

Nanomagnetism: born when spintronics was mere science fiction



La caste des metabarons

A. Jodorowsky & J. Gimenez

<http://www.humano.com/>

A short overview of nanomagnetism



Olivier Fruchart

Institut Néel (CNRS-UJF-INPG)

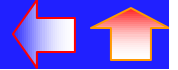
Grenoble - France

<http://neel.cnrs.fr>

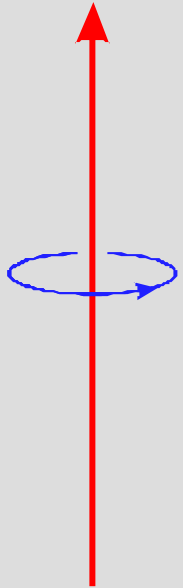


Institut Néel, Grenoble, France.

<http://perso.neel.cnrs.fr/olivier.fruchart/>

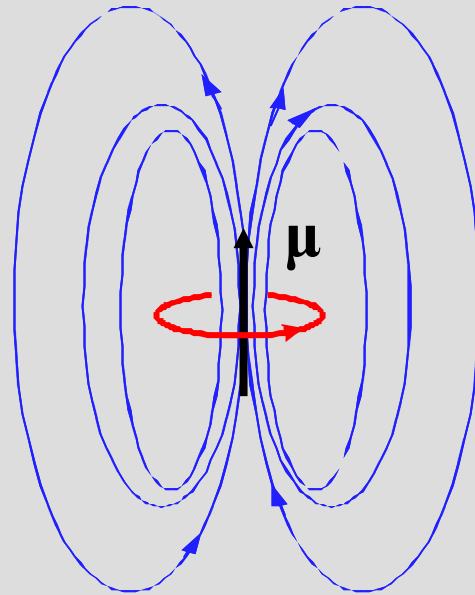


Oersted field



$$B = \frac{\mu_0 I}{2\pi r}$$

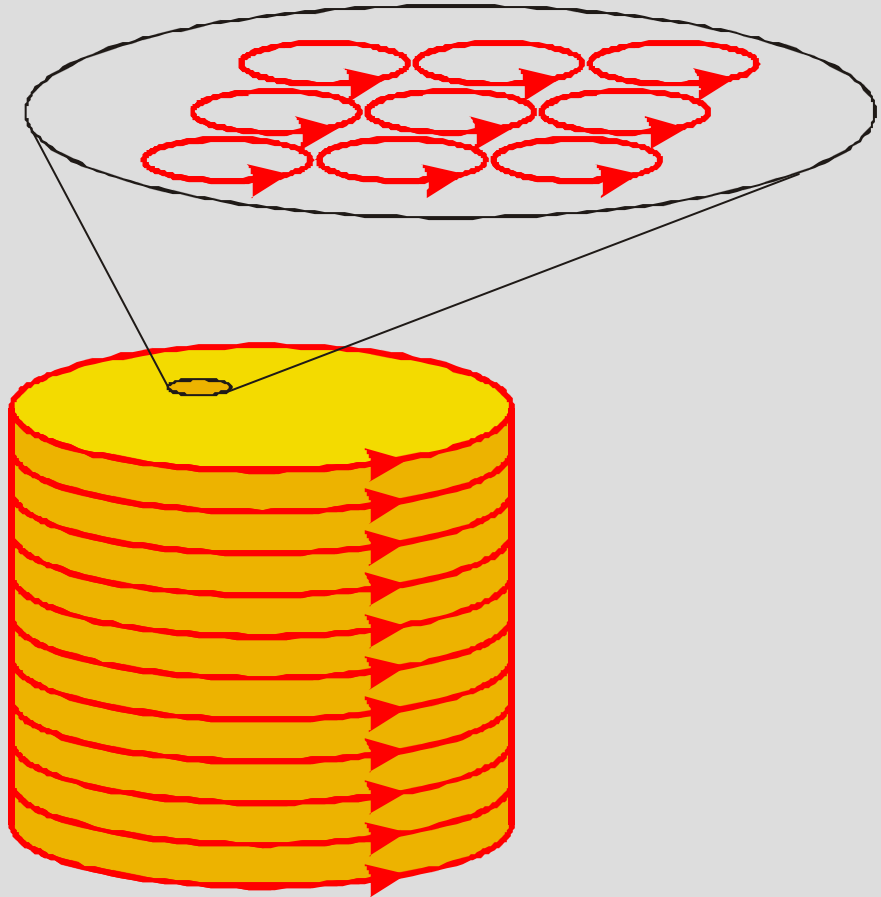
Magnetic dipole



$$B = \frac{\mu_0}{4\pi r^3} \times \left[\frac{3}{r^2} (\boldsymbol{\mu} \cdot \mathbf{r}) \mathbf{r} - \boldsymbol{\mu} \right]$$

