

# Magnetization textures and processes

Olivier FRUCHART

Univ. Grenoble Alpes / CEA / CNRS, SPINTEC, France

Email to [esm@grenoble.cnrs.fr](mailto:esm@grenoble.cnrs.fr) on Aug.19 2009 18:55

## More practicals ahead

Hi,

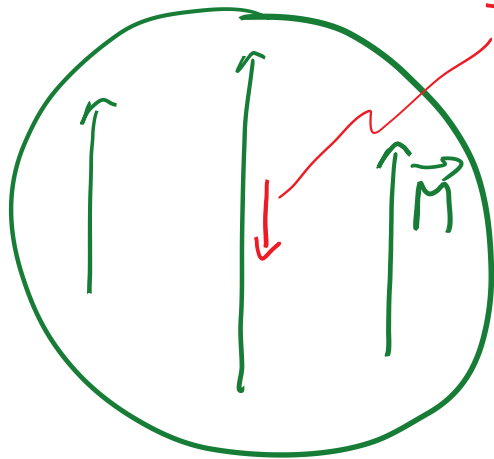
I was investigating about magnetism in the human body and I used a speaker with a plug connected to it and then I started touching my body with the plug to hear how it sounds, I realized that when I put the plug in my nipples it made a louder sound which means that the magnetics were bigger in that area, I have asked about this but I get no answer why, there is no coverage about this subject on the internet either, please if you know about this let me know, **my theory is that our nipples are our bridge of expulsing magnetics and electric signal to control the energy outside our bodies**, hope this helps with some research, thank you...

Xxx YYY

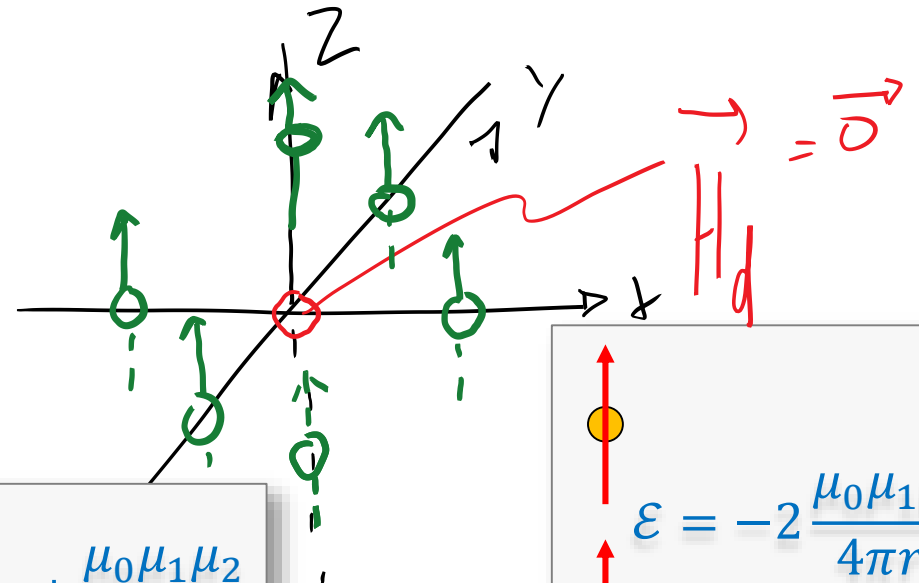
A volunteer to track  
my mistakes?  
(Please)

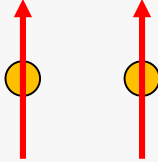
## Quizz #1

I can prove that demagnetizing field does NOT exist!

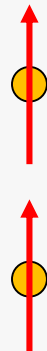


$$-\frac{1}{3}\vec{M}$$





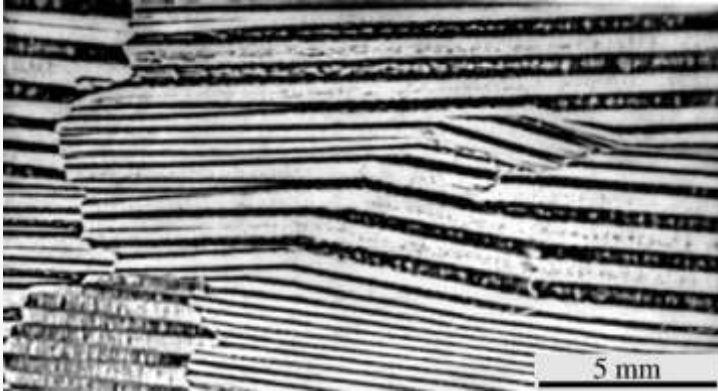
$$\varepsilon = + \frac{\mu_0 \mu_1 \mu_2}{4\pi r^3}$$



$$\varepsilon = -2 \frac{\mu_0 \mu_1 \mu_2}{4\pi r^3}$$

## Magnetic domains

- ❑ Numerous and complex shape of domains



History: Weiss domains

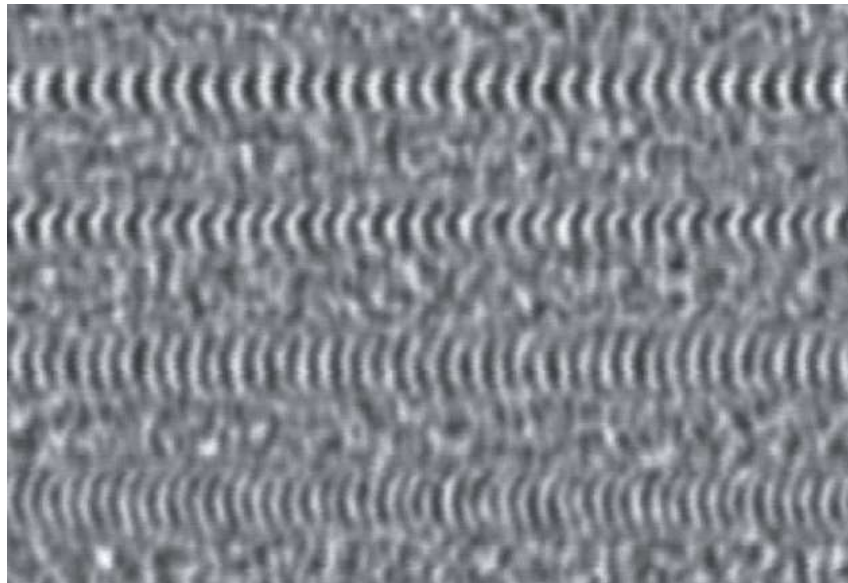
Practical: improve material properties





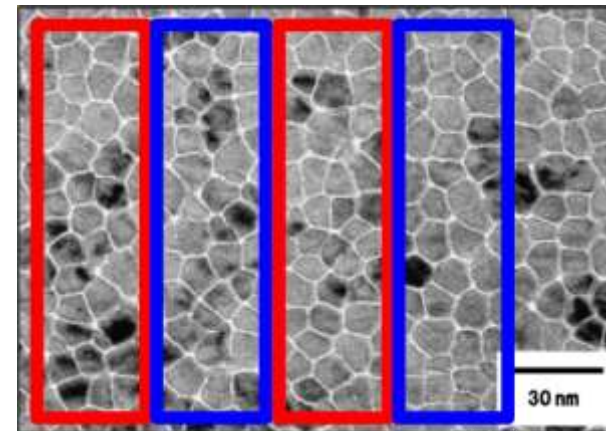
## Magnetic bits on hard disk drives

Co-based hard disk media : bits 50nm and below

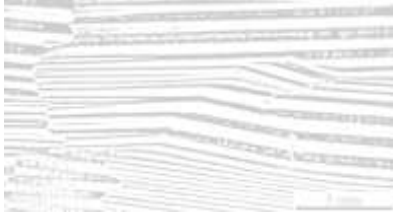


B. C. Stipe, Nature Photon. 4, 484 (2010)

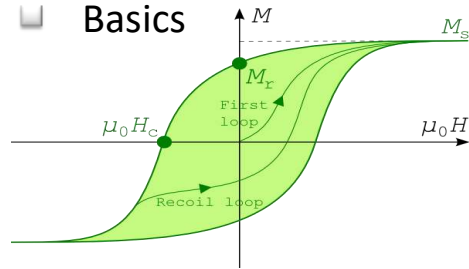
## Underlying microstructure



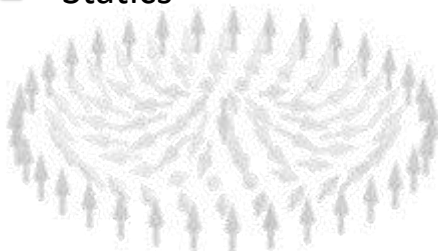
## Motivation



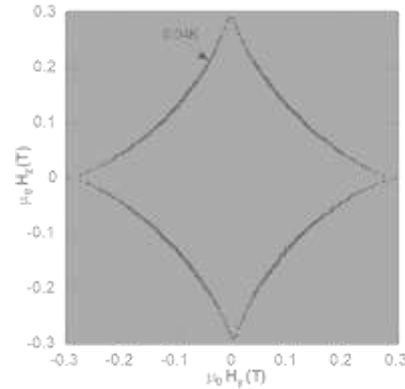
## Basics



## Statics



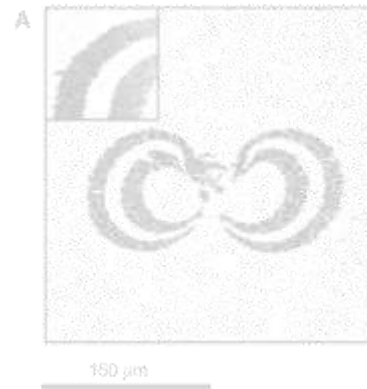
## Macrospin switching



## Extended systems



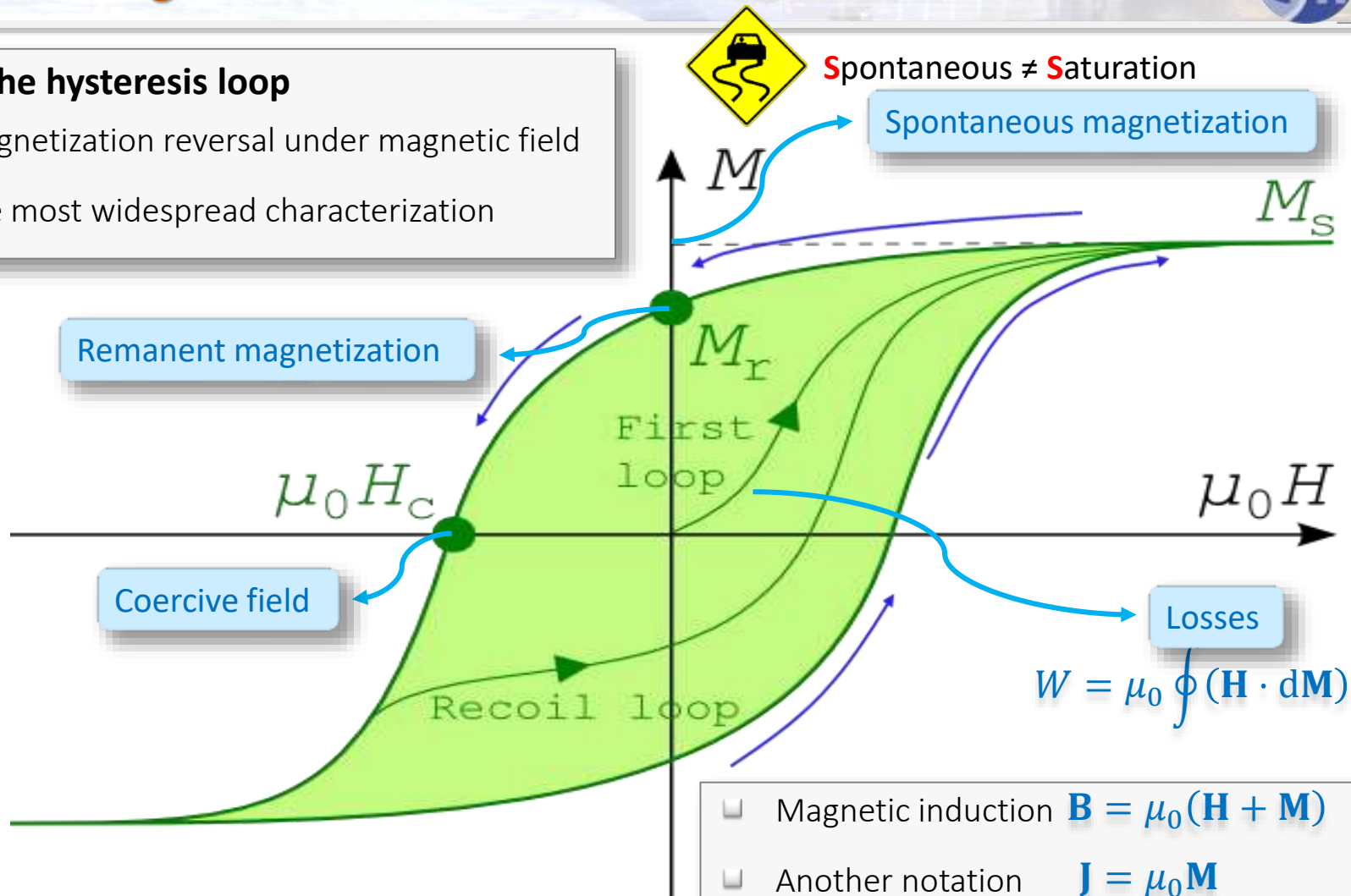
## Precessional dynamics



# Basics – Control magnetization reversal

## The hysteresis loop

- ❑ Magnetization reversal under magnetic field
- ❑ The most widespread characterization

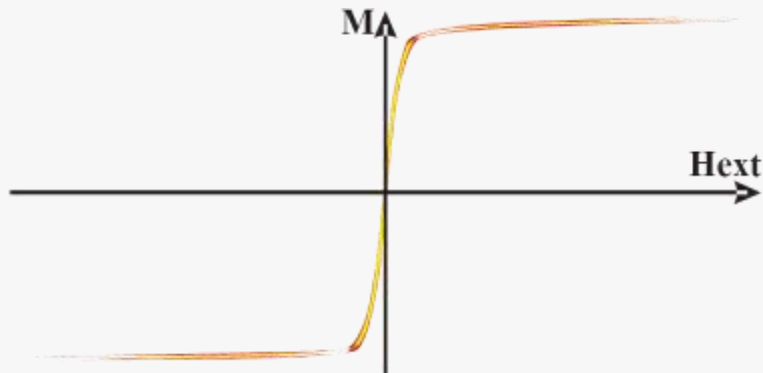


- ❑ Magnetic induction  $\mathbf{B} = \mu_0(\mathbf{H} + \mathbf{M})$
- ❑ Another notation  $\mathbf{J} = \mu_0\mathbf{M}$



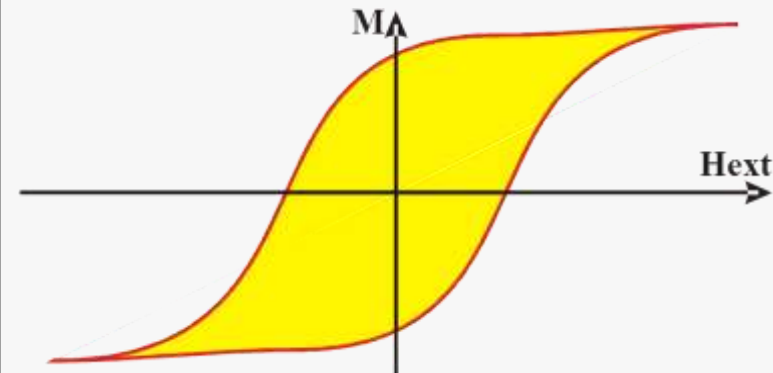
# Basics – Soft and hard magnetic materials

## Soft magnetic material



- ☐ Transformers
- ☐ Magnetic shielding, flux guides
- ☐ Magnetic sensors

## Hard magnetic material



- ☐ Magnetic recording
- ☐ Permanent magnets

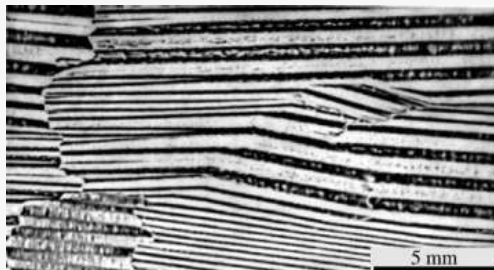
### What determines hysteresis loops?

