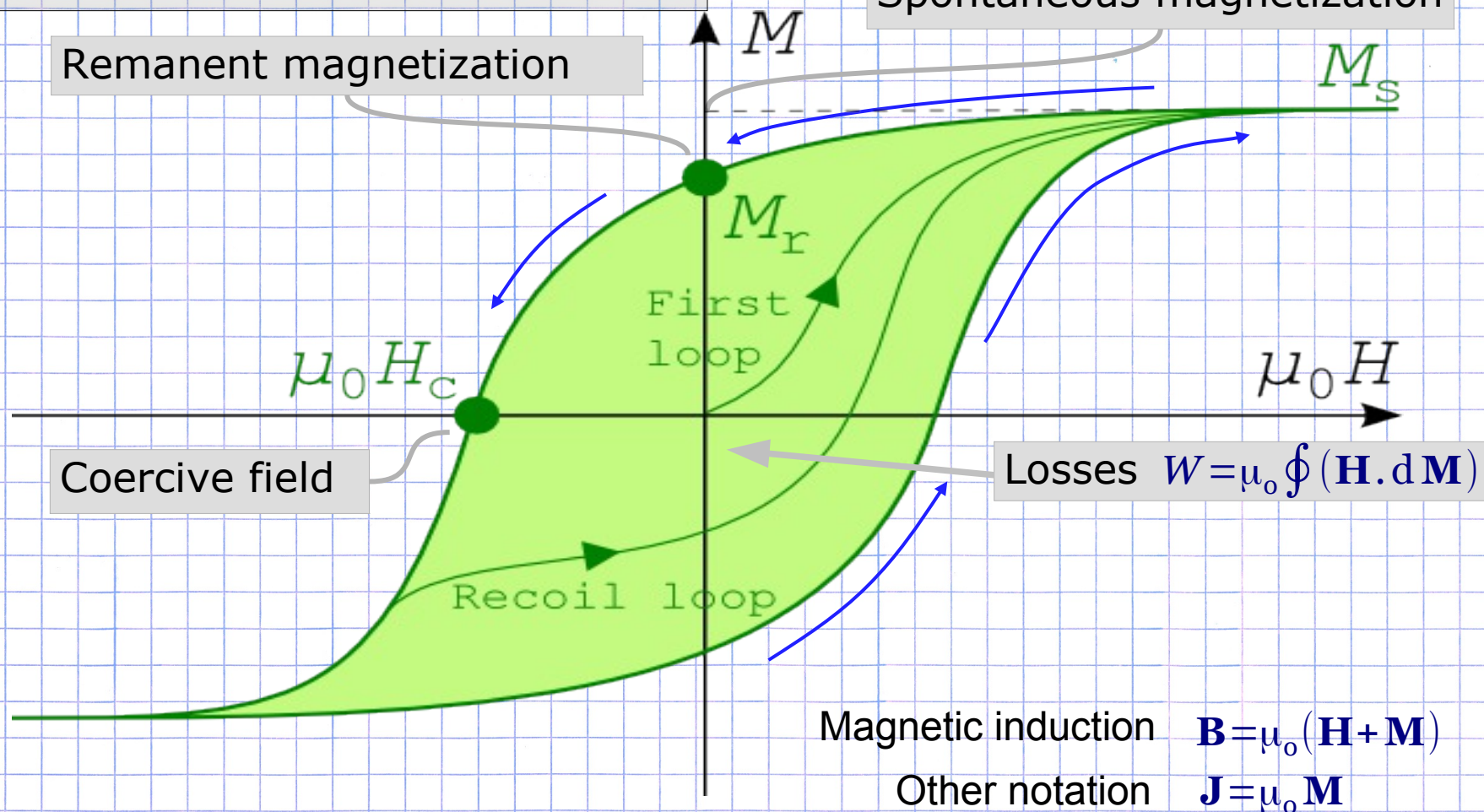
Zeeman energy: $E_Z = -\mu_0 \mathbf{H} \cdot \mathbf{M}$



Spontaneous $\neq$ **S**aturation

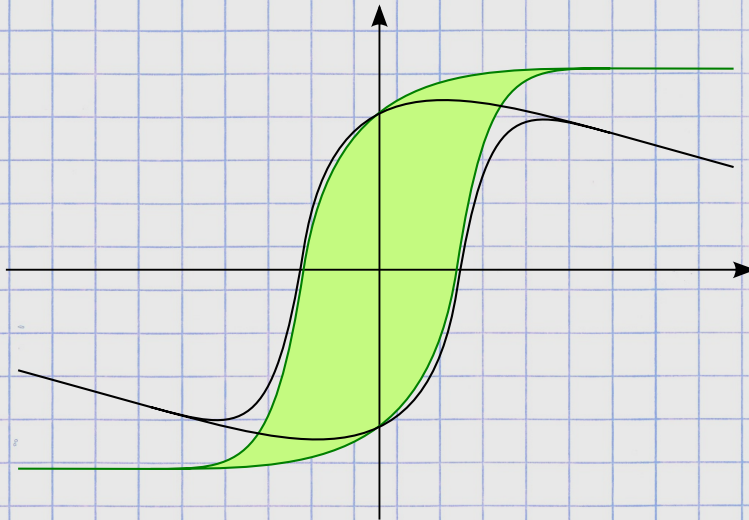
Spontaneous magnetization

Remanent magnetization





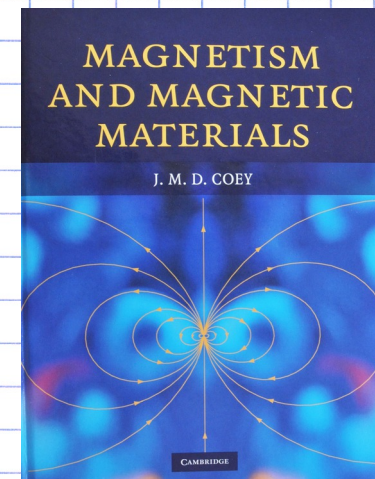
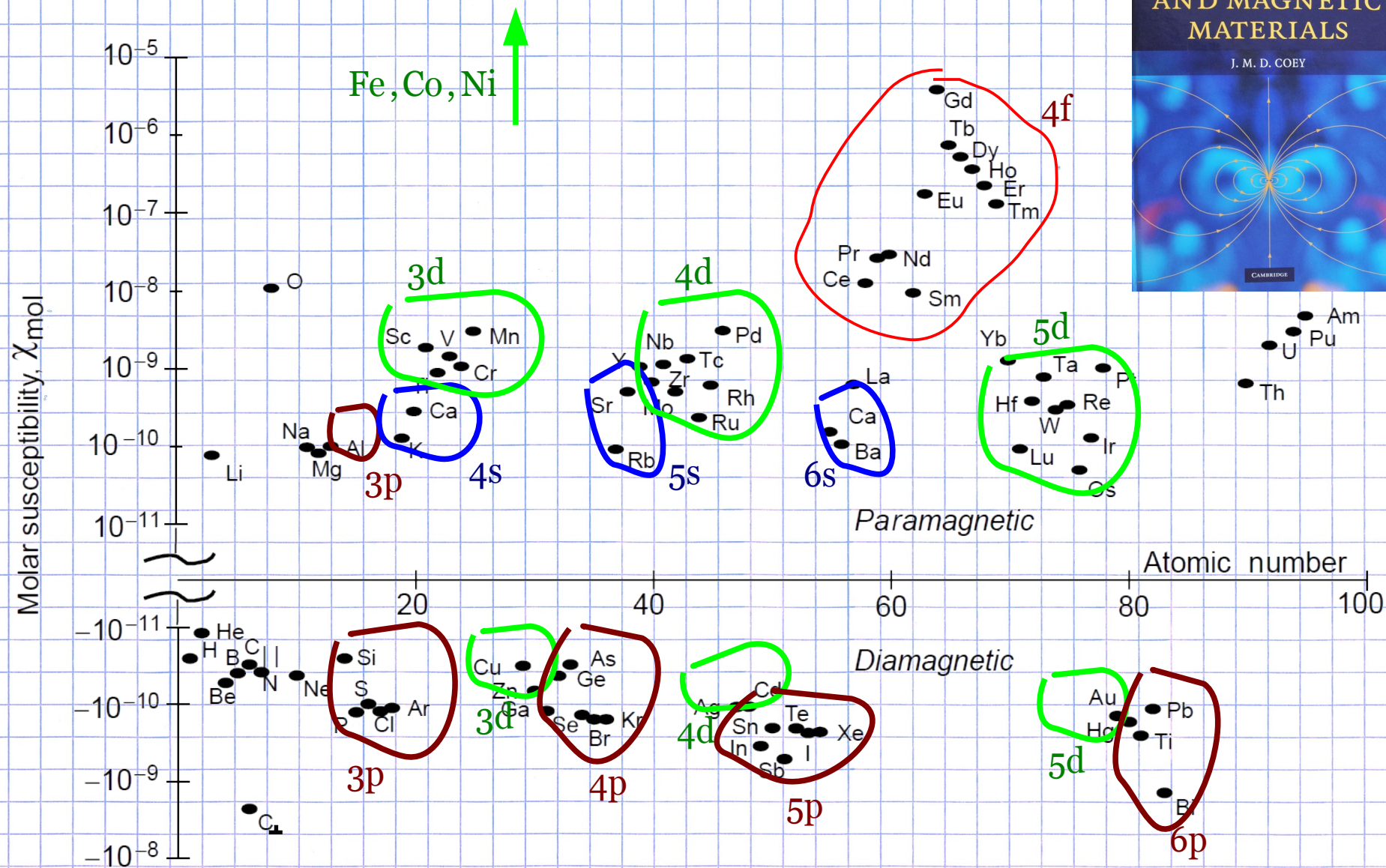
Diamagnetic substrate / holder