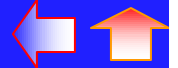
Magnetic dipole: A.m²

Magnetic material



Magnetization: A.m⁻¹

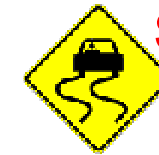
Magnetic moment: A.m²



Manipulation of magnetic materials:

↪ Application of a magnetic field

Zeeman energy: $E_Z = -\mu_0 \mathbf{H} \cdot \mathbf{M}_s$



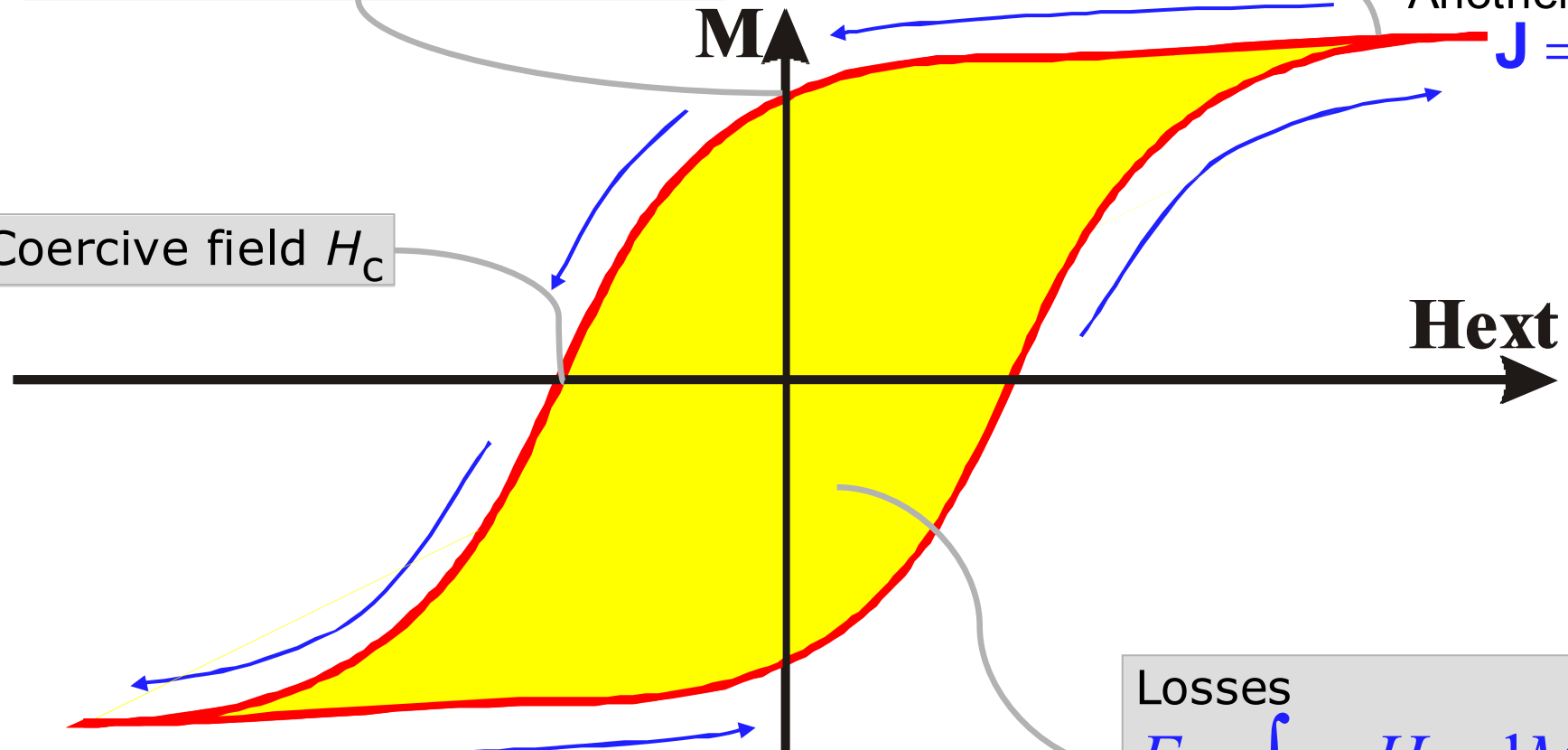
Spontaneous $\neq$ Saturation

Spontaneous magnetization M_s

Another notation