- ☐ Material composition and crystal structure
- ☐ Microstructure

# Basics – Domains, from bulk to nano

## Bulk material

Numerous and complex shape of domains

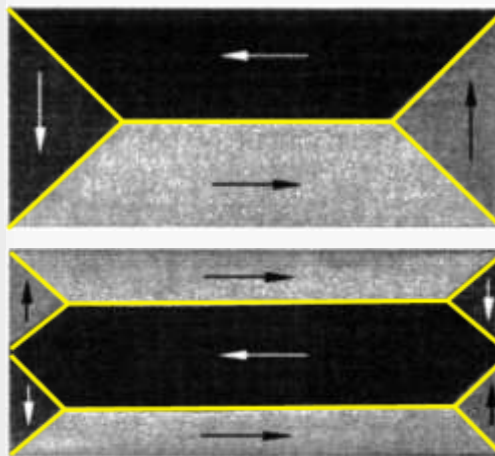


FeSi soft magnetic sheet

A. Hubert, Magnetic domains

## Mesoscopic scale

Small number of domains, simple shape

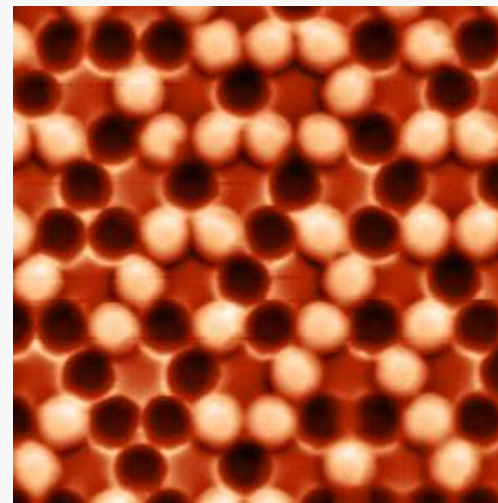


Microfabricated elements  
Kerr microscopy

A. Hubert, Magnetic domains

## Nanosopic scale

Magnetic single domain

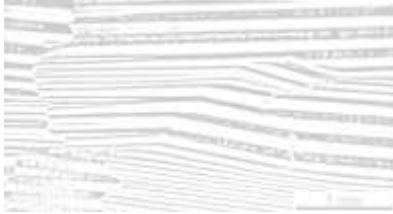


Nanofabricated dots  
MFM

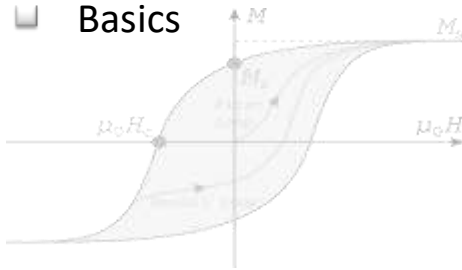
Sample courtesy:  
I. Chioar, N.Rougemaille

☐ Nanomagnetism  $\approx$  Mesomagnetism

## Motivation



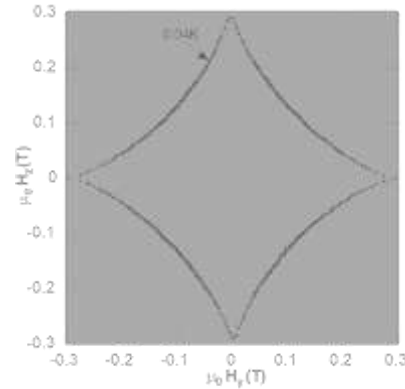
## Basics



## Statics



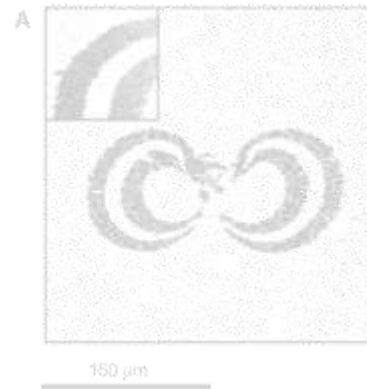
## Macrospin switching



## Extended systems



## Precessional dynamics



## Magnetization

### Magnetization vector $\mathbf{M}$

- Continuous function

- May vary over time and space

- Modulus is constant and uniform  
(hypothesis in micromagnetism)

$$\mathbf{M}(\mathbf{r}) = \begin{pmatrix} M_x \\ M_y \\ M_z \end{pmatrix} = M_s \begin{pmatrix} m_x \\ m_y \\ m_z \end{pmatrix}$$

$$m_x^2 + m_y^2 + m_z^2 = 1$$



Mean field approach is possible:  $M_s = M_s(T)$

## Exchange interaction

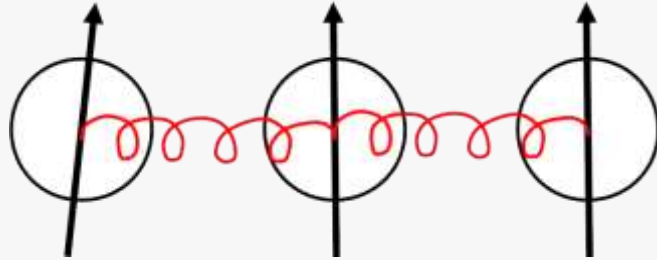
- Atomistic view  $\mathcal{E} = - \sum_{i \neq j} J_{i,j} \mathbf{S}_i \cdot \mathbf{S}_j$  (total energy, J)

- Micromagnetic view  $\mathbf{S}_i \cdot \mathbf{S}_j = S^2 \cos(\theta_{i,j}) \approx S^2 \left( 1 - \frac{\theta_{i,j}^2}{2} \right)$

$$E_{\text{ex}} = A(\nabla \cdot \mathbf{m})^2 = A \sum_{i,j} \left( \frac{\partial m_i}{\partial x_j} \right)^2$$

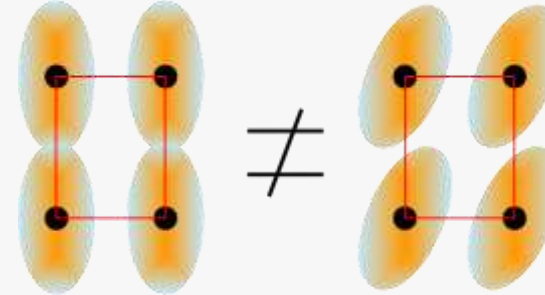
# Statics – The various types of magnetic energy

## Exchange energy



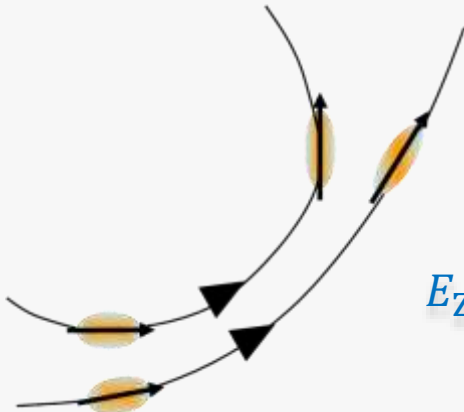
$$E_{\text{ex}} = A(\nabla \cdot \mathbf{m})^2 = A \sum_{i,j} \left( \frac{\partial m_i}{\partial x_j} \right)^2$$

## Magnetocrystalline anisotropy energy



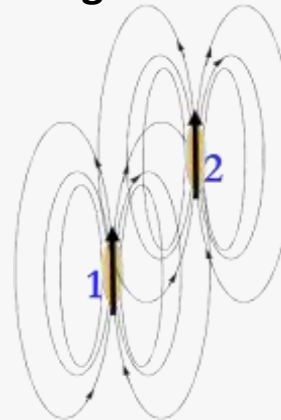
$$E_{\text{mc}} = K f(\theta, \varphi)$$

## Zeeman energy ( $\rightarrow$ enthalpy)



$$E_Z = -\mu_0 \mathbf{M} \cdot \mathbf{H}$$

## Magnetostatic energy



$$E_d = -\frac{1}{2} \mu_0 \mathbf{M} \cdot \mathbf{H}_d$$



# Statics – Dipolar energy

## Analogy with electrostatics

Maxwell equation  $\rightarrow \nabla \cdot \mathbf{H}_d = -\nabla \cdot \mathbf{M}$

$$\Rightarrow \mathbf{H}_d(\mathbf{r}) = -M_s \iiint_{V'} \frac{[\nabla \cdot \mathbf{m}(\mathbf{r}')] (\mathbf{r} - \mathbf{r}')}{4\pi |\mathbf{r} - \mathbf{r}'|^3} dV'$$

To lift the singularity that may arise at boundaries,  
a volume integration around the boundaries yields:

$$\mathbf{H}_d(\mathbf{r}) = \iiint \frac{\rho(\mathbf{r}') (\mathbf{r} - \mathbf{r}')}{4\pi |\mathbf{r} - \mathbf{r}'|^3} dV' + \iint \frac{\sigma(\mathbf{r}') (\mathbf{r} - \mathbf{r}')}{4\pi |\mathbf{r} - \mathbf{r}'|^3} dS'$$

## Magnetic charges

$\rho(\mathbf{r}) = -M_s \nabla \cdot \mathbf{m}(\mathbf{r}) \rightarrow$  volume density of magnetic charges

$\sigma(\mathbf{r}) = M_s \mathbf{m}(\mathbf{r}) \cdot \mathbf{n}(\mathbf{r}) \rightarrow$  surface density of magnetic charges

## Usefull expressions

$$\mathcal{E}_d = -\frac{1}{2} \mu_0 \iiint_V \mathbf{M} \cdot \mathbf{H}_d dV$$

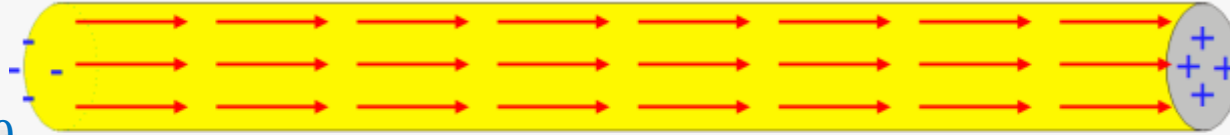
$$\mathcal{E}_d = \frac{1}{2} \mu_0 \iiint_V \mathbf{H}_d^2 dV$$

- ☐ Always positive
- ☐ Zero means minimum

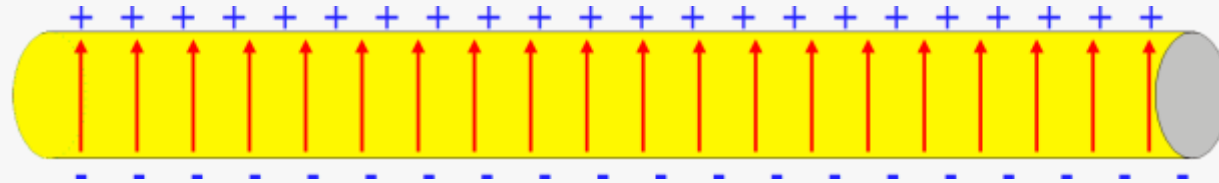
- ☐  $H_d$  depends on shape, not size
- ☐ Synonym: dipolar, magnetostatic

## Examples of magnetic charges

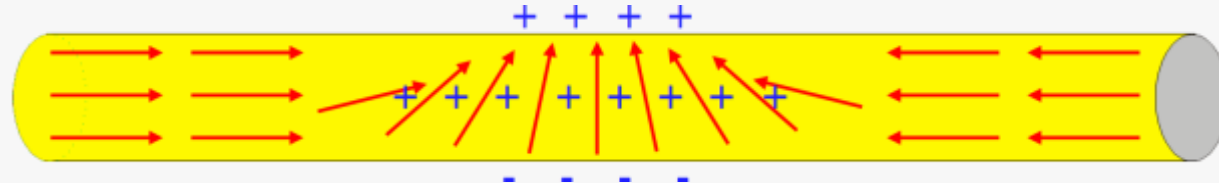
- Note for infinite cylinder:  
no charge  $\epsilon = 0$



- Charges on side surfaces

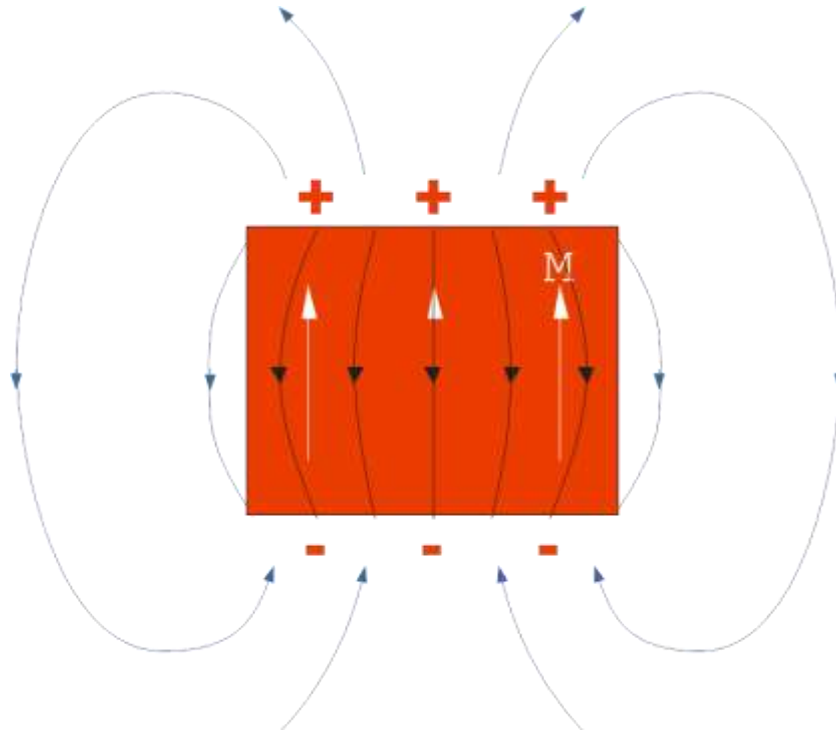


- Surface and volume charges



## Take-away message

- Dipolar energy favors alignment of magnetization with longest direction of sample