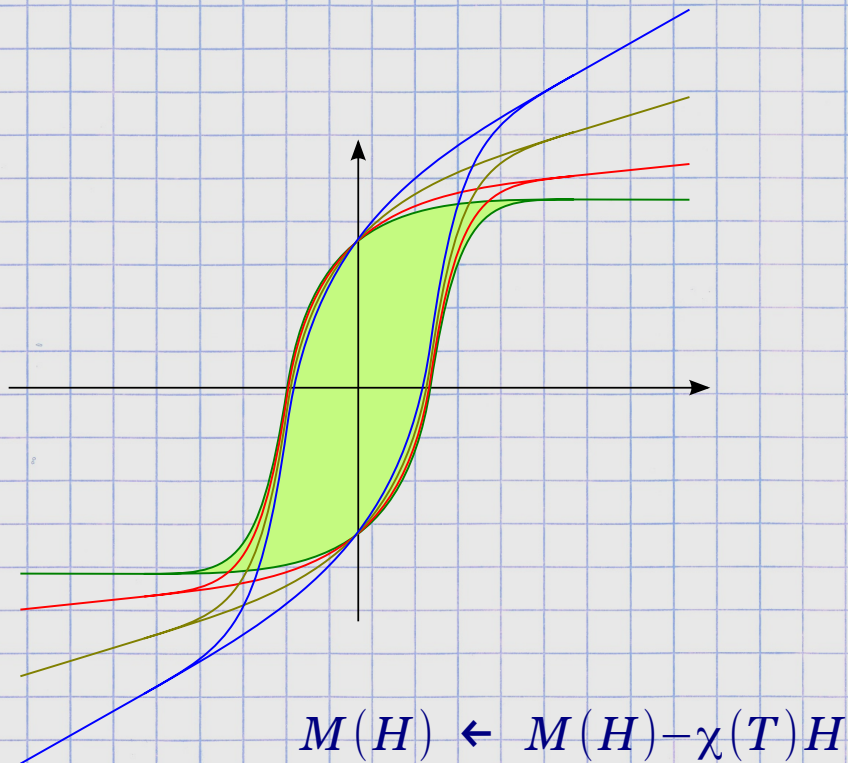
$$M(H) \leftarrow M(H) - \chi H$$

Problems :

- ⇒ Quantitative compensation a priori difficult
- ⇒ Approach to saturation difficult to investigate



Paramagnetic substrate / holder



Example:

- ⇒ 1nm ferro layer
- ⇒ 1ppm in 1mm support

- ⇒ Example : ions impurities in metals, and oxides
- ⇒ Problem : temperature dependent, non-linear



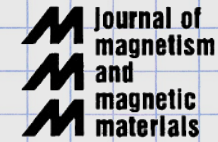
Paramagnetic substrate / holder



Available online at www.sciencedirect.com



Journal of Magnetism and Magnetic Materials 301 (2006) 50–66



www.elsevier.com/locate/jmmm

Magnetism of cigarette ashes

Neli Jordanova^{a,*}, Diana Jordanova^a, Bernard Henry^b, Maxime Le Goff^b,
Dimo Dimov^c, Tsenka Tsacheva^d

⇒ Be careful with : cleanliness, tweezers, holders, ink, etc.

Artifacts in various techniques

- ⇒ X-ray Magnetic Circular Dichroism (XMCD)
- ⇒ Magneto-Optical Kerr Effect (MOKE)
- ⇒ Lorentz microscopy
- ⇒ Etc.

Case of a bulk soft magnetic material

Hypotheses:

1. Use an ellipsoid, cylinder or slab along a main direction so that the demagnetizing field may be homogeneous.
2. Domains can be created to yield a uniform and effective magnetization M_{eff}

Density of energy:

$$E_{\text{tot}} = E_d + E_z$$

$$E_{\text{tot}} = \frac{1}{2} \mu_0 N M_{\text{eff}}^2 - \mu_0 M_{\text{eff}} H_{\text{ext}}$$

Minimization:

$$\frac{\partial E_{\text{tot}}}{\partial M_{\text{eff}}} = \mu_0 N M_{\text{eff}} - \mu_0 H_{\text{ext}} \Rightarrow$$

$$M_{\text{eff}} = \frac{1}{N} H_{\text{ext}}$$



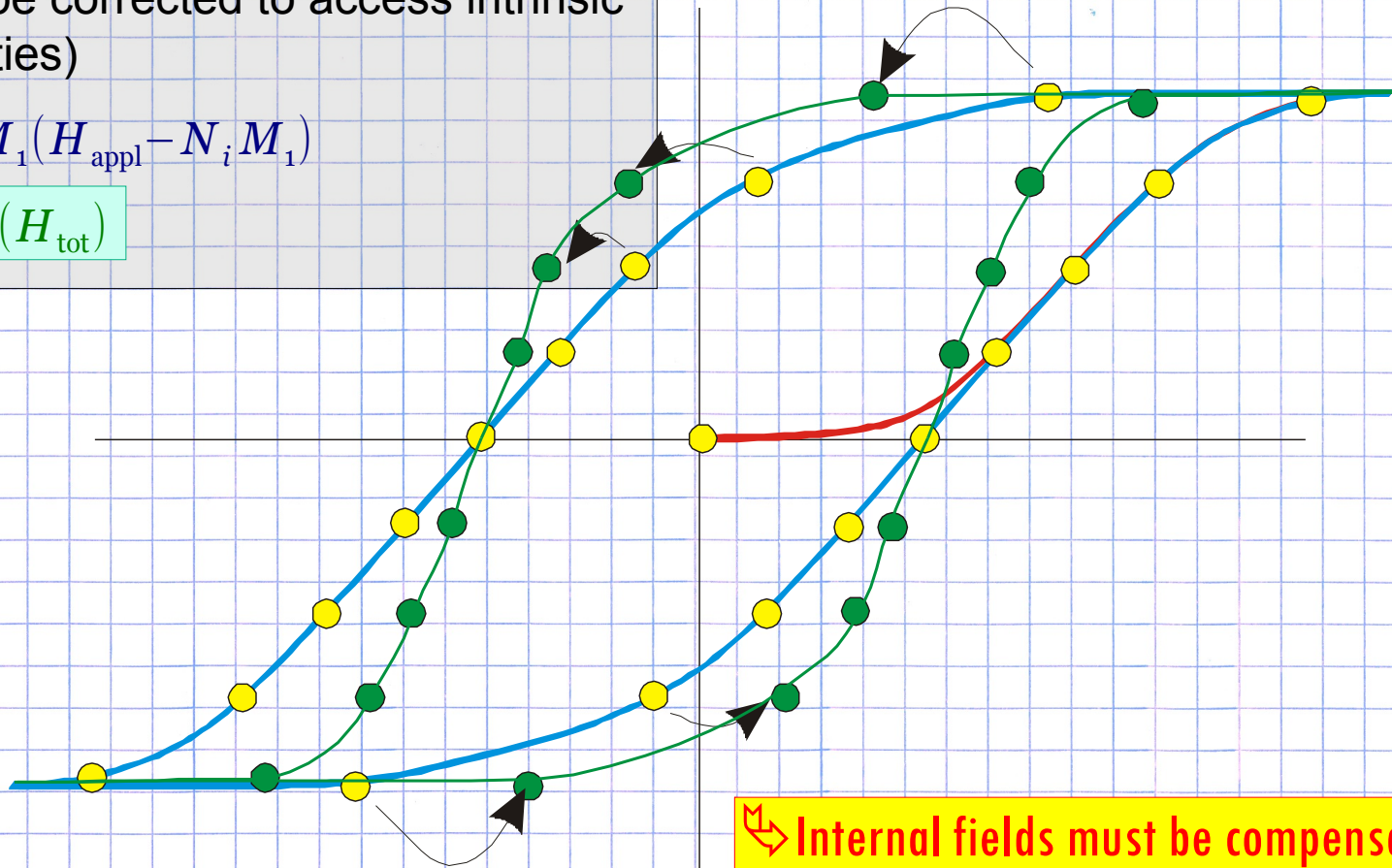
Conclusion for soft magnetic materials

➡ Susceptibility is constant and equal to $1/N$

Case of an arbitrary material

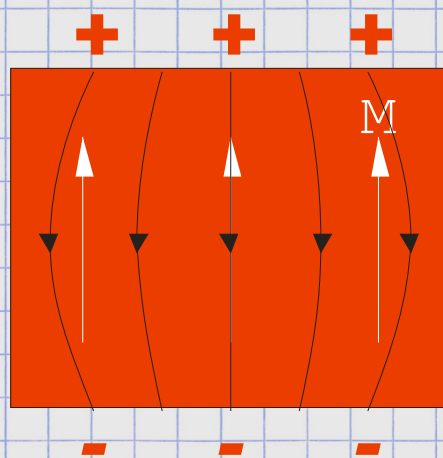
1. Measure a hysteresis loop $M_1(H_{\text{appl}})$
2. Internal field during loop: $H_d = -N_i M_1$
(must be corrected to access intrinsic properties)
3. Plot $M_1(H_{\text{appl}} - N_i M_1)$