 $\mathbf{J} = -\mu_0 \mathbf{M}$

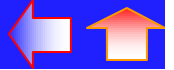
Remanent magnetization M_r

Coercive field H_c

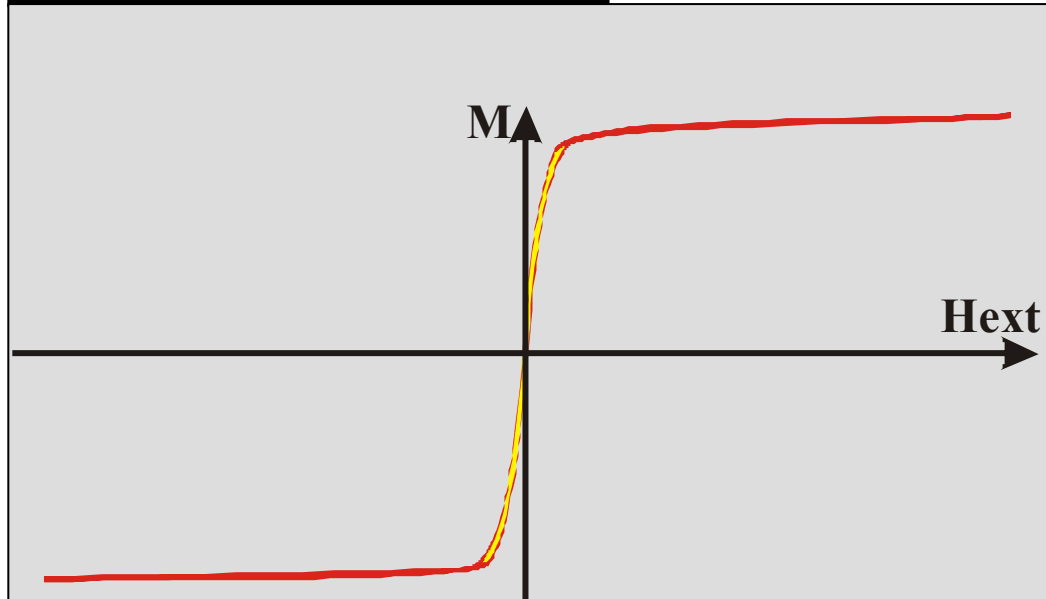


Losses

$$E = \oint \mu_0 H_{\text{ext}} dM$$



Soft materials

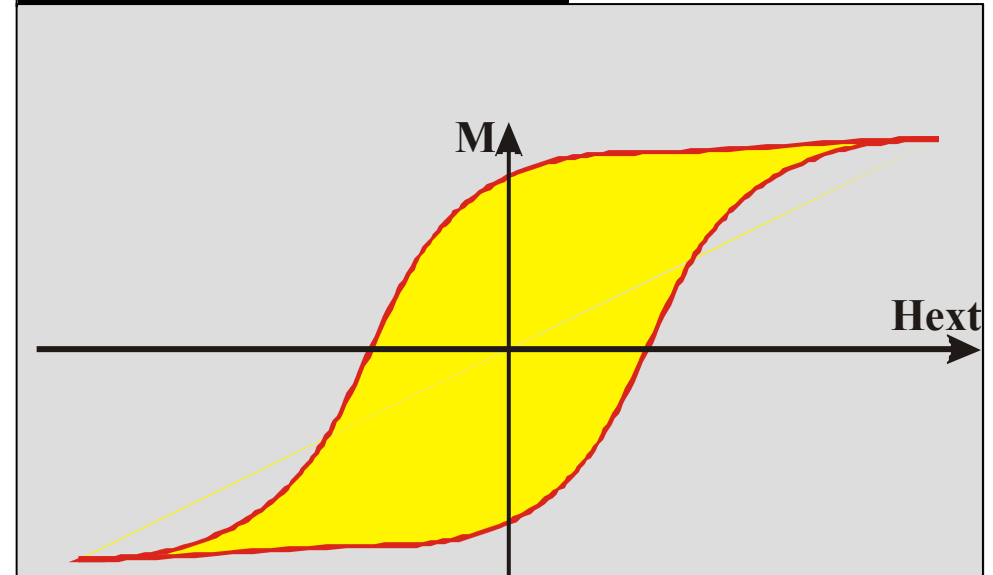


Transformers

Flux guides, sensors

Magnetic shielding

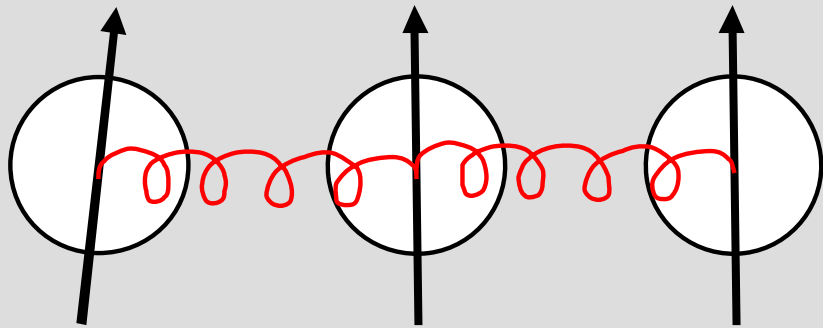
Hard materials



Permanent magnets, motors