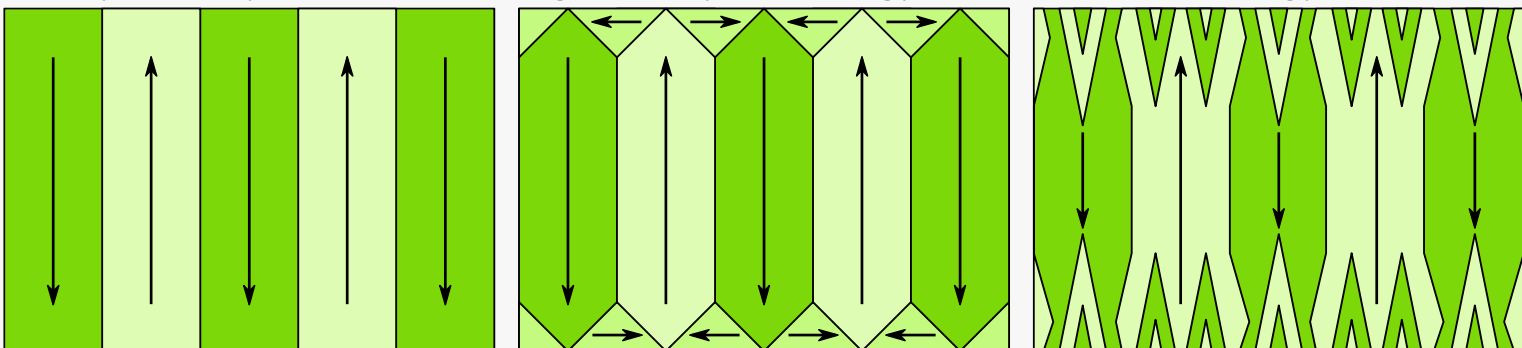
## Vocabulary

- Generic names
  - Magnetostatic field
  - Dipolar field
- Inside material
  - Demagnetizing field
- Outside material
  - Stray field

# Statics – Tendency for flux-closure domains

## Films with easy axis out-of-the-plane: Kittel domains

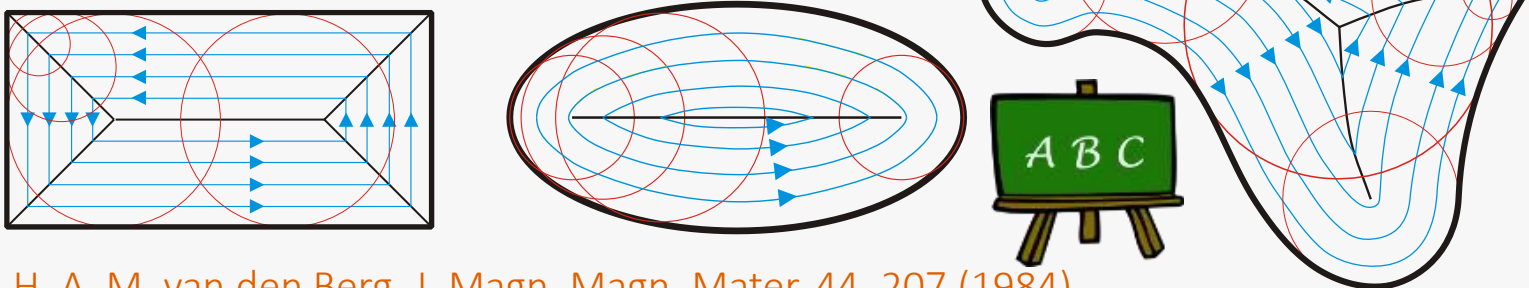
Principle: compromise between gain in dipolar energy, and cost in wall energy



C. Kittel, Physical theory of ferromagnetic domains, Rev. Mod. Phys. 21, 541 (1949)

## Nanostructures with in-plane magnetization – Van den Berg theorem

Principle: Reduce dipolar energy to zero



H. A. M. van den Berg, J. Magn. Magn. Mater. 44, 207 (1984)

# Statics – Magnetic length scales

## The dipolar exchange length

When: anisotropy and exchange compete

$$E = \underbrace{A \left( \frac{\partial m_i}{\partial x_j} \right)^2}_{\substack{\text{Exchange} \\ \text{J/m}}} + \underbrace{K_d \sin^2 \theta}_{\substack{\text{Dipolar} \\ \text{J/m}^3}} \quad K_d = \frac{1}{2} \mu_0 M_s^2$$

$$\Delta_d = \sqrt{A/K_d} = \sqrt{2A/\mu_0 M_s^2}$$

$$\Delta_d \approx 3 - 10 \text{ nm}$$

Critical single-domain size, relevant for small particles made of soft magnetic materials



Often called: exchange length

## The anisotropy exchange length

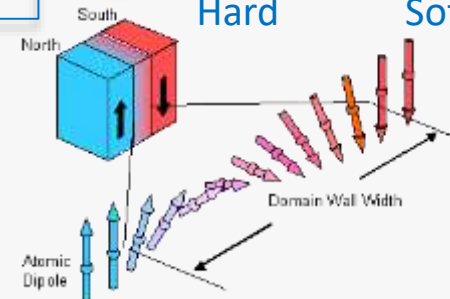
When: anisotropy and exchange compete

$$E = \underbrace{A \left( \frac{\partial m_i}{\partial x_j} \right)^2}_{\substack{\text{Exchange} \\ \text{J/m}}} + \underbrace{K \sin^2 \theta}_{\substack{\text{Anisotropy} \\ \text{J/m}^3}}$$

$$\Delta_u = \sqrt{A/K}$$

$$\Delta_u \approx 1 \text{ nm} \rightarrow 100 \text{ nm}$$

Hard Soft



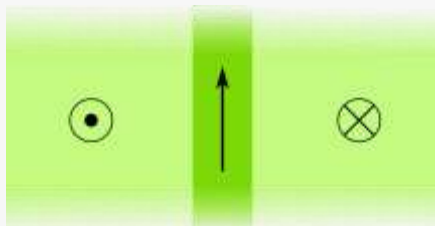
Sometimes called: Bloch parameter, or wall width

**Note:** Other length scales can be defined, e.g. with magnetic field



# Statics – Domain walls and dimensionality

## Bloch wall in the bulk (2D)



- ❑ No magnetostatic energy
- ❑ Width  $\Delta_u = \sqrt{A/K}$
- ❑ Energy  $\gamma_w = 4\sqrt{AK}$



Other angles & anisotropy

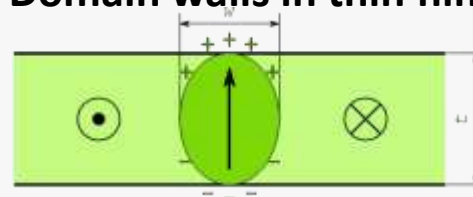
F. Bloch, Z. Phys. 74, 295 (1932)

## Constrained walls (eg in strips)

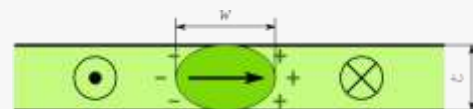
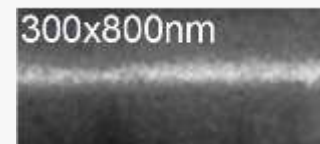


Permalloy (15nm)  
Strip width 500nm

## Domain walls in thin films (towards 1D)



Bloch wall  
 $t \gtrsim w$



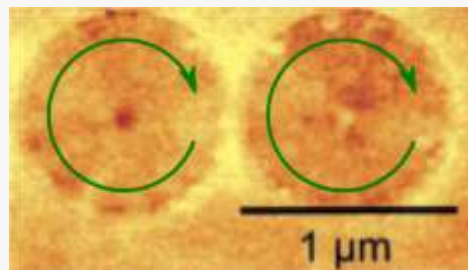
Néel wall  
 $t \lesssim w$



- ❑ Implies magnetostatic energy
- ❑ No exact analytic solution

L. Néel, C. R. Acad. Sciences 241, 533 (1956)

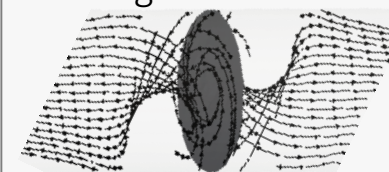
## Vortex (1D → 0D)



T. Shinjo et al.,  
Science 289, 930 (2000)

## Bloch point (0D)

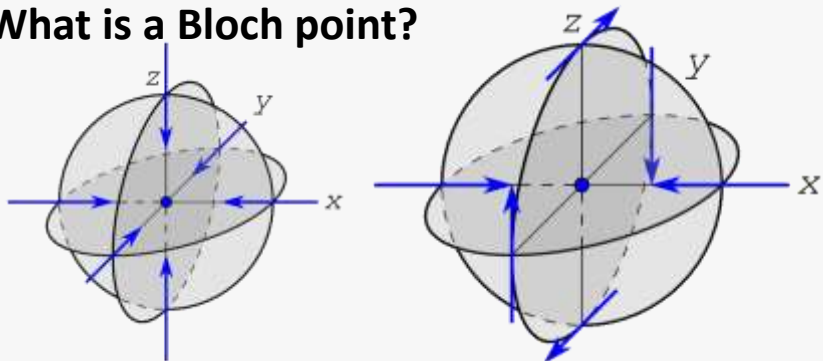
- ❑ Point with vanishing magnetization



W. Döring,  
JAP 39, 1006 (1968)

# Statics – Walls and topology (Bloch point)

## What is a Bloch point?

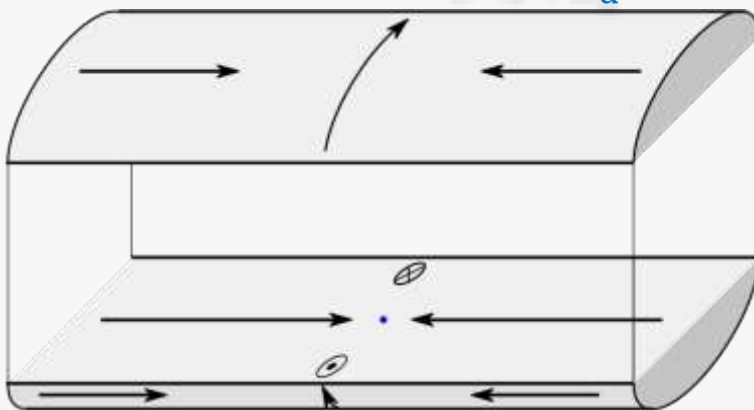


A magnetization texture with local cancellation of the magnetization vector

R. Feldkeller,  
Z. Angew. Physik 19, 530 (1965)

W. Döring,  
J. Appl. Phys. 39, 1006 (1968)

## Bloch-point wall, theory $D \gtrsim 7\Delta_d^2$

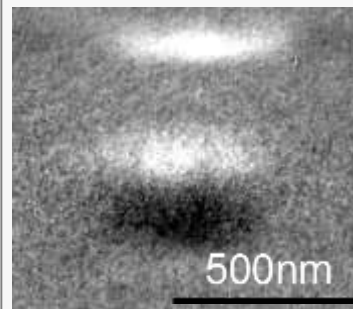


H. Forster et al., J. Appl. Phys. 91, 6914 (2002)

A. Thiaville, Y Nakatani, Spin dynamics in confined magnetic structures III, 101, 161-206 (2006)

## Bloch-point wall, experiments

Experiment



Simulation



SHADOW

Shadow XMCD-PEEM



S. Da-Col et al., PRB (R) 89, 180405, (2014)

# Static – Walls and topology (skyrmions)

## The Dzyaloshinskii-Moriya interaction

- Usual magnetic exchange

$$\mathcal{E}_{i,j} = -J_{i,j} \mathbf{S}_i \cdot \mathbf{S}_j$$



Promotes ferromagnetism  
(or antiferromagnetism)

- The DM interaction

$$\mathcal{E}_{\text{DMI}} = -\mathbf{d}_{i,j} \cdot (\mathbf{S}_i \times \mathbf{S}_j)$$

Requires: loss of inversion symmetry



Promotes spirals and cycloids

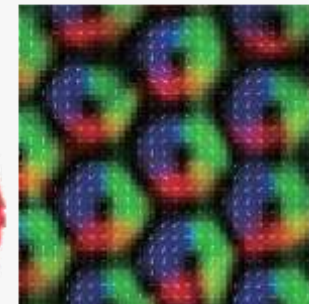


I. Dzyaloshinskii, J. of Phys. Chem. Solids 4, 241 (1958)

T. Moriya, Phys. Rev. 120, 91 (1960)

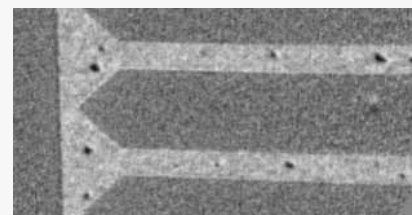
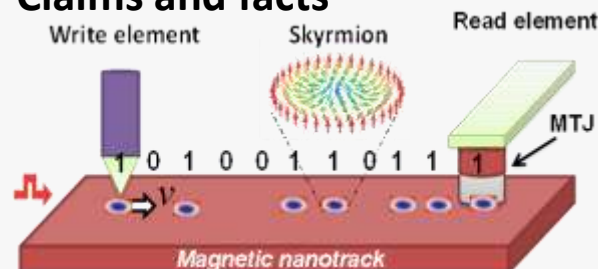
A. Fert and P.M. Levy, PRL 44, 1538 (1980)