➡ $M_2(H_{\text{tot}})$



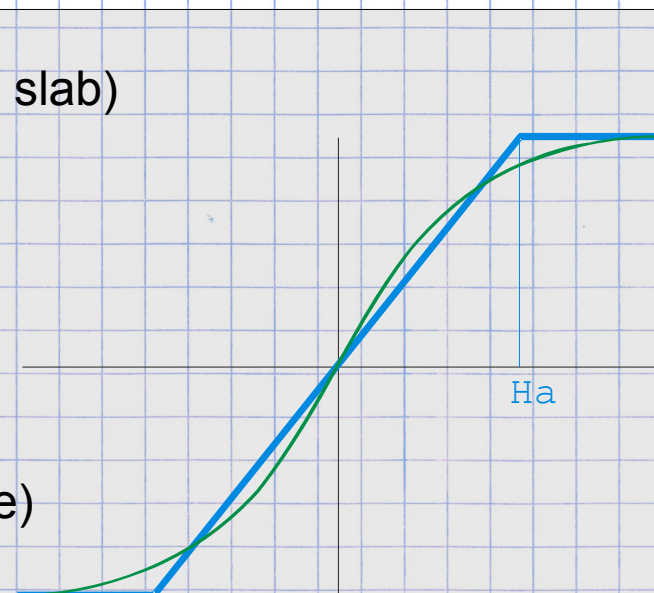
➡ Internal fields must be compensated

Specific aspects to systems with non-ellipsoidal shapes



In a non-ellipsoidal (or cylindrical, slab) system the demagnetizing field is not homogeneous in magnitude nor direction

1. Initial slope higher than $1/N$
(demag field smaller than average)
2. Late slope smaller than $1/N$
(demag field larger than average)



Demagnetizing energy (thus area above loop) is identical $\mathcal{E}_d = \int_0^{M_s} \mu_0 H_{\text{ext}} dM = \frac{1}{2} \mu_0 N M_s^2$

➡ In a non-ellipsoidal sample (or cylinder, slab) the loop is overcompensated at low magnetization and undercompensated at high field, even for soft magnetic materials.

➡ This effect adds up to the previous effect of grain shape

P. O. Jubert, O. Fruchart et al., *Europhys. Lett.* **63**, 102-108 (2003)



- ⇒ Extract loop and moments
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Magnetization loop of a macrospin along a hard axis

$$e = \sin^2 \theta - 2h \cos(\theta - \theta_H)$$

Dipolar energy:

$$e = \mathcal{E} / KV$$

$$h = H / H_a$$

$$H_a = 2K / \mu_0 M_s$$

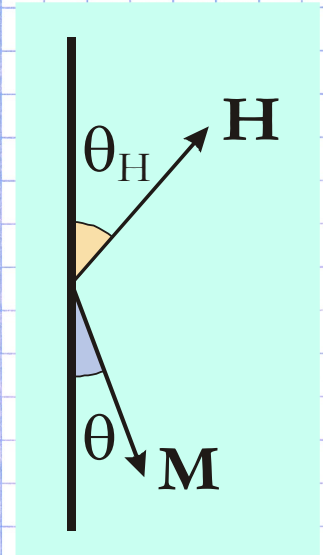
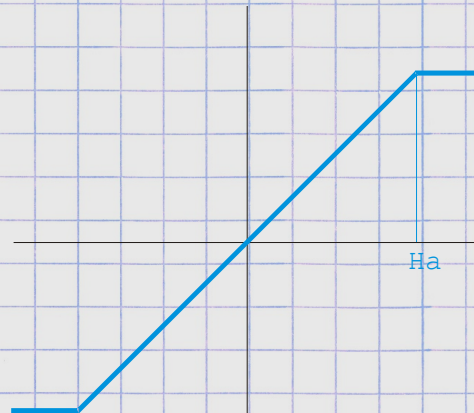
$$e = \sin^2 \theta - 2h \sin(\theta)$$

Hard axis: $\theta_H = \pi/2$

$$\partial_\theta e = 2 \cos \theta (\sin \theta - h)$$

$$h = \sin \theta = \cos(\theta - \theta_H) = \mathbf{m} \cdot \mathbf{u}_h$$

Equilibrium position

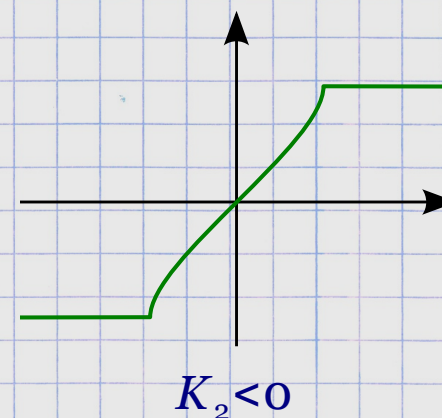
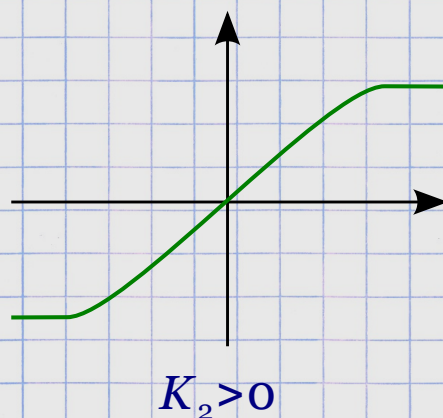
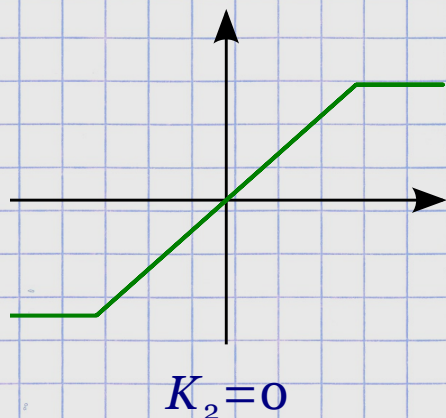




Loops

$$E_{mc} = K_1 \sin^2 \theta + K_2 \sin^4 \theta + \dots$$

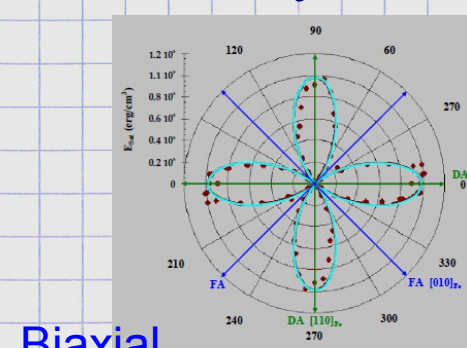
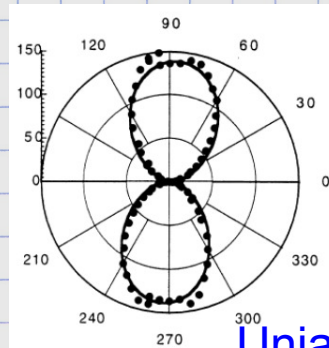
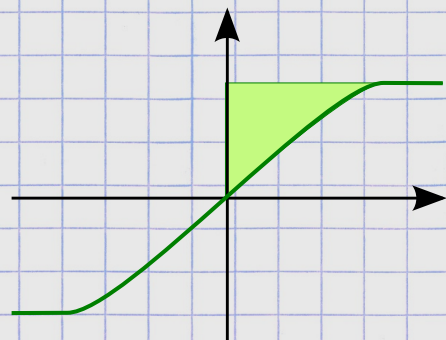
$$K_1 > 0$$



Means of analysis

⇒ Fit curve $H(M)$ (is analytical)

⇒ Initial susceptibility + saturation or area above curve as $E_{sat} - E_o = \mu_o \oint (\mathbf{H} \cdot d\mathbf{M})$





Distribution

- ⇒ Use area above curve
- ⇒ Singular point detection for saturation field

G. Asti et al., J. Appl. Phys. 45, 3600 (1974)

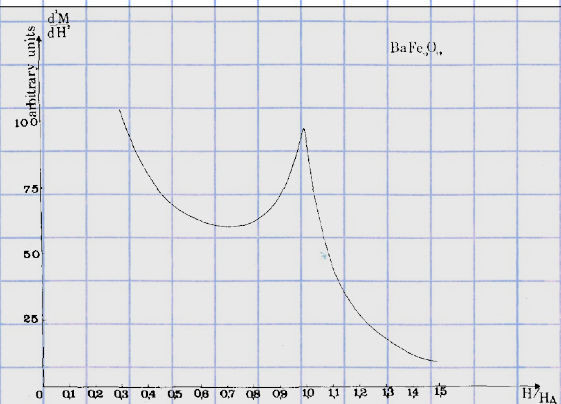
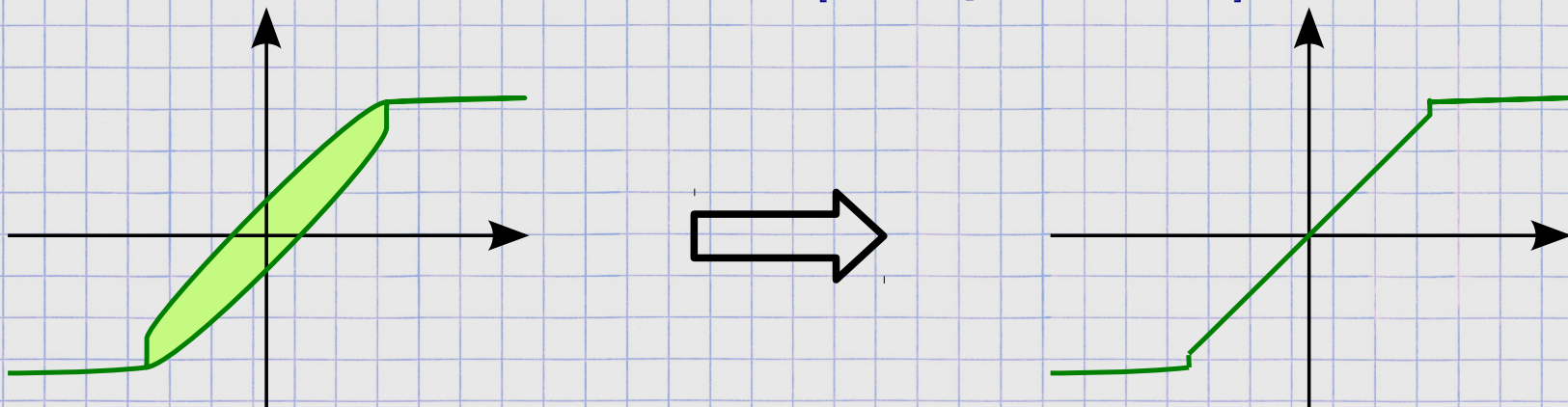