Magnetic recording

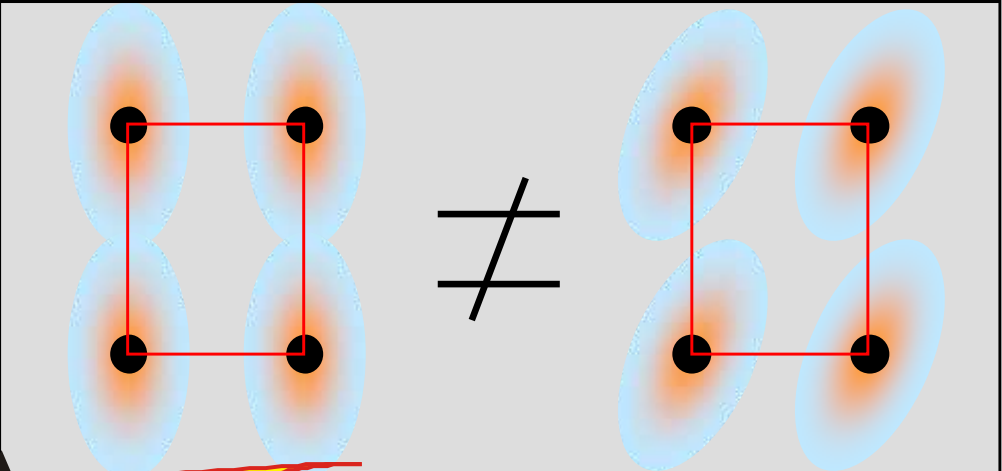
Exchange energy



$$E_{\text{Ech}} = -J_{1,2} \vec{S}_1 \cdot \vec{S}_2$$

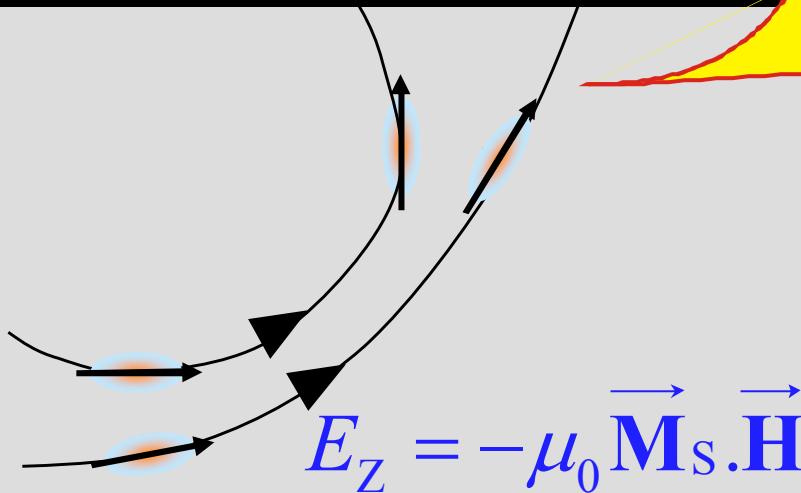
$$= A(\nabla \theta)^2$$

Magnetocrystalline anisotropy energy



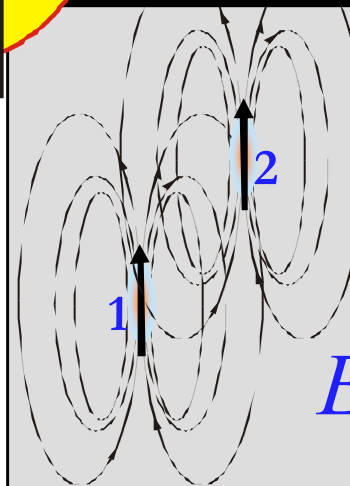
$$E_{\text{mc}} = K \sin^2(\theta)$$

Zeeman energy (enthalpy)



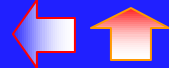
$$E_Z = -\mu_0 \vec{M}_s \cdot \vec{H}$$