## Magnetic skyrmions



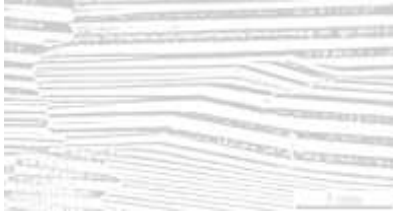
90 nm Bulk FeCoSi  
Lorentz microscopy

## Claims and facts

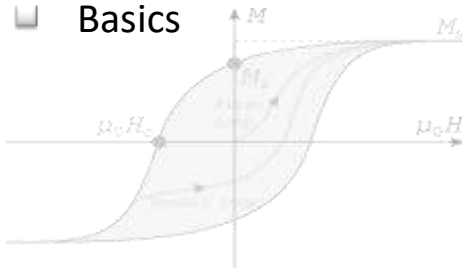


O. Boulle et al.,  
Nat. Nanotech.,  
11, 449 (2016)

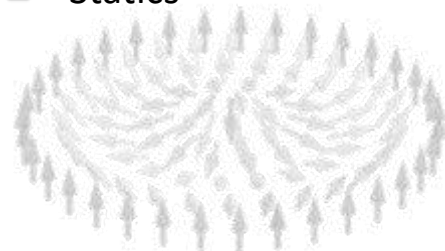
## ■ Motivation



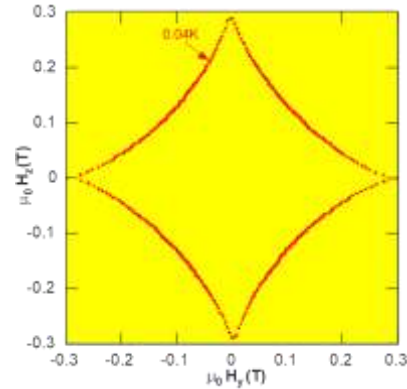
## ■ Basics



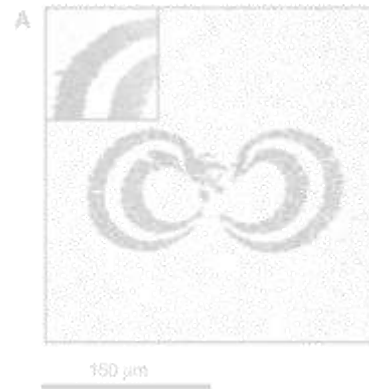
## ■ Statics



## ■ Macrospin switching



## ■ Precessional dynamics

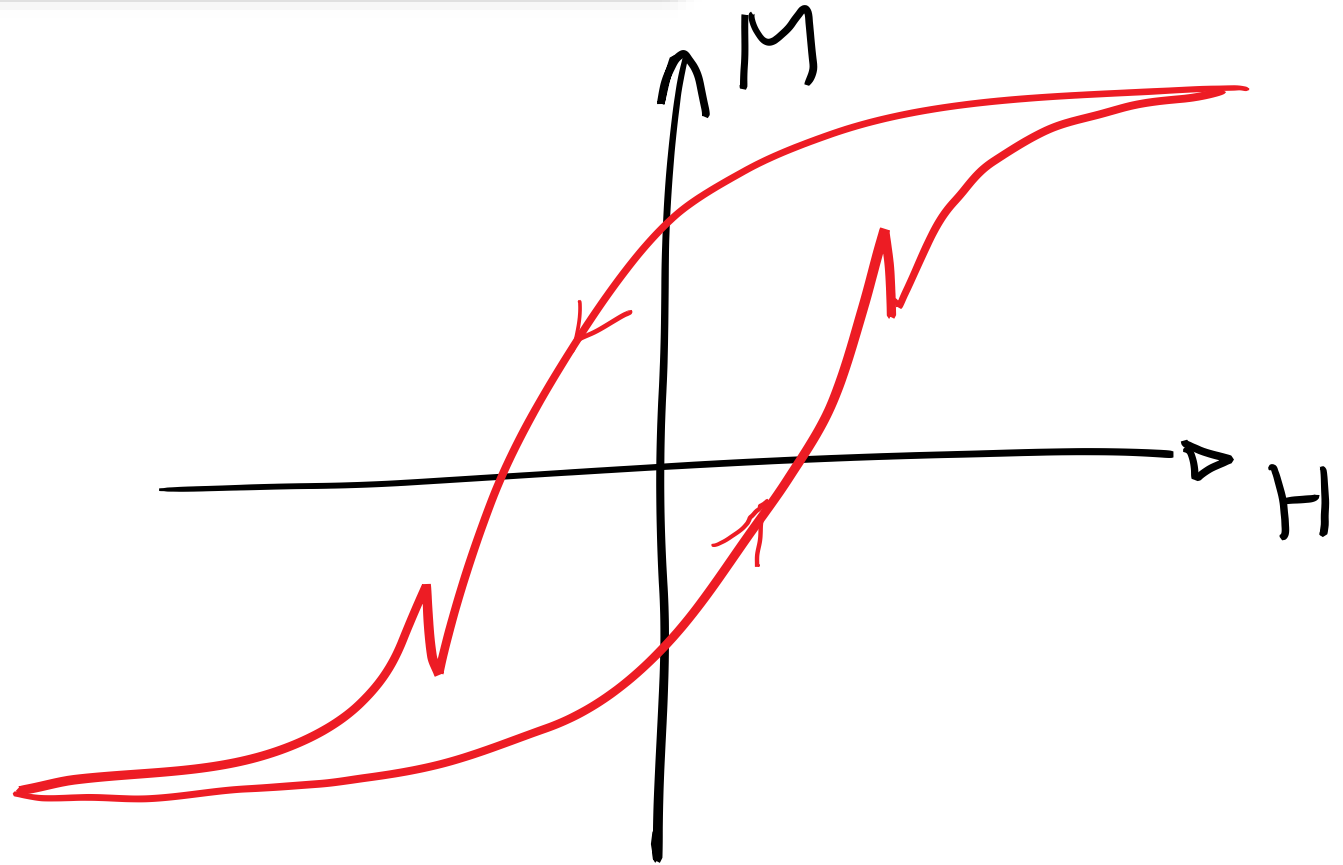


## ■ Extended systems



## Quizz #2

Is such a  
hysteresis loop  
possible?





# Macrospins – Stoner-Wohlfarth

## Framework: uniform magnetization

- ❑ Drastic, unsuitable in most cases
- ❑ Remember: demagnetization field may not be uniform

$$\mathcal{E} = E\mathcal{V}$$

$$= \mathcal{V}[K_{\text{eff}} \sin^2 \theta - \mu_0 M_s H \cos(\theta - \theta_H)]$$

- ❑ Anisotropy:  $K_{\text{eff}} = K_{\text{mc}} + (\Delta N)K_d$



## Names used

- ❑ Uniform rotation / magnetization reversal
- ❑ Coherent rotation / magnetization reversal
- ❑ Macrospin etc.

## Dimensionless units

$$e = \sin^2 \theta - 2h \cos(\theta - \theta_H)$$

$$e = \mathcal{E}/(K\mathcal{V})$$

$$h = H/H_a$$

$$H_a = 2K/(\mu_0 M_s)$$

L. Néel, *Compte rendu Acad. Sciences* 224, 1550 (1947)

E. C. Stoner and E. P. Wohlfarth,

*Phil. Trans. Royal. Soc. London A*240, 599 (1948)

Reprint: *IEEE Trans. Magn.* 27(4), 3469 (1991)

# Macrospins – Stoner-Wohlfarth

Example:  $\theta_H = \pi \rightarrow e = \sin^2 \theta + 2h \cos \theta$

## Equilibrium positions

$$\partial_{\theta} e = 2 \sin \theta (\cos \theta - h) \quad \left| \begin{array}{l} \cos \theta_m = h \\ \theta \equiv 0 [\pi] \end{array} \right.$$

## Stability

$$\partial_{\theta\theta} e = 4 \cos^2 \theta - 2h \cos \theta - 2 \quad \left| \begin{array}{l} \partial_{\theta\theta} e(0) = 2(1 - h) \\ \partial_{\theta\theta} e(\theta_m) = 2(h^2 - 1) \\ \partial_{\theta\theta} e(\pi) = 2(1 + h) \end{array} \right.$$

## Switching field

- Vanishing of local minimum
- Is abrupt

$$h_{sw} = 1$$

$$\rightarrow H = H_a = 2K/(\mu_0 M_s)$$

## Energy barrier

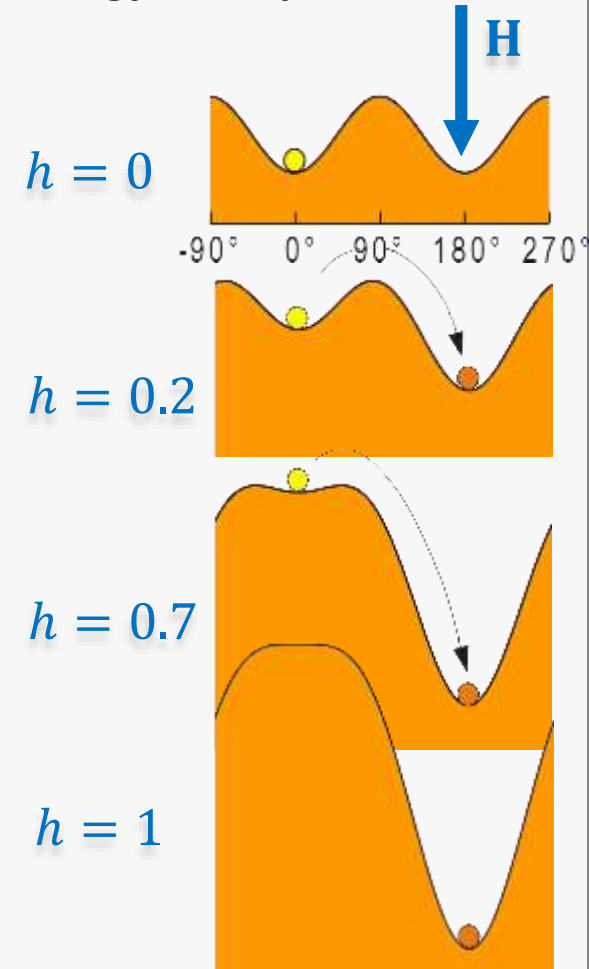
$$\Delta e = e(\theta_m) - e(0) = (1 - h)^2$$



$$\Delta e \sim (1 - h)^{1.5} \text{ In general}$$

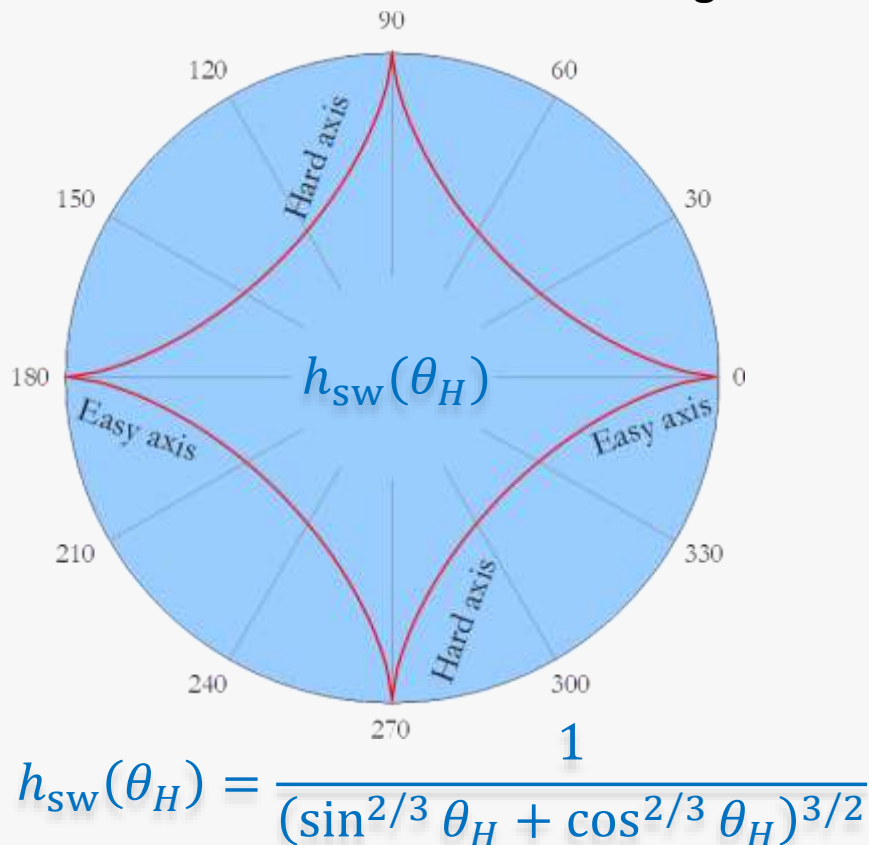
(breaking of symmetry)