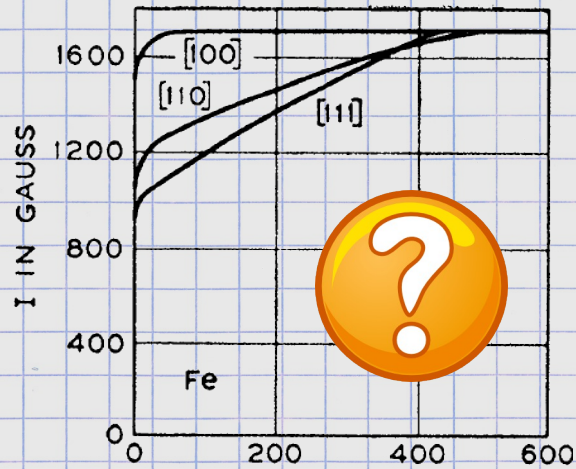
FIG. 5. Experimental plot of d^2M/dH^2 vs $H = H_{\text{ext}} - NM$ for an isotropic polycrystalline sample of $\text{BaFe}_{12}\text{O}_{19}$. H_{ext} is the applied field, and N denotes the demagnetizing factor of the sample.

Residual hysteresis

- ⇒ Compute anhysteretic curve $M(H) \rightarrow [M(H_{\text{up}}) + M(H_{\text{down}})]/2$



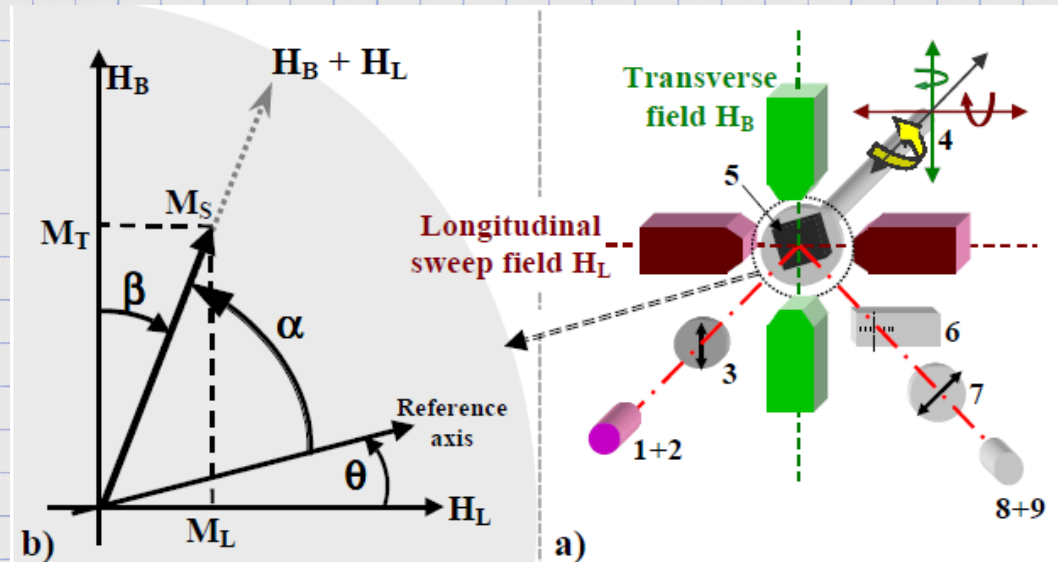
Issue



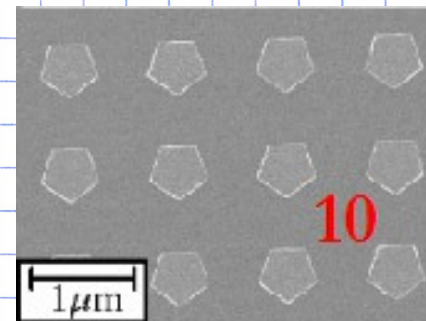
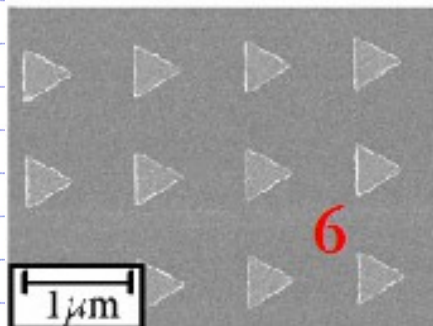
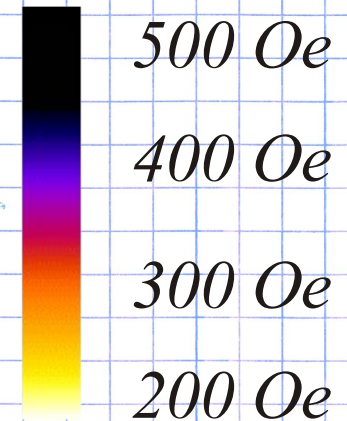
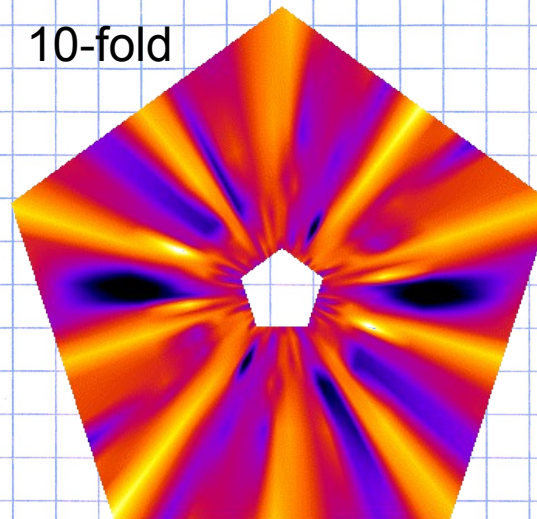
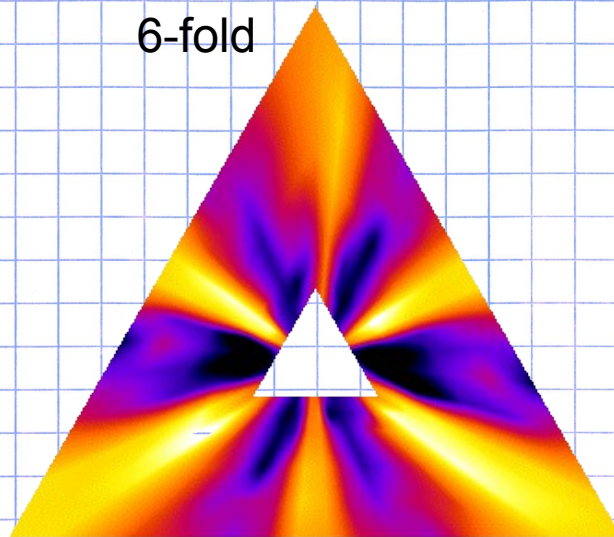
- ➡ High remanence in all directions
- ➡ Fit over small part of loop
→ sensitive to imperfections
- ➡ Solution : loop under transverse bias field