Dipolar energy

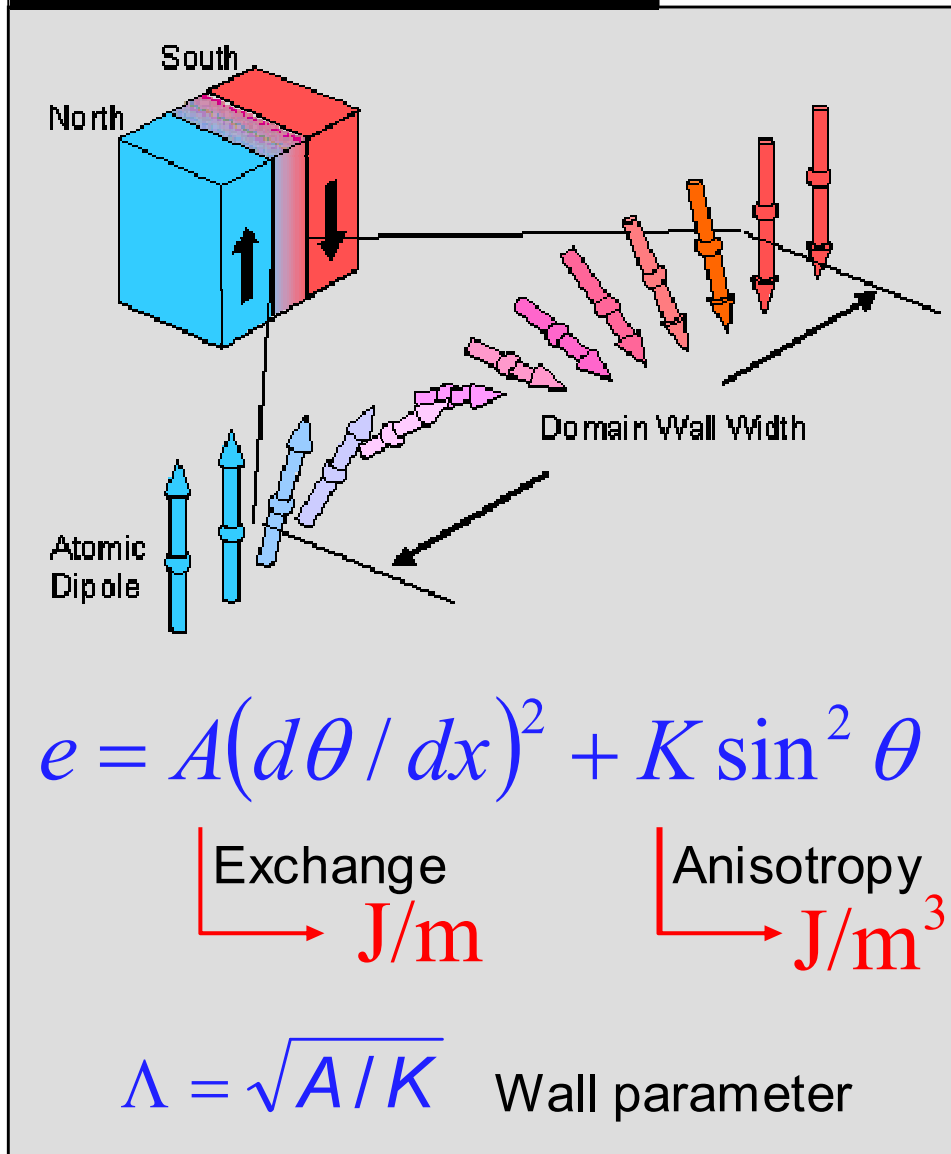


Long-ranged

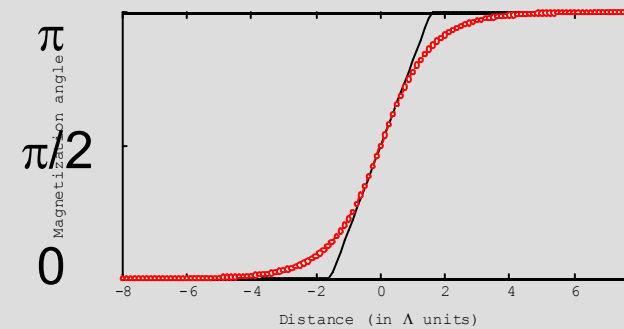
$$E_d = -\frac{1}{2} \mu_0 \vec{M}_s \cdot \vec{H}_d$$



Typical length scale:
Bloch wall width λ_B



Textbook solution and numerical values

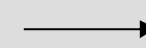


$$\theta = 2A \tan[\exp(x/\Lambda)]$$

$$\pi\sqrt{A/K}$$

Wall width (asymptote)