## Energy landscape



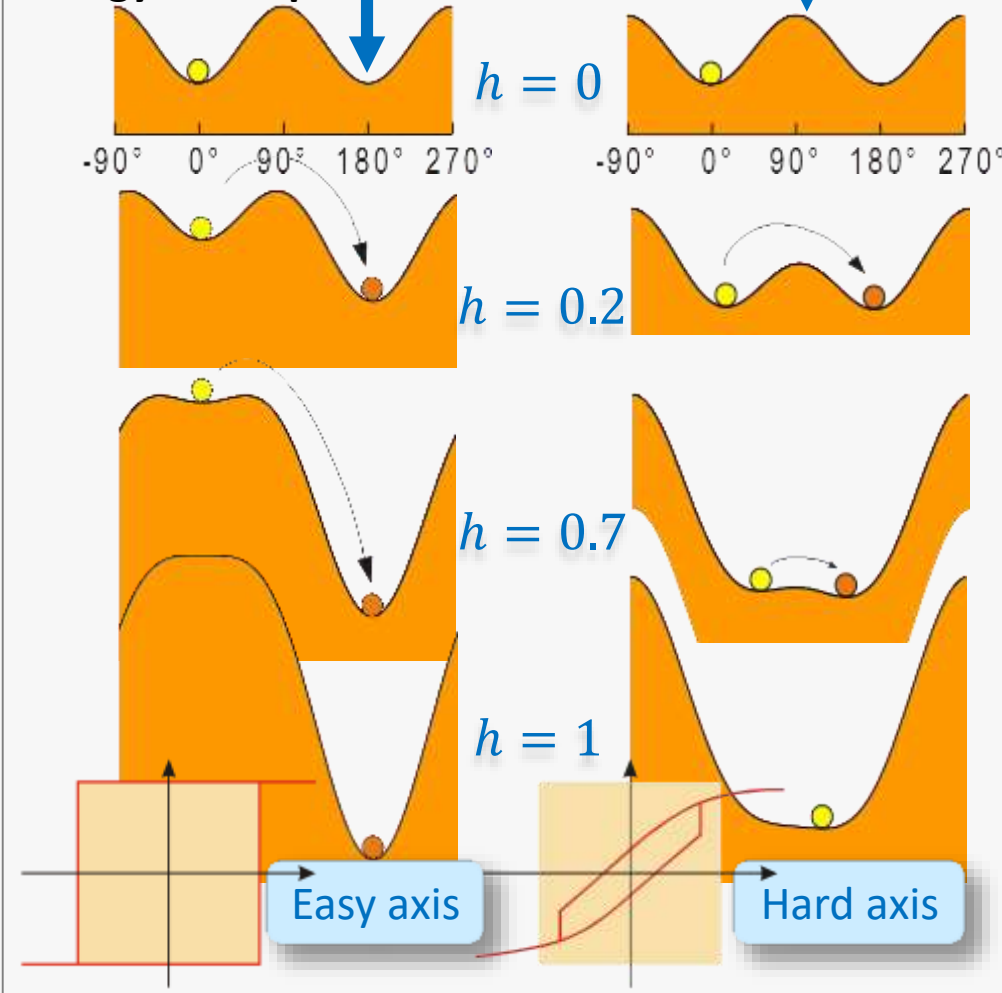
# Macrospins – Stoner-Wohlfarth

## Stoner-Wohlfarth astroid: switching field



J. C. Slonczewski, Research Memo RM 003.111.224, IBM Research Center (1956)

## Energy landscape



# Macrospins – Switching vs coercive field

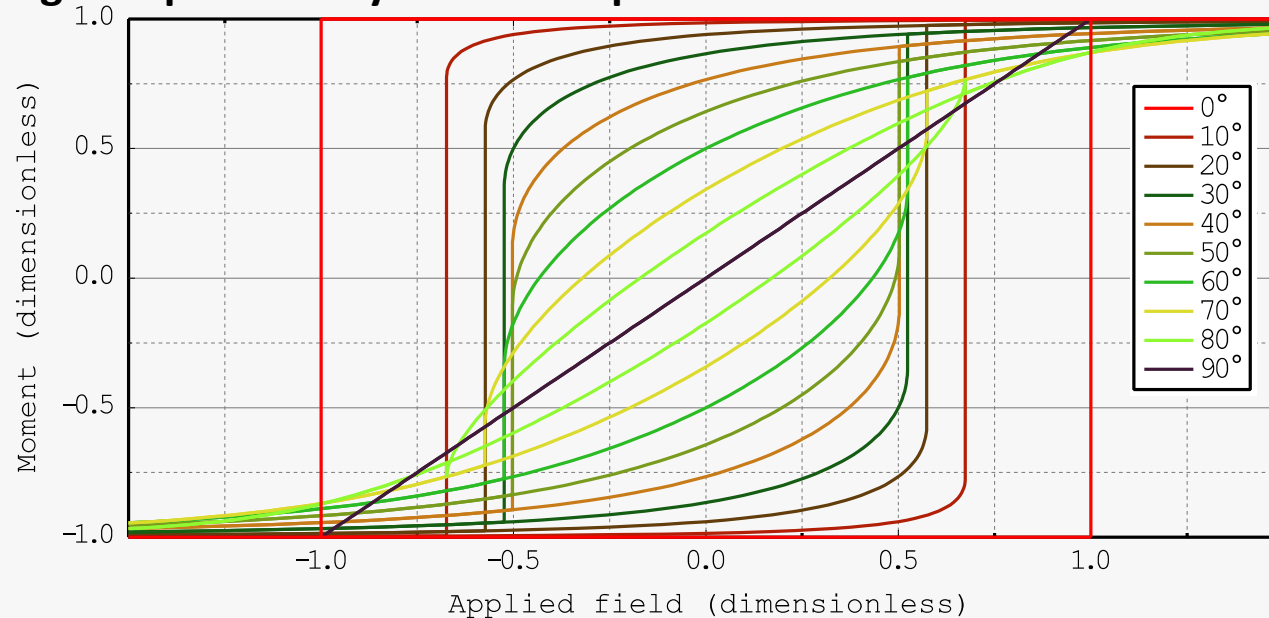
## Switching field $H_{sw}$

- A value of field at which an irreversible (abrupt) jump of magnetization angle occurs.
- Can be measured only in single particles.

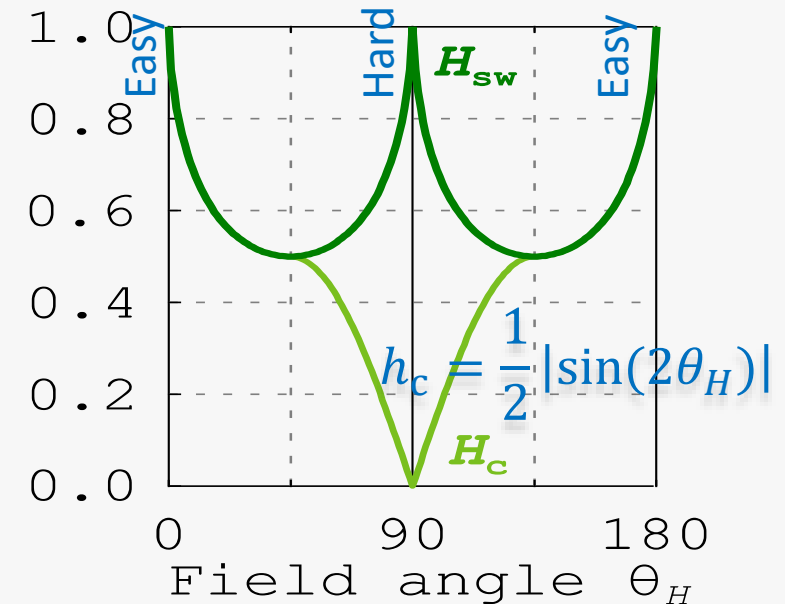
## Coercive field $H_c$

- The field at which  $\mathbf{H} \cdot \mathbf{M} = 0$
- Measurable in materials (large number of 'particles').
- May or may not be a measure of the mean switching field at the microscopic level

## Angle-dependent hysteresis loops

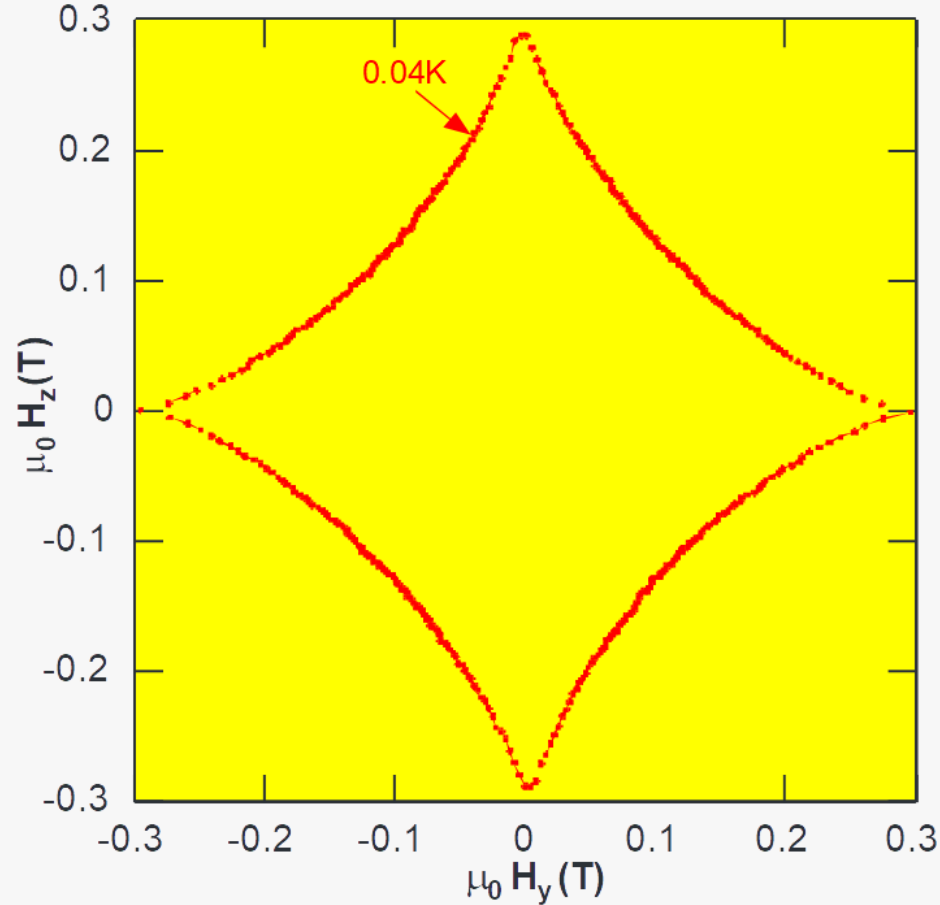


## Switching versus coercive field

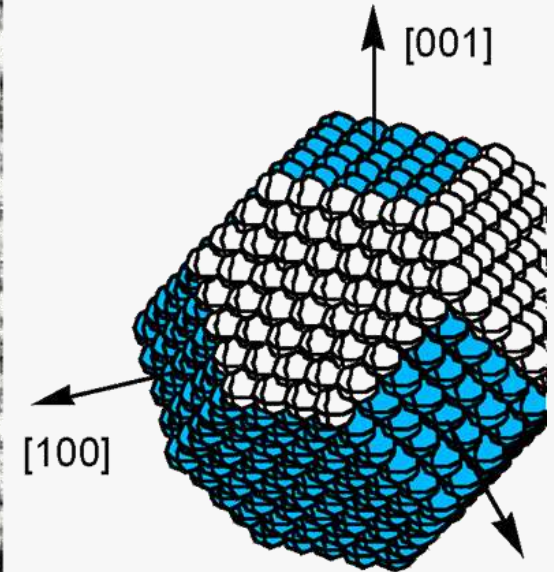
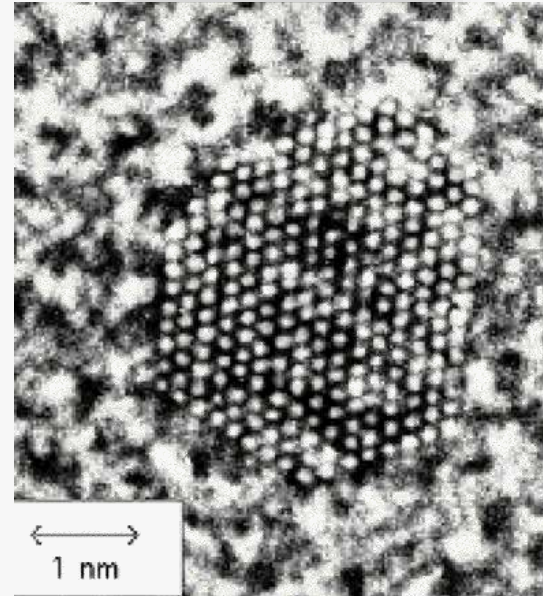


# Macrospins – Experiments

## First experimental evidence



Co cluster



W. Wernsdorfer et al., Phys. Rev. Lett. 78, 1791 (1997)

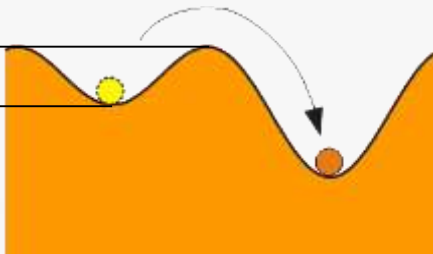


# Macrospins – Thermal activation

## Barrier height (reminder)

$$\Delta e = (1 - h)^2$$

$$h = \left( \frac{\mu_0 M_s}{2K} \right) H$$



## Thermal activation

- Mean waiting time to switch with excitations

$$\tau = \tau_0 \exp\left(\frac{\Delta \mathcal{E}}{k_B T}\right) \quad \text{Brown, Phys.Rev.130, 1677 (1963)}$$

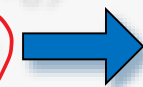
$$\tau_0 \approx 10^{-10} \text{ s} \quad \text{Inverse attempt frequency}$$

- Barrier height preventing spontaneous switching in time  $\tau$

$$\Delta \mathcal{E} = k_B T \ln(\tau / \tau_0)$$

Lab time scale

1 s



$$\Delta \mathcal{E} = 25 k_B T$$



$$H_c(T, \tau) = \frac{2K}{\mu_0 M_s} \left( 1 - \sqrt{\frac{25 k_B T}{KV}} \right)$$

Sharrock law

M. P. Sharrock, J. Appl. Phys. 76, 6413-6418 (1994)

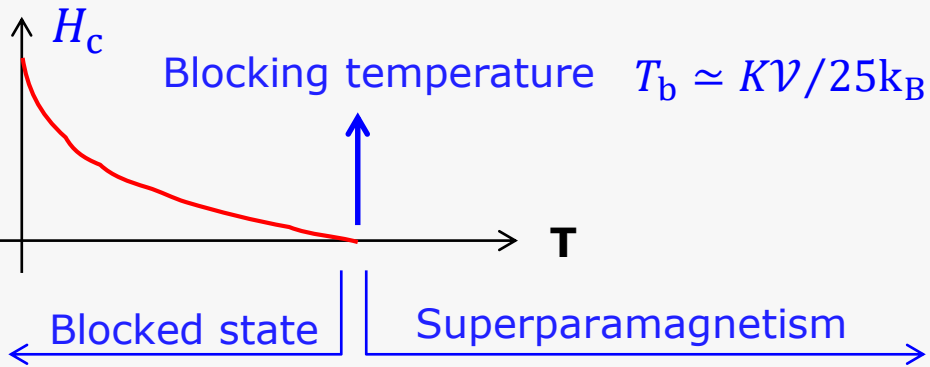
$\approx 10 \text{ years}$

40 to 60  $k_B T$   
for magnetic recording

# Macrospins – Thermal activation

## Superparamagnetism

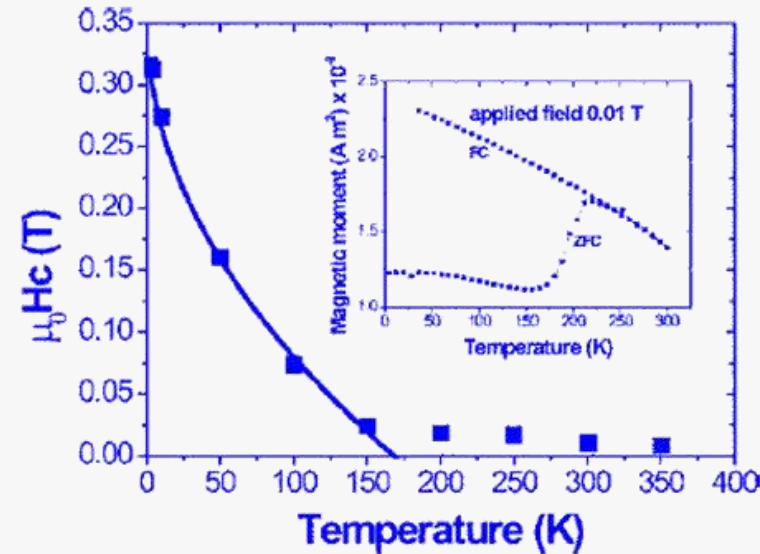
Thermally-induced loss of all coercivity