Solution

TBIIST: Transverse Bias Initial Inverse Susceptibility and Torque



D. Berling, J. Magn. Magn. Mater. 297, 118 (2006)



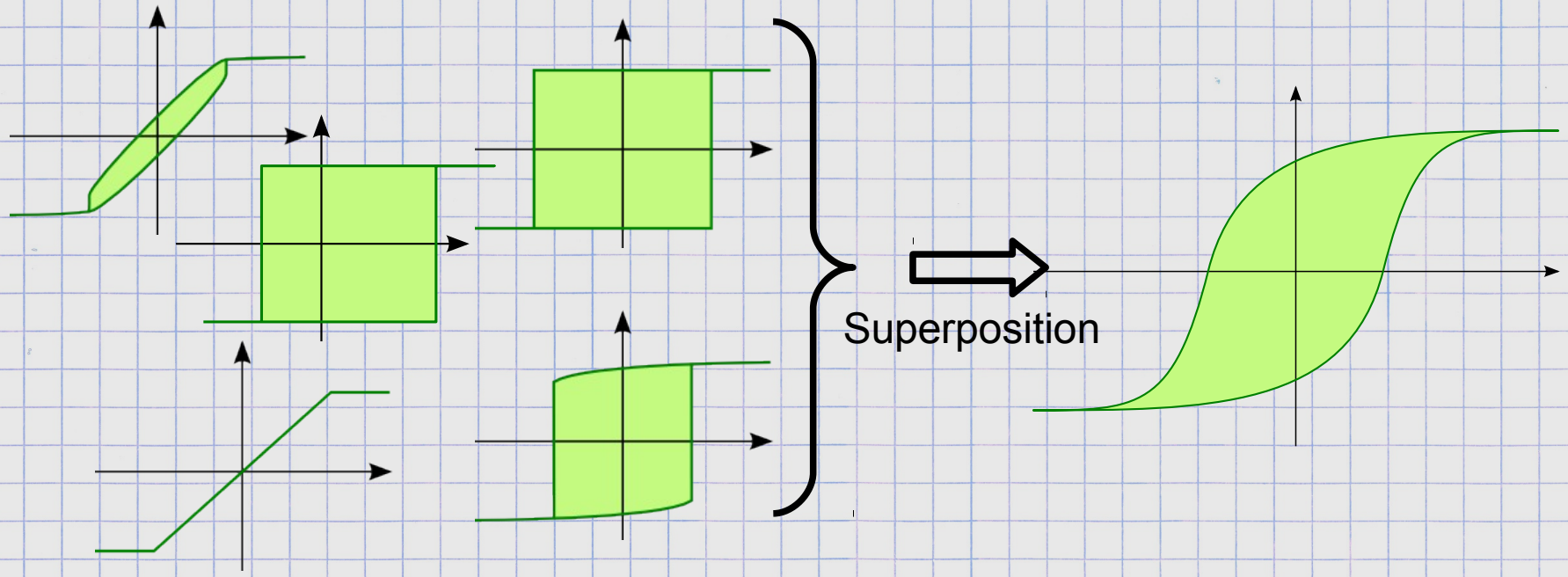
R.P. Cowburn, J.Phys.D:Appl.Phys.33, R1–R16 (2000)



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Physics : coercivity determined dual grains

⇒ Different loops with distribution



Possible effects that may arise

- Distribution of coercive fields
- (Dipolar) interactions
- The loops of the macrospins are slanted



Textbook case

- ⇒ Uniaxial anisotropy, second order : $E_{mc} = K \sin^2 \theta$
- ⇒ Fully remanent grains

3D distribution

- ⇒ Remanence : $m_r^{3D} = 1/2$
- ⇒ Measured anisotropy : $\langle K^{3D} \rangle = 2K/3$

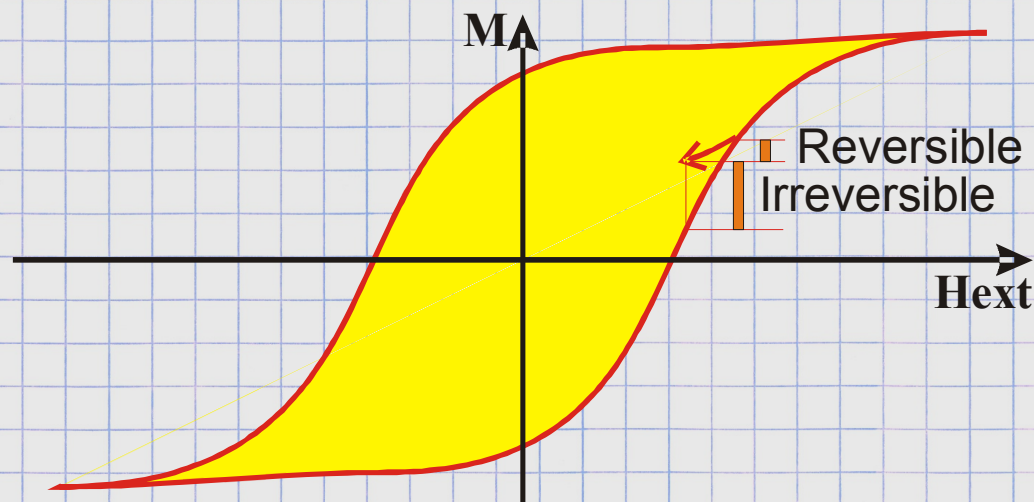
2D distribution

- ⇒ Remanence : $m_r^{3D} = 2/\pi$
- ⇒ Measured anisotropy : $\langle K^{3D} \rangle = K/2$

Use

- ⇒ Distribution : estimate K
- ⇒ Interactions : impact on increased or decreased remanence

Distribution of properties



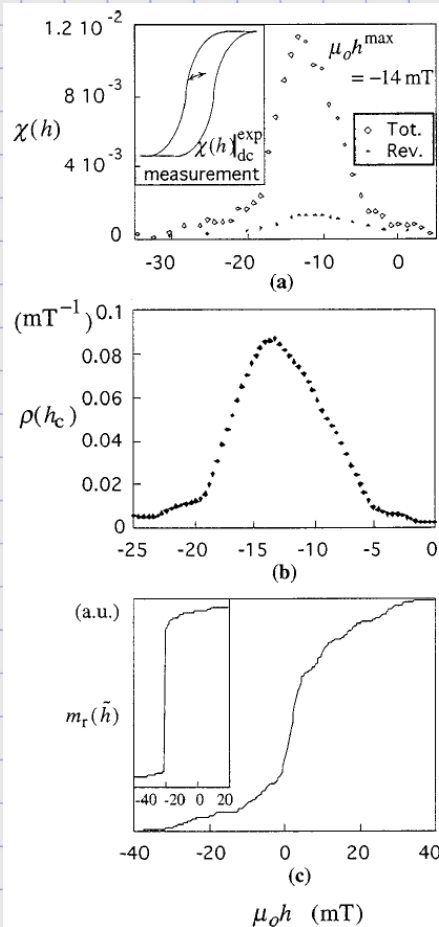
$$\rho(H_r) = \left. \frac{dm}{dH} \right|_{\text{irreversible}}$$

H_c(T) for a given population of the distribution can be studied at a given stage of the reversal (10%, 20% etc.)

Effect of distributions and dipolar interactions are sometimes difficult to disentangle

Reconstruct average single hysteresis loop

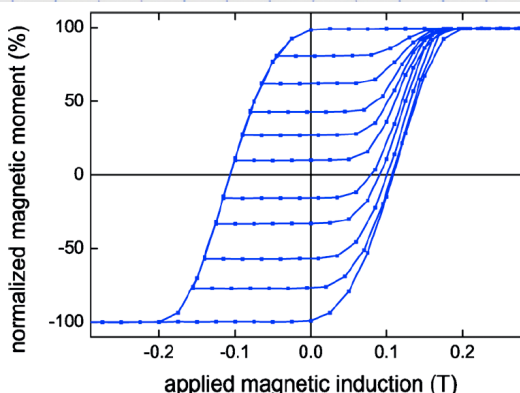
Ultrathin Fe(110) dots



O. Fruchart et al.,
Phys. Rev. B 57, 2596 (1998)

Susceptibility or distribution ?

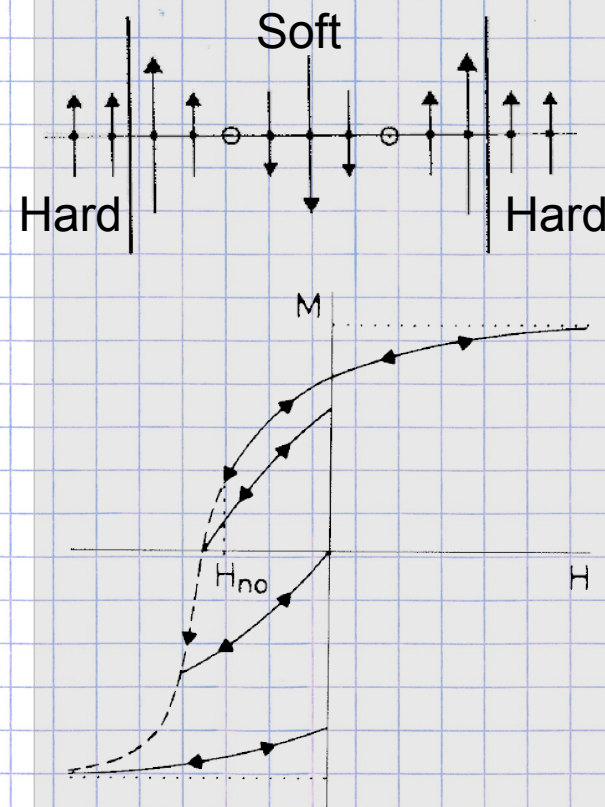
Arrays of electroplated parallel Ni nanowires



S. Da-Col et al.,
Appl. Phys. Lett. 98,
112501 (2011)

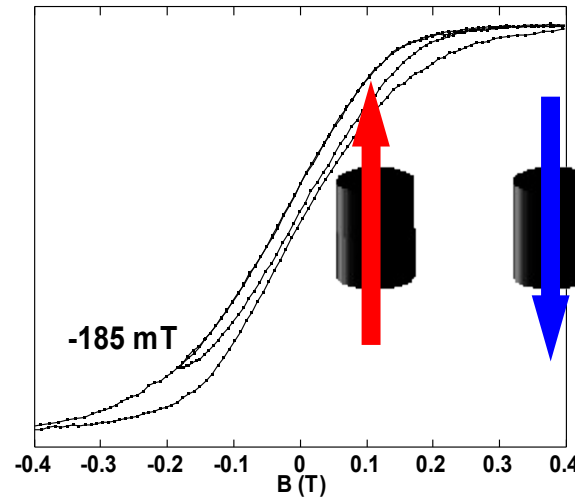
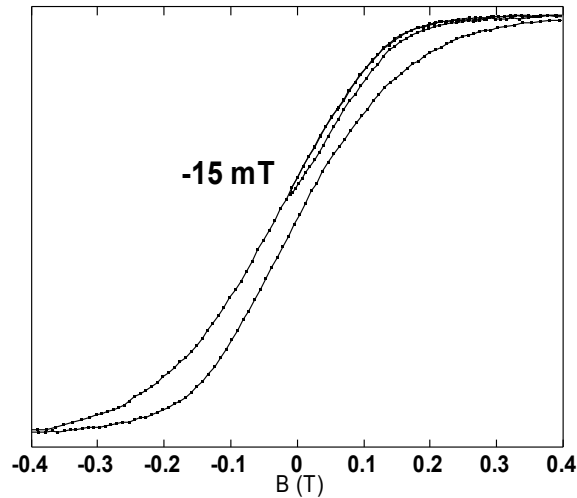
Scrutinize multiphased materials