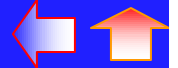
2 – 3 nm



100 nm

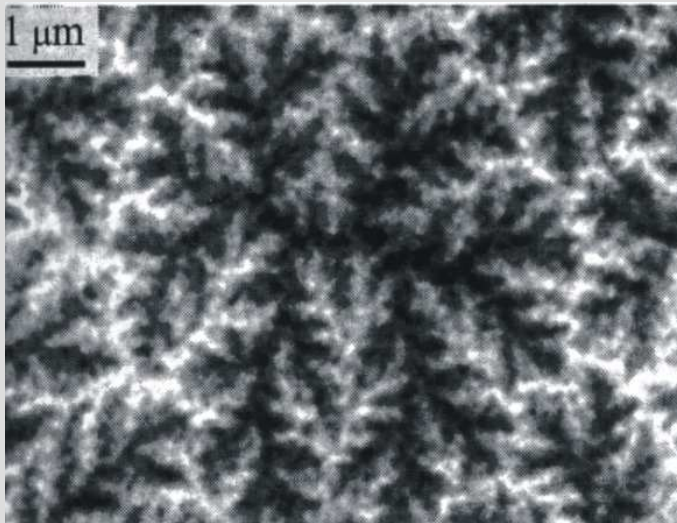
Hard

Soft



Bulk material

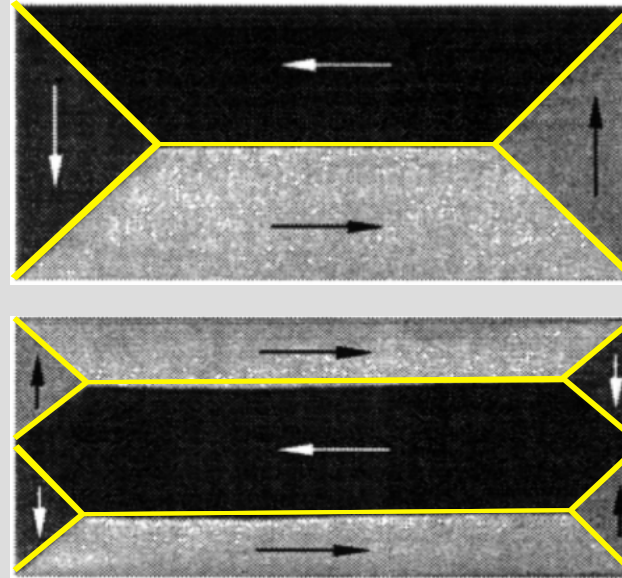
Numerous and complex magnetic domains



Co(1000) crystal – SEMPA
A. Hubert, *Magnetic domains*

Mesoscopic scale

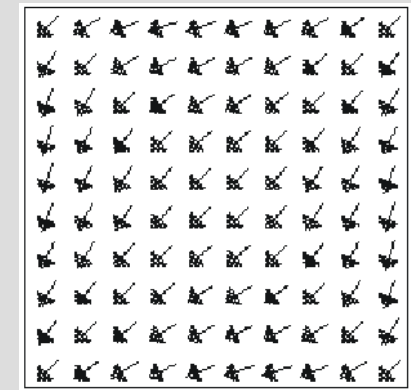
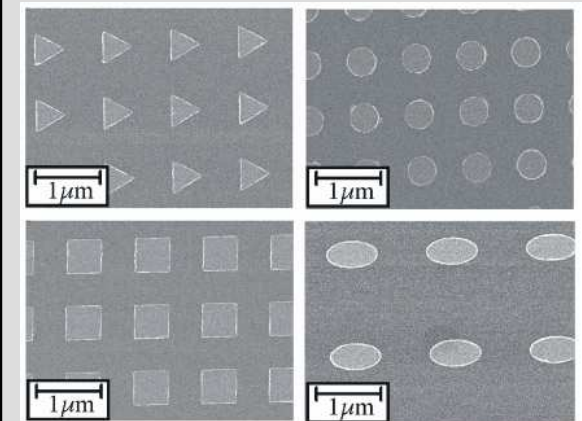
Small number of domains, simple shape



Microfabricated dots
Kerr magnetic imaging
A. Hubert, *Magnetic domains*

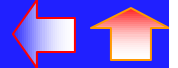
Nanometric scale

Magnetic single-domain



R.P. Cowburn,
*J.Phys.D:Appl.Phys.*33,
R1 (2000)

↪ Nanomagnetism $\approx$ mesoscopic magnetism
↪ Size of nanostructures to be compared with a relevant length scale. No universal scale!



0. Introduction

1. A word about dipolar energy

2. Single-domain: Stoner-Wohlfarth, superparamagnetism

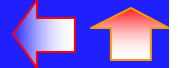
3. Near-single domain: edge states, magnetization reversal

4. Flux-closure domains and vortices

5. Domain walls in stripes

6. Summary on magnetic length scales

7. Inter-objects dipolar interactions



Density of dipolar energy

$$E_d(\mathbf{r}) = -\frac{1}{2} \mu_0 \mathbf{M}(\mathbf{r}) \cdot \mathbf{H}_d(\mathbf{r})$$

$$(E_Z = -\mu_0 \vec{M}_S \cdot \vec{H})$$

By definition $\text{div}(\mathbf{H}_d) = -\text{div}(\mathbf{M})$. As $\text{curl}(\mathbf{H}_d) = \mathbf{0}$ we have (analogy with electrostatics):

$$\mathbf{H}_d(\mathbf{r}) = -M_s \iiint_{\text{space}} \frac{\text{div}[\mathbf{m}(\mathbf{r}')] \cdot (\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^3 r'$$