E. F. Kneller, J. Wijn (ed.) Handbuch der Physik XIII/2: Ferromagnetismus, Springer, 438 (1966)

### Example

J. Appl. Phys. **99**, 08Q514 (2006)



# Macrospins – Thermal activation

## Superparamagnetism – Formalism

Energy

$$\mathcal{E} = KVf(\theta, \phi) - \mu_0 \boldsymbol{\mu} \cdot \mathbf{H}$$

Partition function

$$Z = \sum \exp(-\beta \mathcal{E})$$

Average moment

$$\langle \mu \rangle = \frac{1}{\beta \mu_0 Z} \frac{\partial Z}{\partial H}$$

### Isotropic case

$$Z = \int_{-\mathcal{M}}^{\mathcal{M}} \exp(\beta \mu_0 \mu H) d\mu$$

$$\Rightarrow \langle \mu \rangle = \mathcal{M} \left[ \coth \left( x - \frac{1}{x} \right) \right]$$

Langevin function



Consider total moment,  
not with spin 1/2

$$x = \beta \mu_0 \mathcal{M} H$$

### Infinite anisotropy

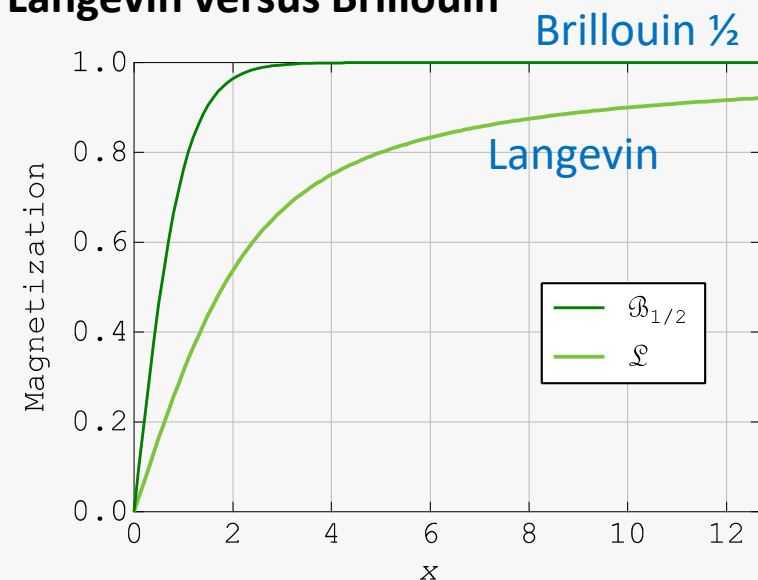
$$Z = \exp(\beta \mu_0 \mathcal{M} H) + \exp(-\beta \mu_0 \mathcal{M} H)$$

$$\Rightarrow \langle \mu \rangle = \mathcal{M} \operatorname{th}(x)$$

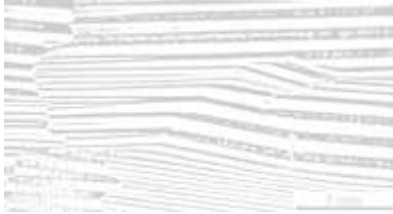
Brillouin 1/2 function



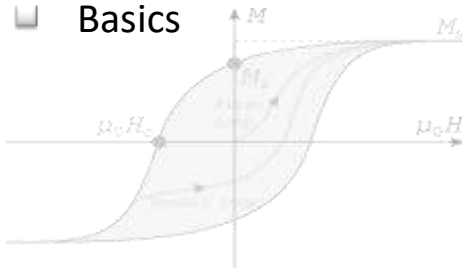
### Langevin versus Brillouin



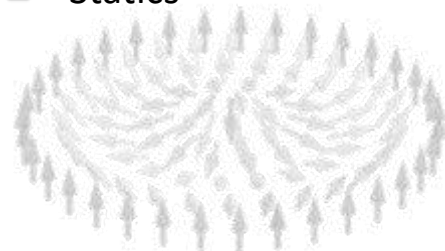
## ■ Motivation



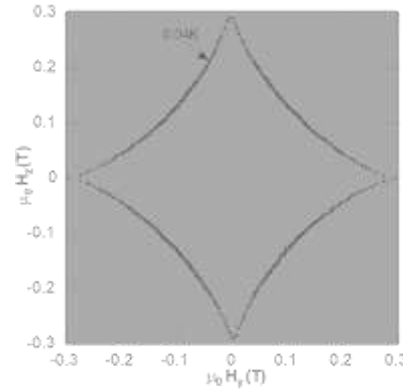
## ■ Basics



## ■ Statics



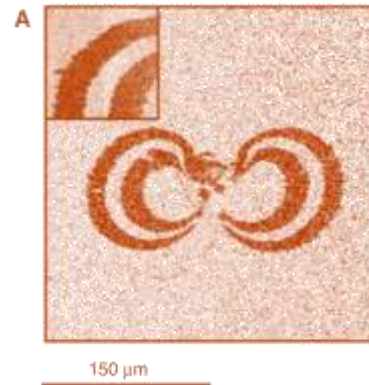
## ■ Macrospin switching



## ■ Extended systems



## ■ Precessional dynamics



# Precessional dynamics – The Landau-Lifshitz-Gilbert equation

## LLG equation

- Describes: precessional dynamics of magnetic moments
- Applies to magnetization, with phenomenological damping

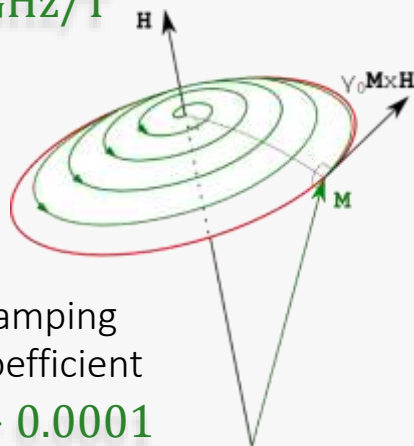
$$\frac{d\mathbf{m}}{dt} = -|\gamma_0|\mathbf{m} \times \mathbf{H} + \alpha \mathbf{m} \times \frac{d\mathbf{m}}{dt}$$

$$\gamma_0 = \mu_0\gamma < 0 \quad \text{Gyromagnetic ratio}$$

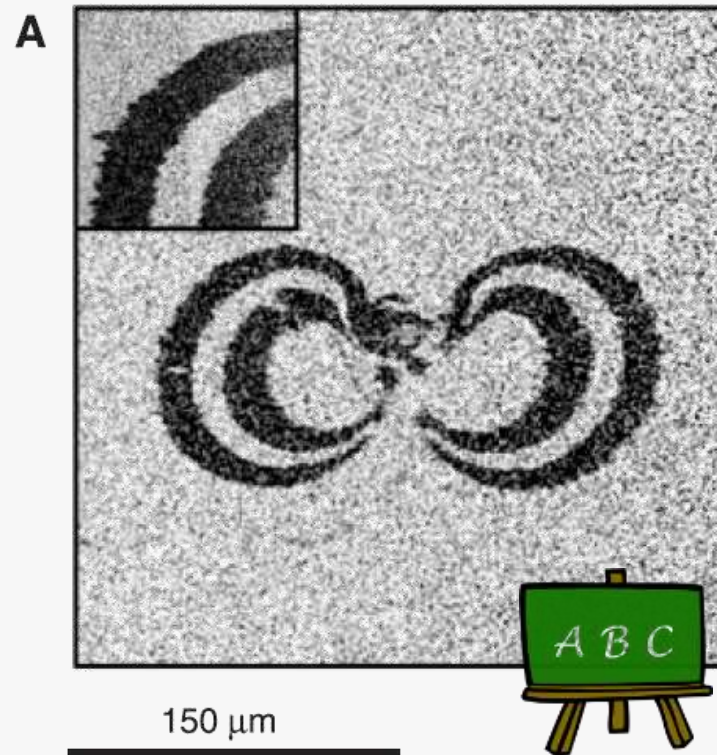
$$\gamma_s = 28 \text{ GHz/T}$$

$$\alpha > 0 \quad \text{Damping coefficient}$$

$$\alpha = 0.1 - 0.0001$$



## Pioneering experiment of precessional magnetization reversal

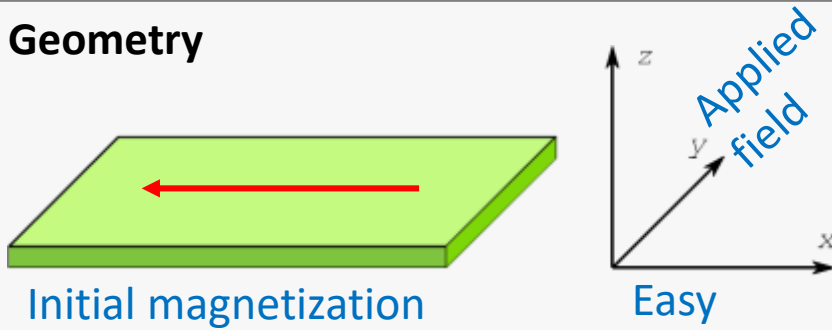


C. Back et al., Science 285, 864 (1999)



# Precessional dynamics – Trajectories

## Geometry

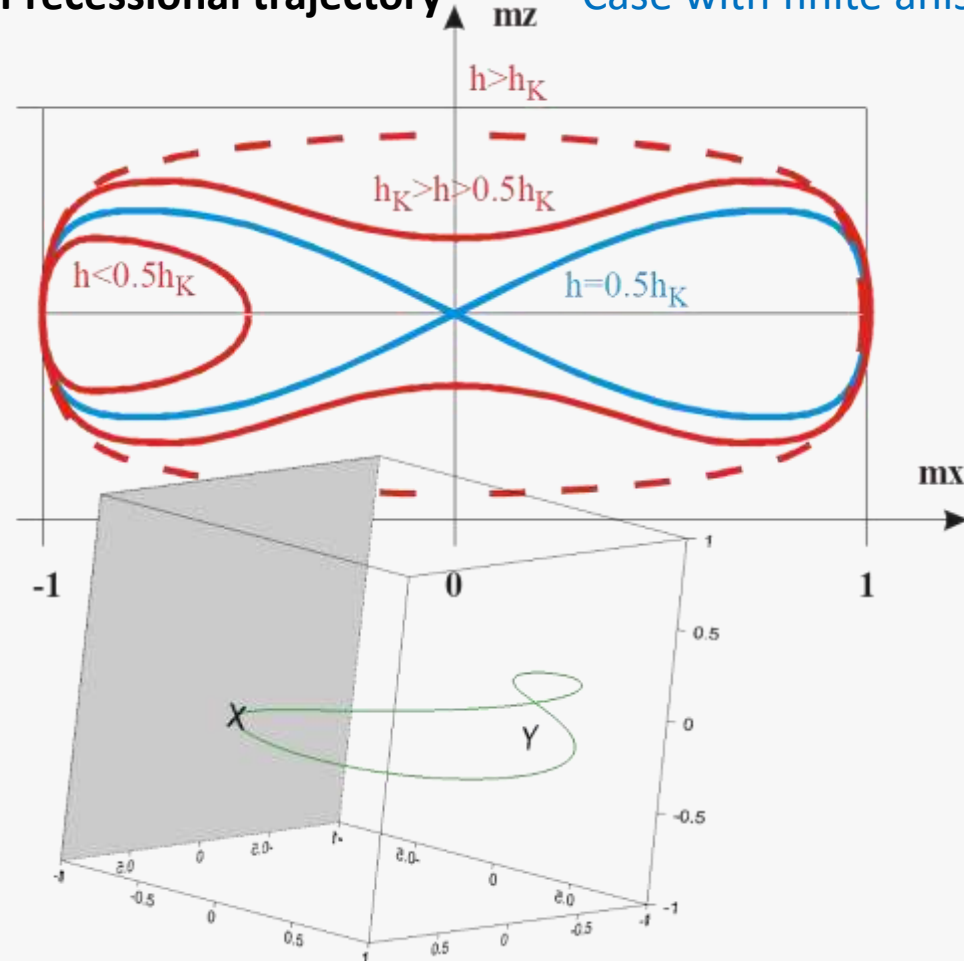


$$\frac{d\mathbf{m}}{dt} = -|\gamma_0|\mathbf{m} \times \mathbf{H} + \text{damping}$$

- Precession around its own demagnetizing field
- Threshold for switching is half the Stoner-Wohlfarth one

## Precessional trajectory

Case with finite anisotropy

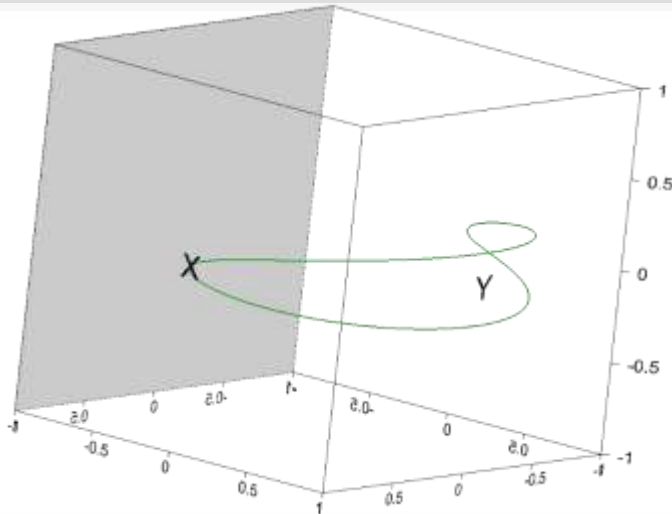


# Precessional dynamics – Energy considerations

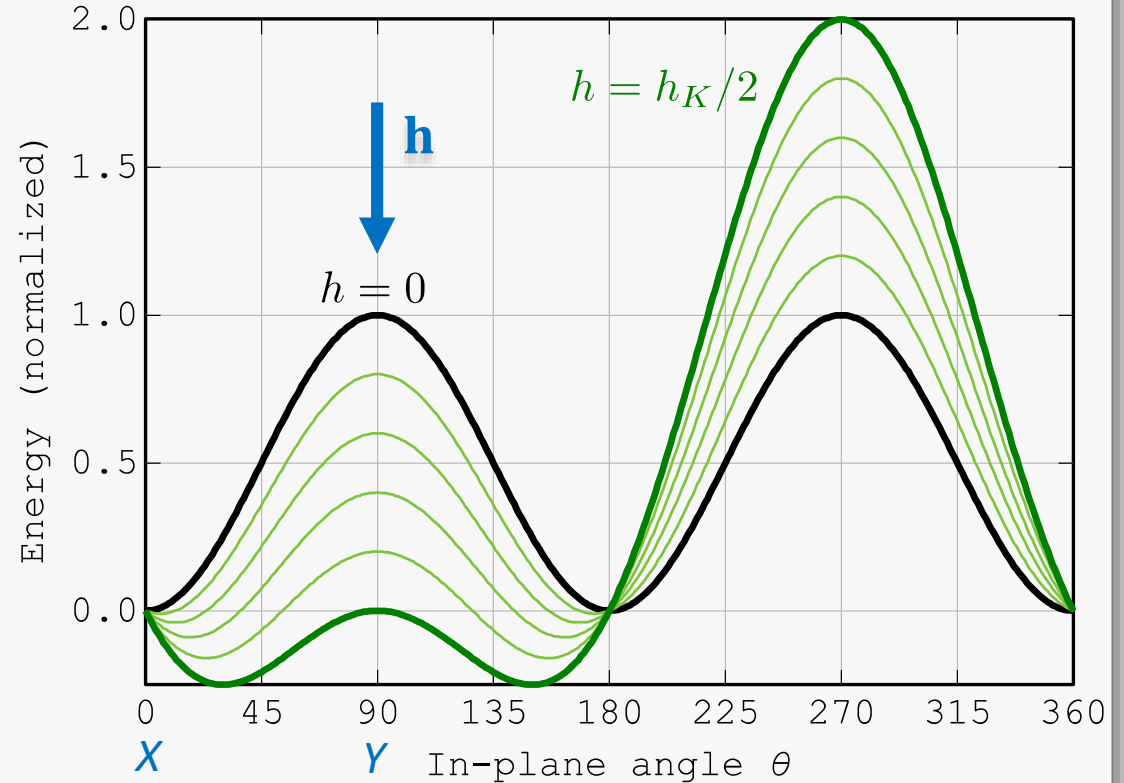
## Stoner-Wohlfarth versus precessional switching