Exchange-spring magnets

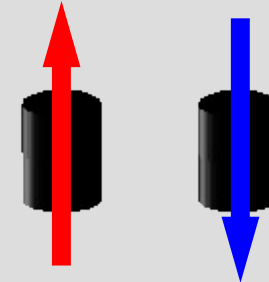


E. Kneller et al.,
IEEE Trans. Magn. 27,
3588 (1991)

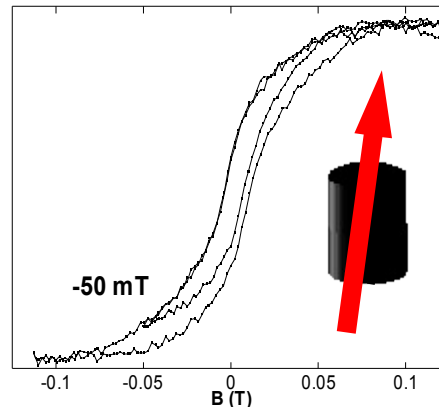
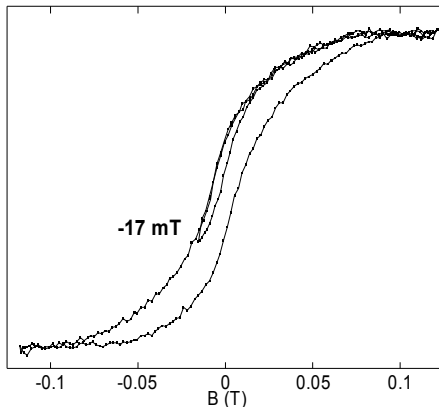
Minor loops: negative interactions



Example: dipolar interactions in arrays of Co/Au(111) pillars



Minor loops: negligible interactions

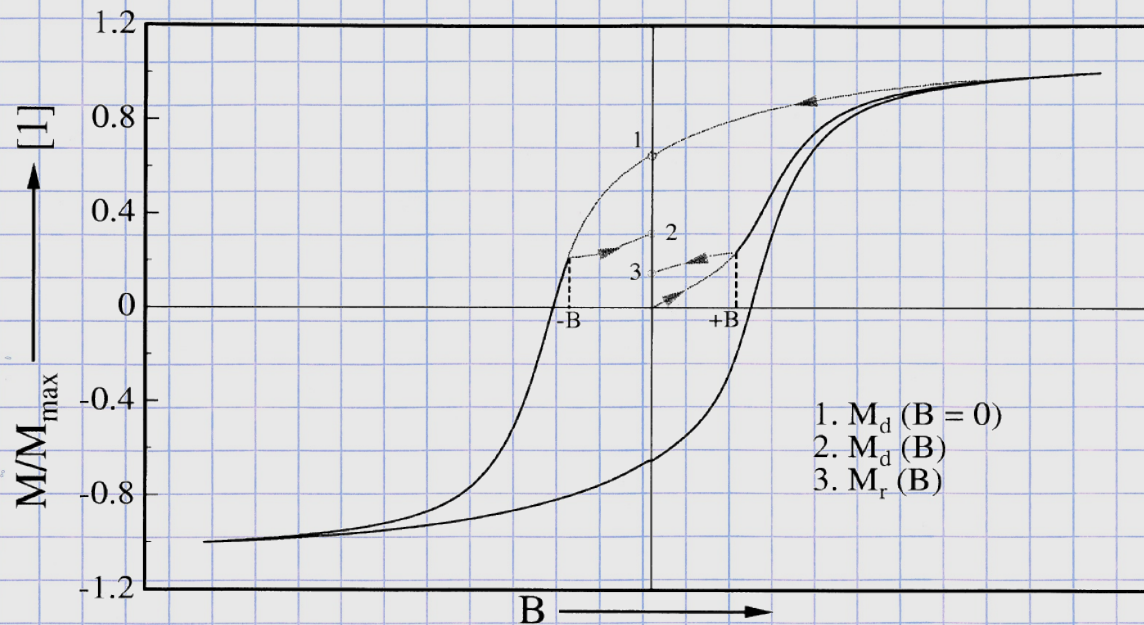


↪ Faster than Henkel and Preisach
↪ Other applications: characterization of exchange bias

O. Fruchart et al., unpublished



Henkel plots



O. Henkel,
Phys. Stat. Sol. 7, 919 (1964)
S. Thamm et al.,
JMMM184, 245 (1998)

Fig. 1. Explanation of how to measure the two different remanent magnetisations M_r and M_d .

Measure of dipolar interactions

$$\Delta M_H(x) = M_d(x) - [1 - 2M_r(x)]$$

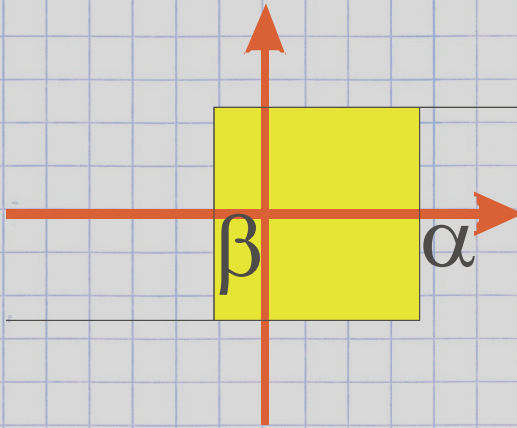
↪ The analysis of interactions on qualitative

↪ Long experiments (ac demagnetization)

Preisach model

G. Biorci et al., *Il Nuov. Cim.* VII, 829 (1958)

I. D. Mayergoyz, *Mathematical models of hysteresis*, Springer (1991)

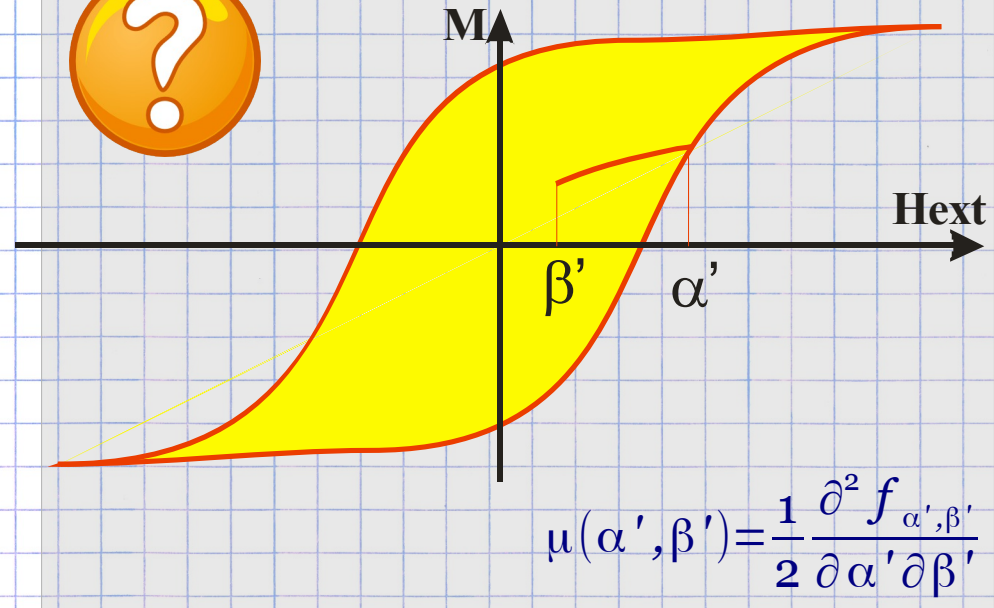


⇒ Distribution function

$\mu(\alpha, \beta)$ with $\alpha > \beta$

⇒ No true link between real particles and μ

Solving



⇒ Long experiments (1D set of hysteresis curves)