$\rho(\mathbf{r}) = -M_s \text{div}[\mathbf{m}(\mathbf{r})]$ is called the **volume density of magnetic charges**

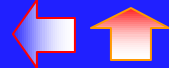
To lift the divergence that may arise at sample boundaries a volume integration around the boundaries yields:

$$\mathbf{H}_d(\mathbf{r}) = M_s \left(- \iiint_{\text{space}} \frac{\text{div}[\mathbf{m}(\mathbf{r}')] \cdot (\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^3 r' + \iint_{\text{sample}} \frac{[\mathbf{m}(\mathbf{r}') \cdot \mathbf{n}(\mathbf{r}')] \cdot (\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 r' \right)$$

$\sigma(\mathbf{r}) = M_s \mathbf{m}(\mathbf{r}) \cdot \mathbf{n}(\mathbf{r})$ is called the **surface density of magnetic charges**, where $\mathbf{n}(\mathbf{r})$ is the outgoing unit vector at boundaries



Do not forget boundaries between samples with different M_s



Some ways to handle dipolar energy

Integrated dipolar energy:

$$\mathcal{E} = -\frac{1}{2} \mu_0 \iiint_{\text{sample}} \mathbf{M} \cdot \mathbf{H}_d \cdot dV$$

Notice: six-fold integral over space:
non-linear, long-range, time-consuming.

Bottle-neck of micromagnetic calculations

Usefull theorem for finite samples:

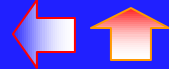
$$\mathcal{E} = -\frac{1}{2} \mu_0 \iiint_{\text{sample}} \mathbf{M} \cdot \mathbf{H}_d \cdot dV = \frac{1}{2} \mu_0 \iiint_{\text{space}} \mathbf{H}_d^2 \cdot dV$$

⇒ $\mathcal{E}$ is always positive

⇒ Significance of (BHmax) for permanent magnets

$$\begin{aligned} -\frac{1}{2} \mu_0 \iiint_{\text{sample}} (\mathbf{M} + \mathbf{H}_d) \cdot \mathbf{H}_d \cdot dV &= -\frac{1}{2} \mu_0 \iiint_{\text{sample}} \mathbf{B} \cdot \mathbf{H}_d \cdot dV \\ &= \frac{1}{2} \mu_0 \iiint_{\text{space} \setminus \text{sample}} \mathbf{H}_d^2 \cdot dV \end{aligned}$$

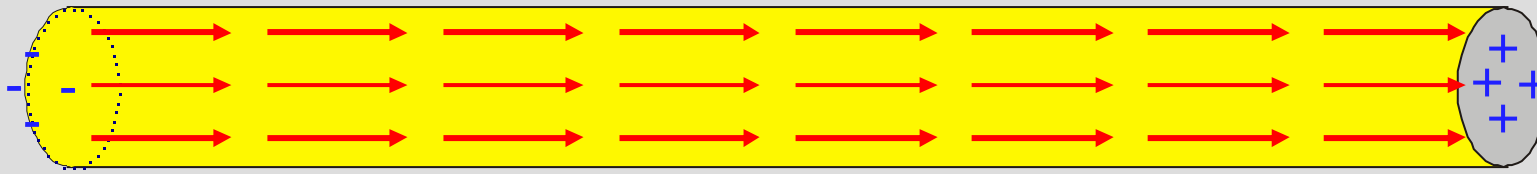
Energy available outside the sample, ie usefull for devices



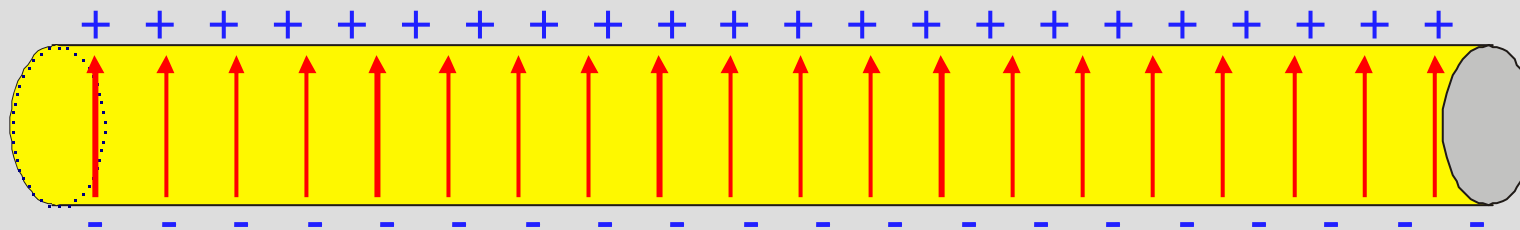
Volume: $\rho(\mathbf{r}) = -M_s \text{div}[\mathbf{m}(\mathbf{r})]$