- Stoner-Wohlfarth: slow field variation; system remains quasistatically at local minimum
- Precessional: short time scale; system may follow iso-energy lines in case of moderate damping

Precession period:  $\frac{2\pi}{|\gamma|} = 35 \text{ ps} \cdot T$

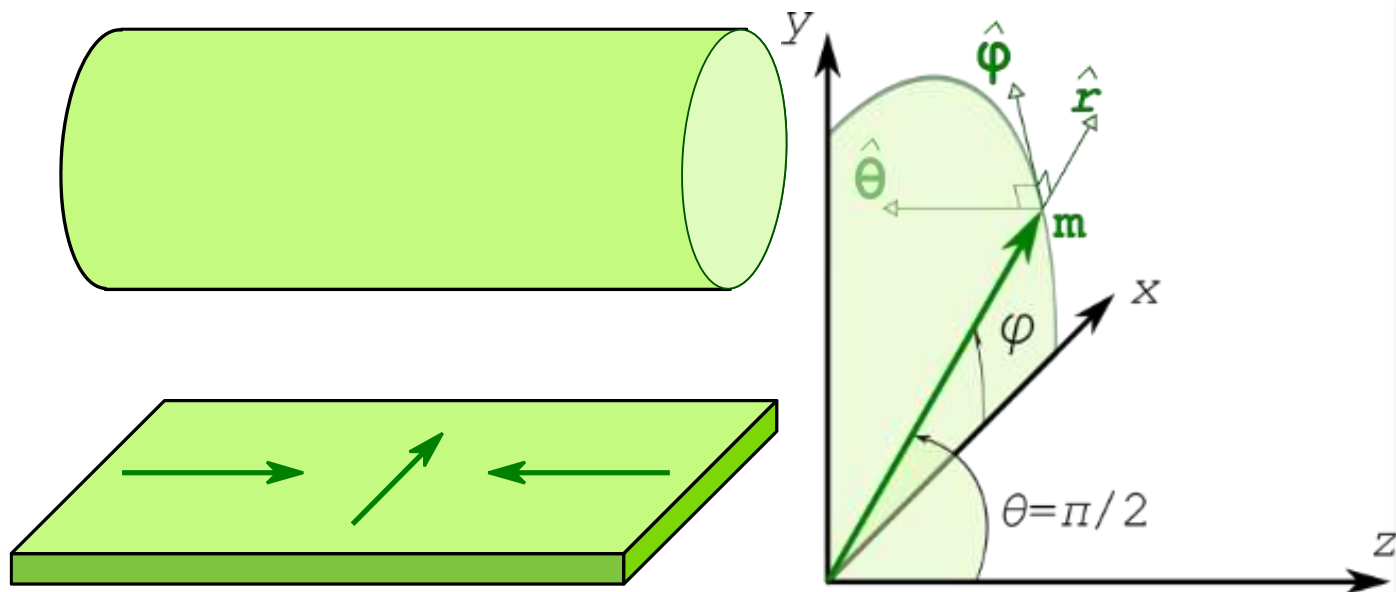


## Energy landscape



- In practice, difficult to control (backswitching due to distributions)

# Precessional dynamics – Motion of domain walls

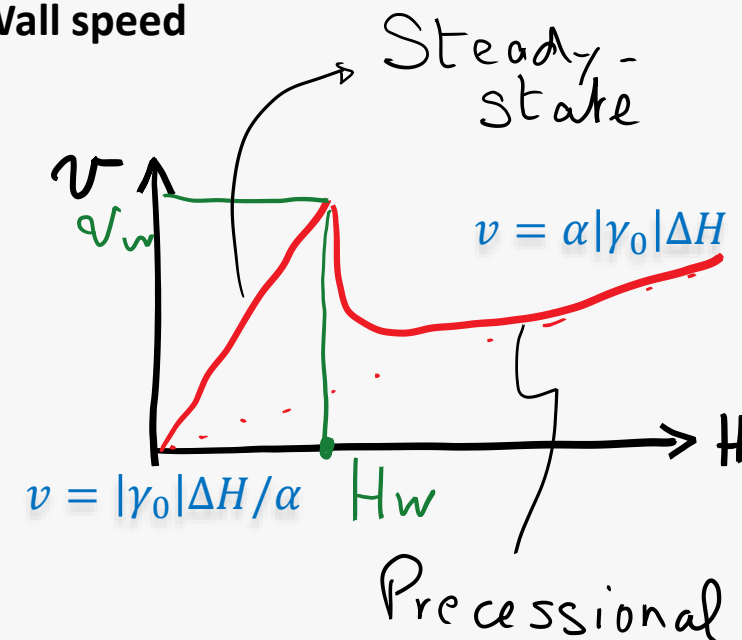


## Precessional dynamics under magnetic field

$$\frac{d\mathbf{m}}{dt} = -|\gamma_0|\mathbf{m} \times \mathbf{H} + \alpha \mathbf{m} \times \frac{d\mathbf{m}}{dt}$$



## Wall speed

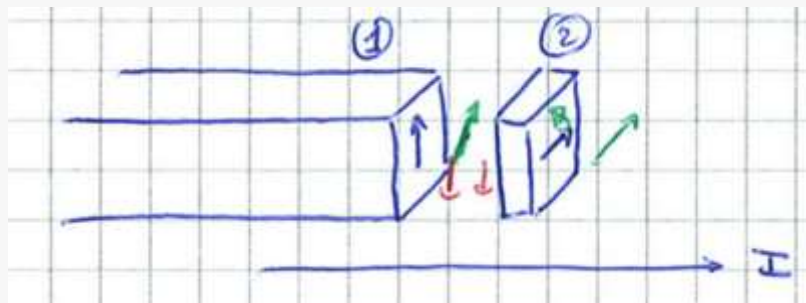


- Walker field  $H_w = \alpha M_s/2$   
 $\approx \text{few mT}$
- Walker speed  $v = |\gamma_0|M_s\Delta/2$   
 $\approx \text{few } 10\text{'s of m/s, to km/s}$

A. Thiaville, Y. Nakatani, Domain-wall dynamics in nanowires and nanostrips, in *Spin dynamics in confined magnetic structures {III}*, Springer (2006)

# Precessional dynamics – Spin transfer phenomena

## Macrospins (1d model)



$$\frac{d\mathbf{M}_2}{dt} = -|\gamma_0|\mathbf{M}_2 \times \mathbf{H}_{\text{eff}} + \alpha \frac{\mathbf{M}_2}{M_{s,2}} \times \frac{d\mathbf{M}_2}{dt} - P_{\text{trans}} \mathbf{M}_2 \times (\mathbf{M}_2 \times \mathbf{M}_1) \quad P_{\text{trans}} \sim P \frac{J}{|e|}$$

J. C. Slonczewski, J. Magn. Magn. Mater. 159, L1 (1996)

L. Berger, Phys. Rev. B 54, 9353 (1996)

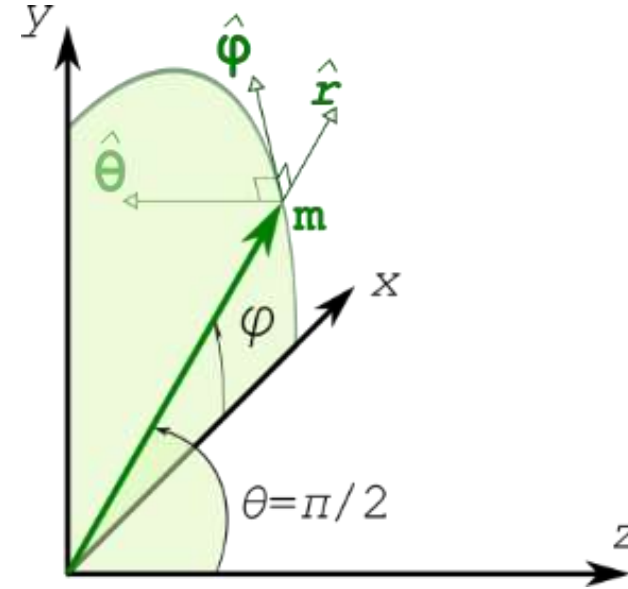
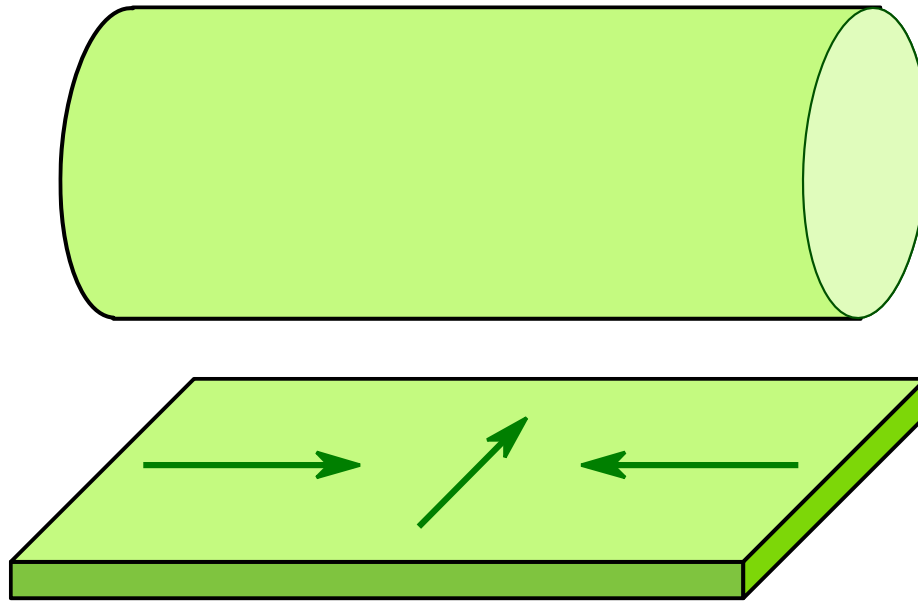
Number of spin-polarized  
electrons per unit time

## Magnetization texture (domain wall etc.)

$$\frac{d\mathbf{m}}{dt} = -|\gamma_0|\mathbf{m} \times \mathbf{H} + \alpha \mathbf{m} \times \frac{d\mathbf{m}}{dt} - \overset{\text{Transfer}}{(\mathbf{u} \cdot \nabla)\mathbf{m}} + \overset{\text{Field-like}}{\beta \mathbf{m} \times [(\mathbf{u} \cdot \nabla)\mathbf{m}]}$$

A. Thiaville, Y. Nakatani, Micromagnetic simulation of domain wall dynamics in nanostrips, in *Nanomagnetism and Spintronics*, Elsevier (2009)

# Precessional dynamics – Motion of domain walls



Precessional dynamics under current

$$\frac{d\mathbf{m}}{dt} = -|\gamma_0|\mathbf{m} \times \mathbf{H} + \alpha\mathbf{m} \times \frac{d\mathbf{m}}{dt} - (\mathbf{u} \cdot \nabla)\mathbf{m} + \beta\mathbf{m} \times [(\mathbf{u} \cdot \nabla)\mathbf{m}]$$

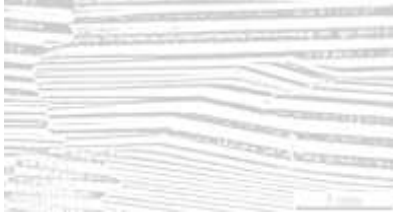
Adiabatic  
Non-adiabatic

Reflects spin-polarized current

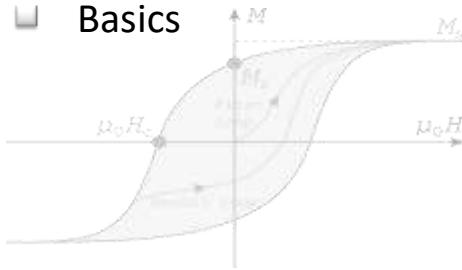
A. Thiaville, Y. Nakatani, Micromagnetic simulation of domain wall dynamics in nanostrips, in *Nanomagnetism and Spintronics*, Elsevier (2009)



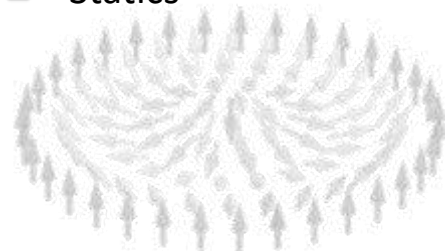
## Motivation



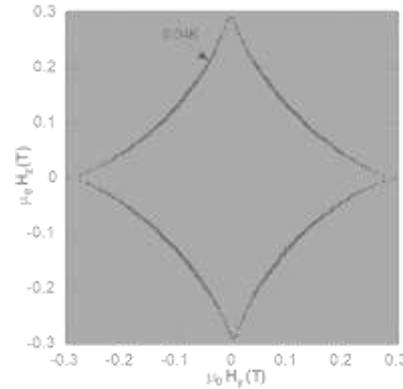
## Basics



## Statics



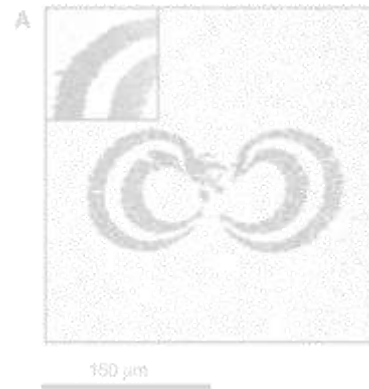
## Macrospin switching



## Extended systems

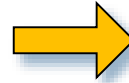


## Precessional dynamics



## Brown paradox

In most (extended systems):  $H_c \ll \frac{2K}{\mu_0 M_s}$



## (Micromagnetic) modeling

Exhibit analytic, nevertheless realistic models for magnetization reversal

PHYSICAL REVIEW

VOLUME 119, NUMBER 1

JULY 1, 1960

## Reduction in Coercive Force Caused by a Certain Type of Imperfection

A. AHARONI

*Department of Electronics, The Weizmann Institute of Science, Rehovot, Israel*

(Received February 1, 1960)

As a first approach to the study of the dependence of the coercive force on imperfections in materials which have high magnetocrystalline anisotropy, the following one-dimensional model is treated. A material which is infinite in all directions has an infinite slab of finite width in which the anisotropy is 0. The coercive force is calculated as a function of the slab width. It is found that for relatively small widths there is a considerable reduction in the coercive force with respect to perfect material, but reduction saturates rapidly so that it is never by more than a factor of 4.