⇒ Better suited to bulk materials with strong interactions



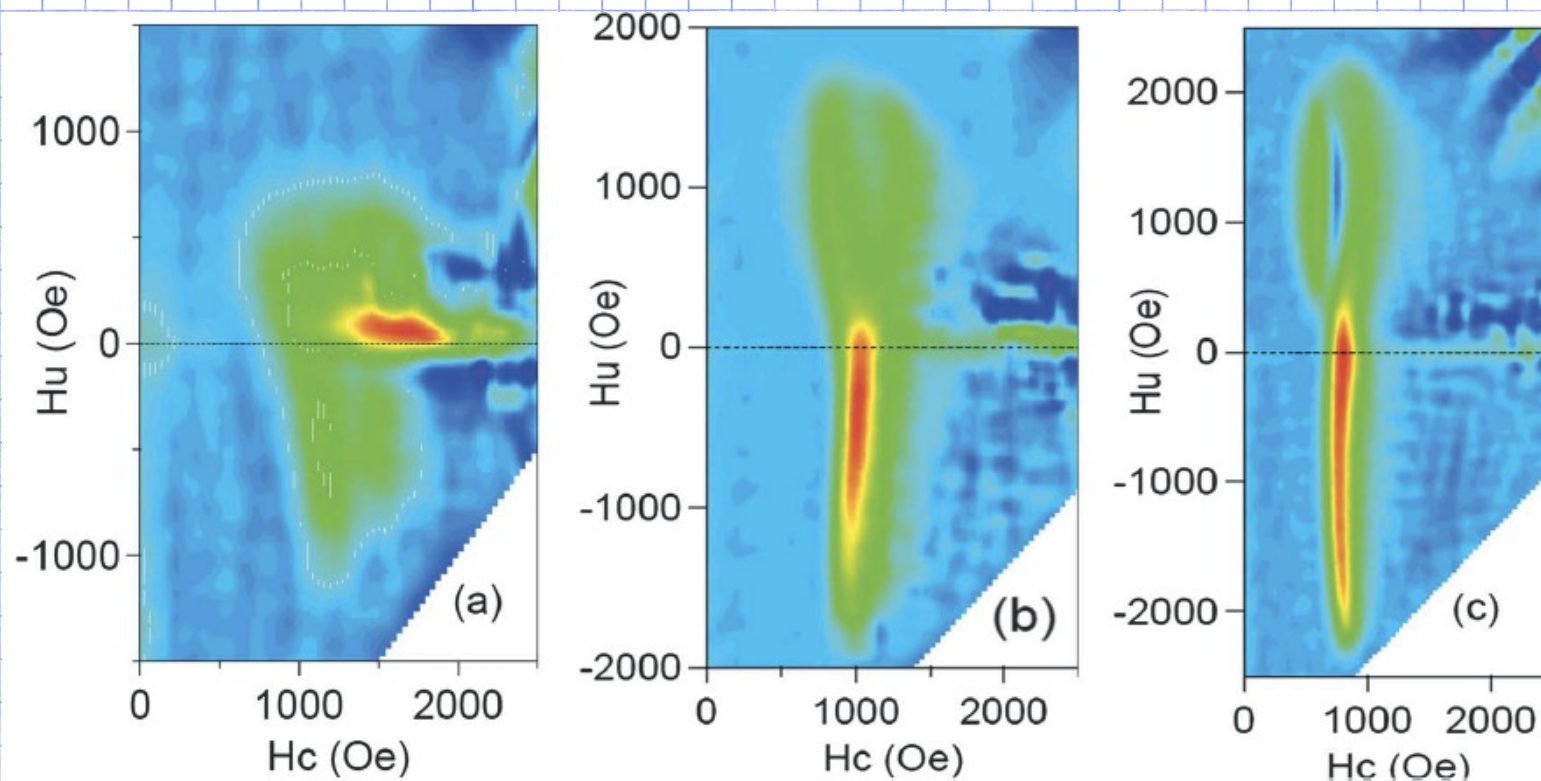
Recent 'rediscovery' or 're-interpretation' : the FORC diagrams:

First-Order Reversal Curves

→ Outline distribution of switching field and bias field

C. Pike et al., J. Appl. Phys. 85, 6668 (1999)

Ex : arrays of parallel permalloy nanowires wire increasing diameter



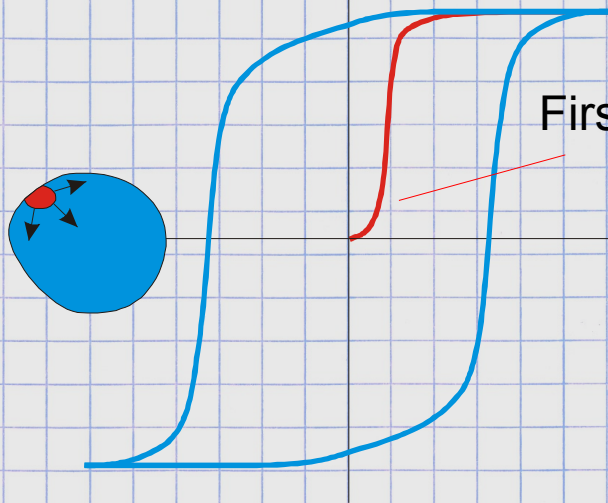
M. S. Salem et al., J. Mater. Chem. 22, 8549 (2012)



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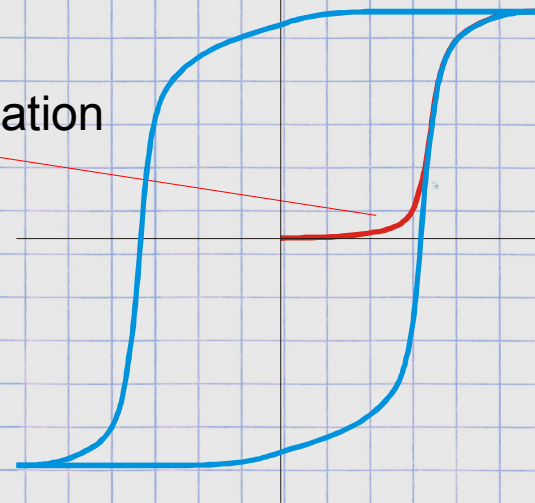


Use first-magnetization curves to determine the type of coercivity



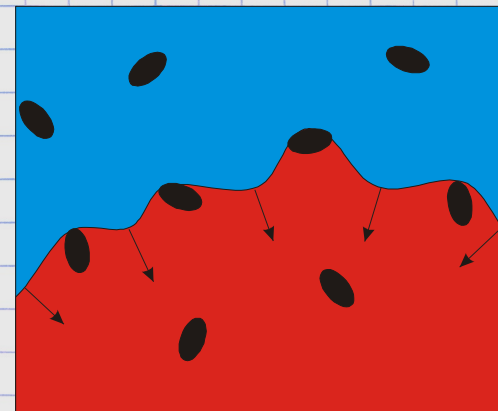
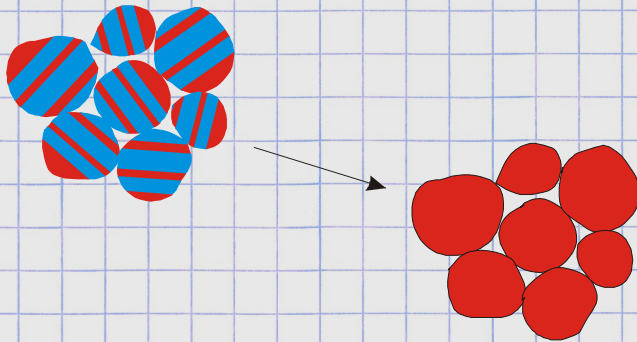
Nucleation-limited

Ex: $\text{Sm}_2\text{Co}_{17}$



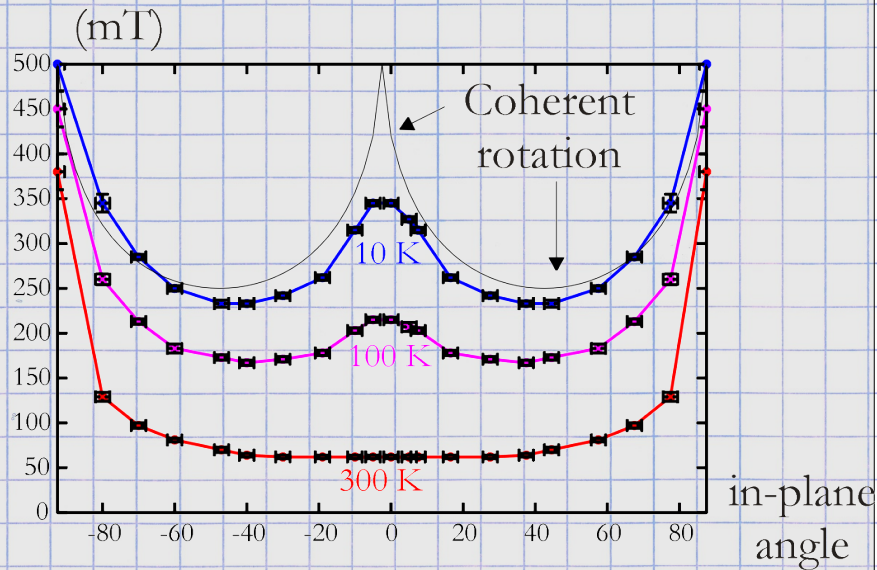
Propagation-limited

Ex: SmCo_5



Max(H_c) for easy axis $\rightarrow$ nucleation

Ultrathin uniaxial Fe(110) dots



O. Fruchart et al.,
Phys. Rev. Lett. 82, 1305-1308 (1999)

$1/\cos\theta_H$ law $\rightarrow$ propagation

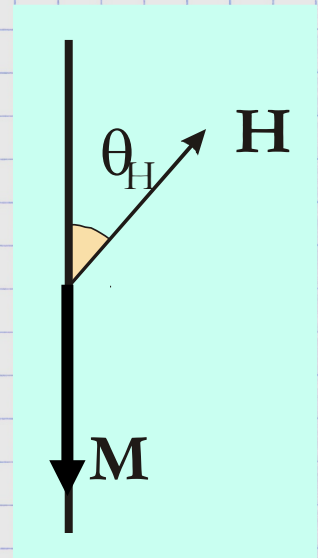
E. J. Kondorsky, J. Exp. Theor. Fiz. 10, 420 (1940)