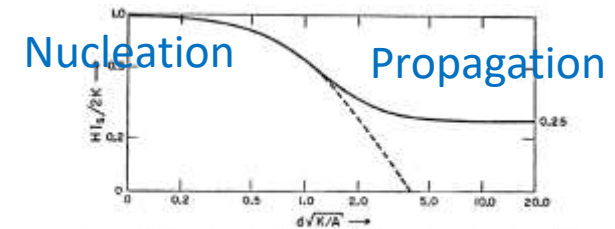
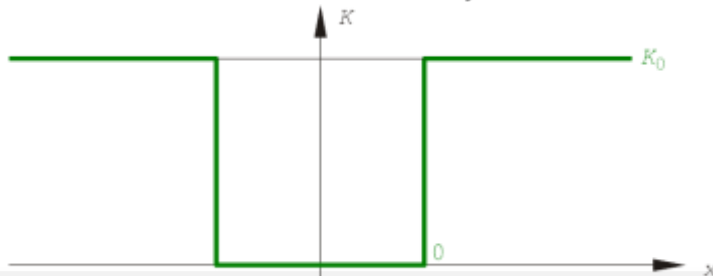
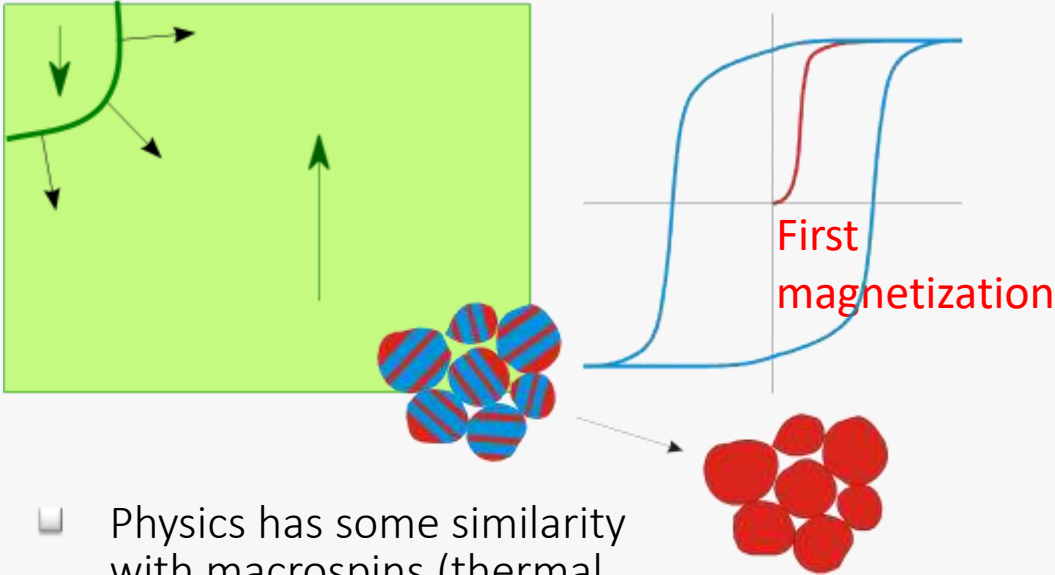


FIG. 1. The nucleation field (dashed) and coercive force (full curve) in terms of the coercive force of perfect material,  $H_{1/2}/2K$ , as functions of the defect size,  $d$ .

# Switching – Extended systems

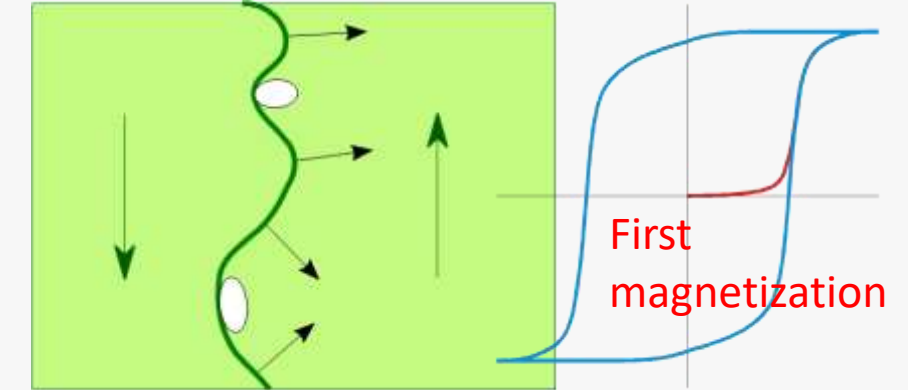
## Nucleation-limited coercivity



- Physics has some similarity with macrospins (thermal activation etc.)
- Concept of nucleation volume

Ex:  $\text{Nd}_2\text{Fe}_{14}\text{B}$  coarse-grained magnets

## Propagation-limited coercivity



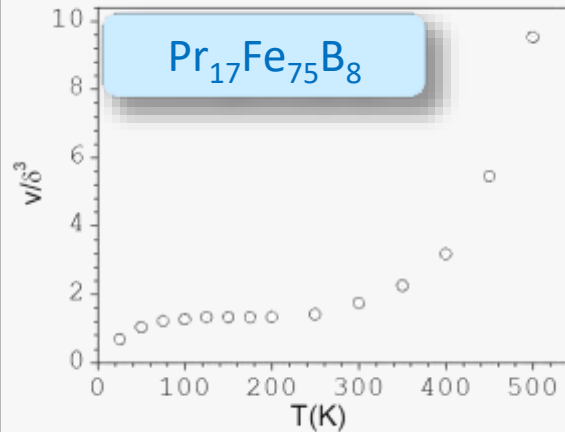
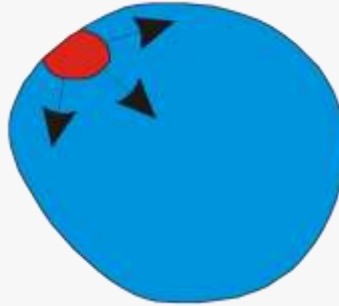
- Physics of surface/string in a disordered landscape
- See in thin films: creep, Fatuzzo-Raquet model  
M. Labrune et al., J. Magn. Magn. Mater. 80, 211 (1989)

Ex:  $\text{Sm}_2\text{Co}_{17}$  magnets

# Switching – Extended systems

## Activation volume

- Also called: nucleation volume
- Should be considered if system is larger than the characteristic length scale
- Use for: estimate  $H_c(T)$ , long-time relaxation, dimensionality
- Size similar to wall width  $\delta$



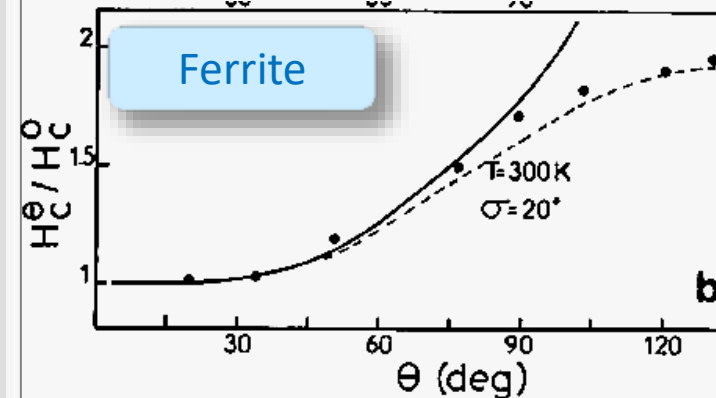
Courtesy D. Givord

## 1/cos( $\vartheta$ ) law, Becker-Kondorski model

E. J. Kondorsky, J. Exp. Theor. Fiz. 10, 420 (1940)

- Assumes:  
coercivity  $\ll$  anisotropy field
- Energy barriers overcome by Zeeman + thermal energy

$$\Delta E = -\mu_0 M_s H v_a \cos \theta_H + 25 k_B T$$




REVIEW: D. Givord et al., JMMM258, 1 (2003)

D. Givord et al., JMMM72, 247 (1988)

Alex Hubert  
Rudolf Schäfer

## Magnetic Domains

The Analysis  
of Magnetic Microstructures

 Springer

Alberto P. Guimarães

NANOSCIENCE AND TECHNOLOGY

## Principles of Nanomagnetism

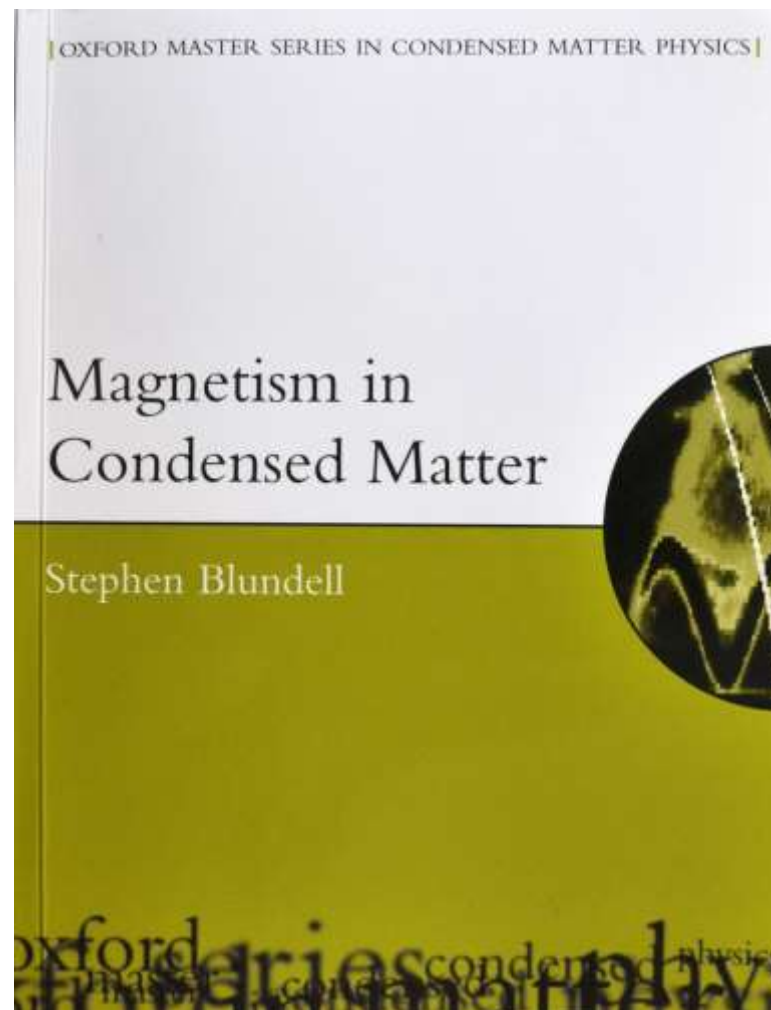
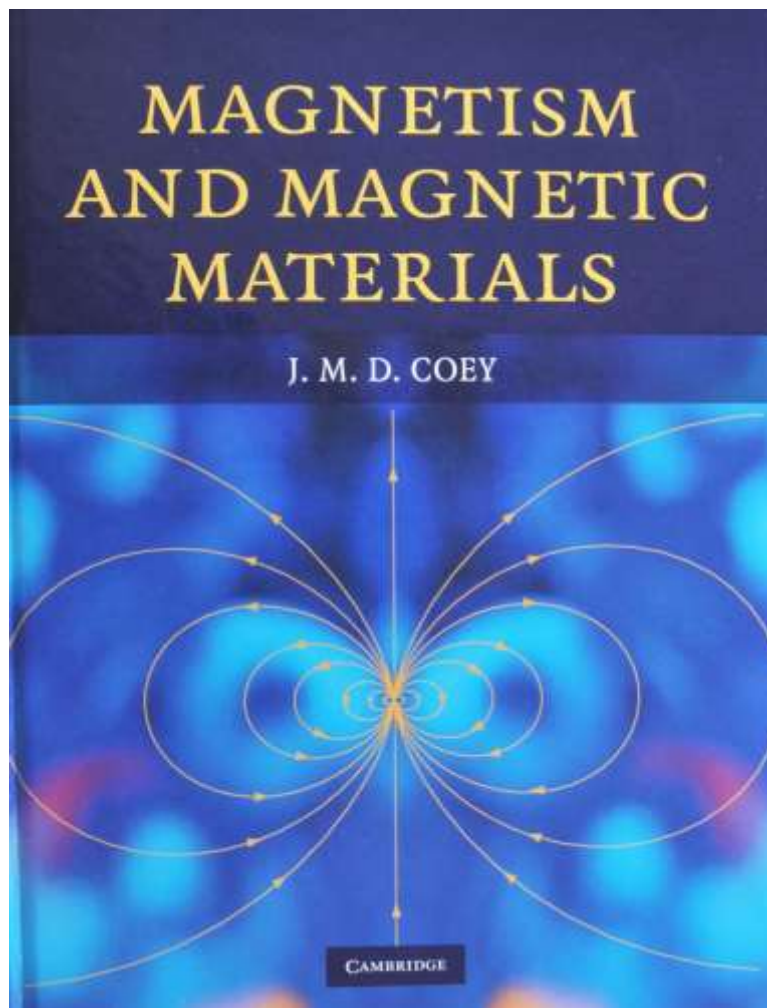
 Springer

## Simple Models of Magnetism

Ralph Skomski

OXFORD GRADUATE TEXTS





More extensive slides on: <http://magnetism.eu/esm/repository-authors.html#F>

2013, 2009, 2007

Lecture notes from undergraduate lectures, plus various slides on magnetization reversal:

<http://fruchart.eu/olivier/slides/>

- [1] Magnetic domains, A. Hubert, R. Schäfer, Springer (1999, reed. 2001)
- [2] R. Skomski, Simple models of Magnetism, Oxford (2008).
- [3] R. Skomski, Nanomagnetism, J. Phys.: Cond. Mat. 15, R841–896 (2003).
- [4] O. Fruchart, A. Thiaville, Magnetism in reduced dimensions,  
C. R. Physique 6, 921 (2005) [Topical issue, Spintronics].
- [5] J.I. Martin et coll., Ordered magnetic nanostructures: fabrication and properties,  
J. Magn. Magn. Mater. 256, 449-501 (2003)

# Thank you for your attention !

[www.spintec.fr](http://www.spintec.fr) | 

email: [olivier.fruchart@cea.fr](mailto:olivier.fruchart@cea.fr)