Hypothesis:

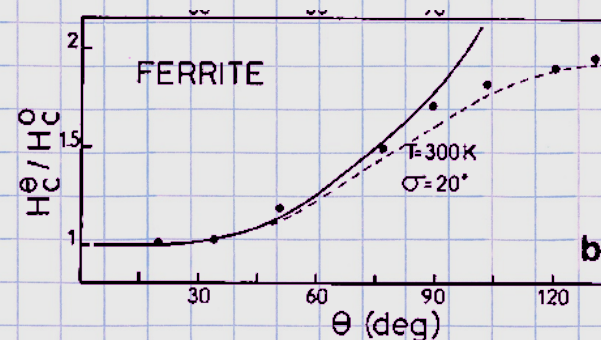
$\Rightarrow$ Based on nucleation volume

$\Rightarrow H_c \ll H_a$

Energy barrier E_0
overcome by gain in
Zeeman energy plus
thermal energy



$$E_0 = -\mu_0 M_s v_a H \cos\theta_H + 25k_B T$$



D. Givord et al., JMMM72, 247 (1988)



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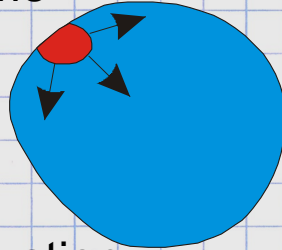


Activation volume

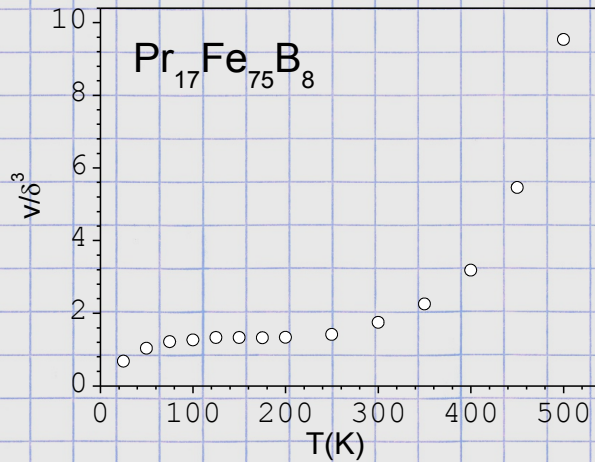
Also called: nucleation volume

Can be used for:

- ⇒ Estimating $H_c(T)$
- ⇒ Estimating long-time relaxation
- ⇒ Determination of dimensionality



Note: of the order of domain wall width δ

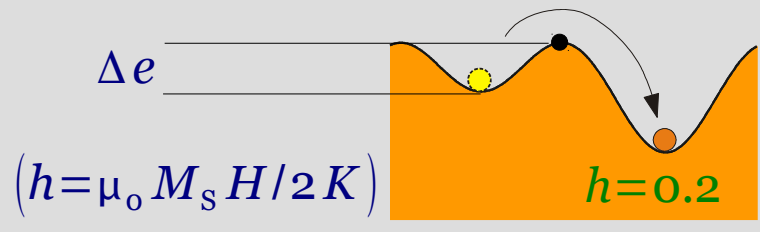


More detailed models:

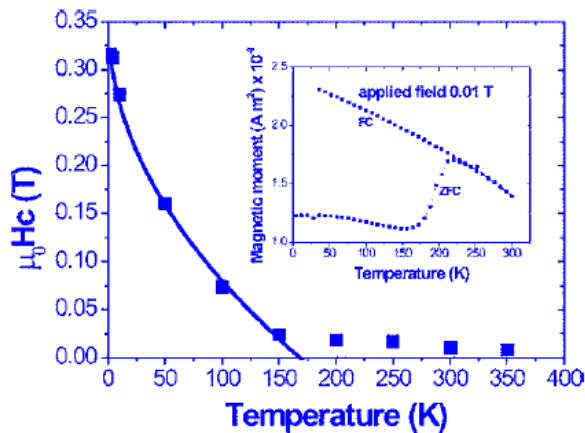
D. Givord et al., JMMM258, 1 (2003)

Barrier height

$$\Delta e = e(\theta_{\max}) - e(0) = (1-h)^2$$



J. Appl. Phys. **99**, 08Q514 (2006)



Thermal activation

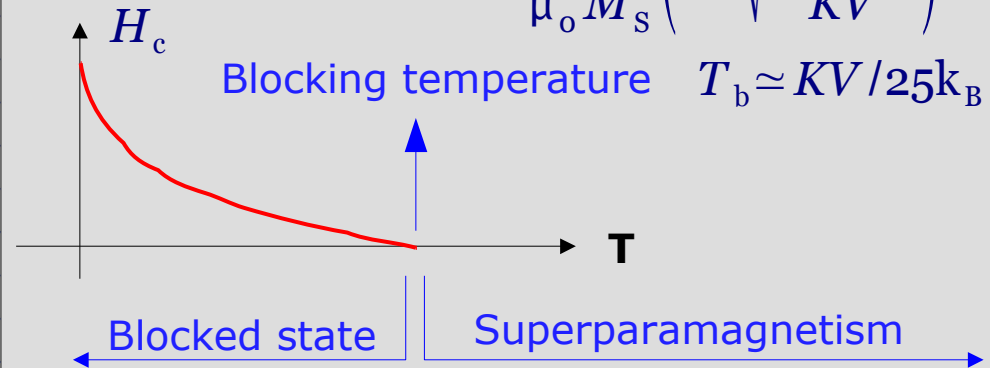
Brown, Phys.Rev.130, 1677 (1963)

$$\tau = \tau_0 \exp\left(\frac{\Delta \mathcal{E}}{k_B T}\right) \quad \Rightarrow \quad \Delta \mathcal{E} = k_B T \ln(\tau / \tau_0)$$

$$\tau_0 \approx 10^{-10} \text{ s}$$

Lab measurement: $\tau \approx 1 \text{ s} \Rightarrow \Delta \mathcal{E} \approx 25 k_B T$

$$\Rightarrow H_c = \frac{2K}{\mu_0 M_s} \left(1 - \sqrt{\frac{25 k_B T}{KV}}\right)$$



E. F. Kneller, J. Wijn (ed.) Handbuch der Physik XIII/2: Ferromagnetismus, Springer, 438 (1966)

M. P. Sharrock, J. Appl. Phys. 76, 6413-6418 (1994)

Notice, for magnetic recording : $\tau \approx 10^9 \text{ s}$ $KV_b \approx 40 - 60 k_B T$



Formalism

C. P. Bean & J. D. Livingston, J. Appl. Phys. 30, S120 (1959)

$$\mathcal{E} = KV f(\theta, \varphi) - \mu_0 \mu H$$

Partition function

$$Z = \sum \exp(-\beta \mathcal{E})$$

Average moment

$$\langle \mu \rangle = \frac{1}{\beta \mu_0 Z} \frac{\partial Z}{\partial H}$$

Isotropic case

$$Z = \int_{-\mathcal{M}}^{\mathcal{M}} \exp(\beta \mu_0 \mu H) d\mu$$

Note: equivalent to integration over solid angle

$$\langle \mu \rangle = \mathcal{M} \left[\coth\left(x - \frac{1}{x}\right) \right]$$

Langevin function

Note:

Use the moment $\mathcal{M}$ of the particule, not spin $\frac{1}{2}$.

$$x = \beta \mu_0 \mathcal{M} H$$

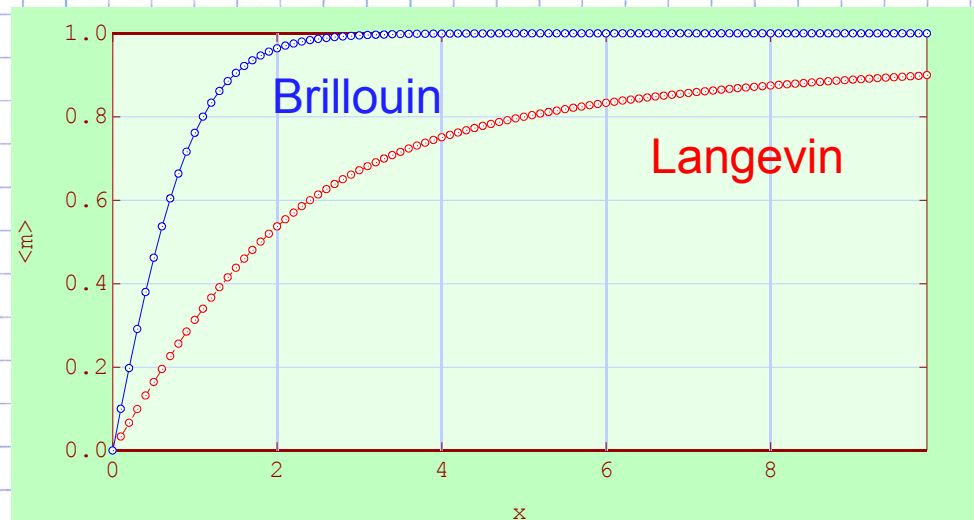


Infinite anisotropy

$$Z = \exp(\beta \mu_0 \mathcal{M} H) + \exp(-\beta \mu_0 \mathcal{M} H)$$

$$\langle \mu \rangle = \mathcal{M} \tanh(x)$$

Brillouin $\frac{1}{2}$ function



REVIEW : S. Bedanta & W. Kleemann, Supermagnetism, J. Phys. D: Appl. Phys., 013001 (2009)