Surface: $\sigma(\mathbf{r}) = M_s \mathbf{m}(\mathbf{r}) \cdot \mathbf{n}(\mathbf{r})$

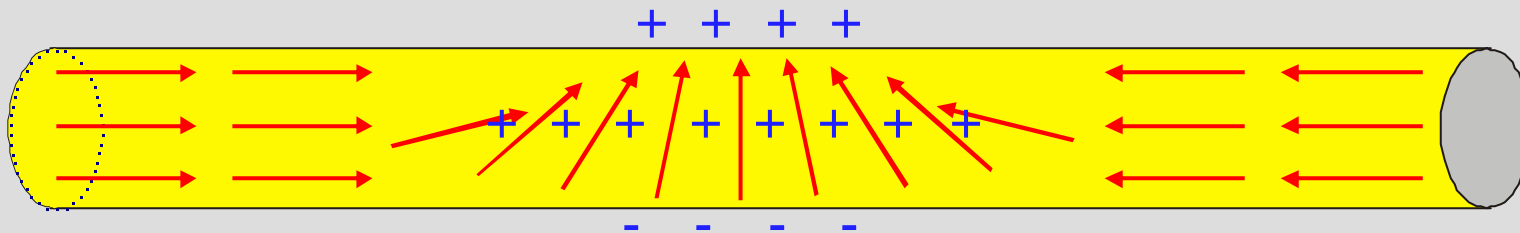
Examples of magnetic charges



Notice: no charges and $\epsilon=0$ for infinite cylinder

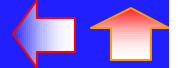


Charges on surfaces



Surface and volume charges





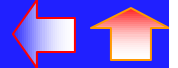
Assume uniform magnetization $\mathbf{M}(\mathbf{r}) \equiv \mathbf{M} = M_s (m_x \mathbf{x} + m_y \mathbf{y} + m_z \mathbf{z}) = M_s m_i \mathbf{u}_i$

$$\begin{aligned} \mathbf{H}_d(\mathbf{r}) &= M_s \iint_{\text{sample}} \frac{[\mathbf{m} \cdot \mathbf{n}(\mathbf{r}')].(\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 r' \\ &= M_s m_i \iint_{\text{sample}} \frac{n_i(\mathbf{r}') \cdot (\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 r' \end{aligned}$$

$$\begin{aligned} \mathcal{E}_d &= -\frac{1}{2} \mu_0 \iiint_{\text{sample}} \mathbf{H}_d(\mathbf{r}) \cdot \mathbf{M} d^3 \mathbf{r} \\ &= -\frac{1}{2} \mu_0 M_s^2 m_i \iiint_{\text{sample}} d^3 \mathbf{r} \iint_{\text{sample}} \frac{n_i(\mathbf{r}') \cdot [\mathbf{m} \cdot (\mathbf{r}' - \mathbf{r})]}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 \mathbf{r}' \\ &= -K_d m_i m_j \iiint_{\text{sample}} d^3 \mathbf{r} \iint_{\text{sample}} \frac{n_i(\mathbf{r}') \cdot (r_j' - r_j)}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 \mathbf{r}' \end{aligned}$$

$$\mathcal{E}_d = K_d V N_{ij} m_i m_j = K_d V \mathbf{m} \cdot \bar{\mathbf{N}} \cdot \mathbf{m} \qquad K_d = \frac{1}{2} \mu_0 M_s^2$$

See more detailed approach: M. Beleggia and M. De Graef, J. Magn. Magn. Mater. 263, L1-9 (2003)



$$\varepsilon_d = K_d N_{ij} m_i m_j = K_d {}^t \mathbf{m} \cdot \overline{\mathbf{N}} \cdot \mathbf{m}$$

N is a positive second-order tensor

$$\langle \mathbf{H}_d(\mathbf{r}) \rangle = -M_s \overline{\mathbf{N}} \cdot \mathbf{m}$$



...and can be defined and diagonalized for any sample shape

$$N = \begin{pmatrix} N_x & 0 & 0 \\ 0 & N_y & 0 \\ 0 & 0 & N_z \end{pmatrix}$$

$$\varepsilon_d = K_d (N_x m_x^2 + N_y m_y^2 + N_z m_z^2)$$

$$\langle H_{d,i}(\mathbf{r}) \rangle = -M_s N_i \quad \leftarrow \text{Valid along main axes only!}$$

$$N_x + N_y + N_z = 1$$

What with ellipsoids???

Self-consistency: the magnetization must be at equilibrium and therefore fulfill $\mathbf{m} // \mathbf{H}_{\text{eff}}$

➡ Assuming $\mathbf{H}_{\text{applied}}$ and $\mathbf{H}_a$ are uniform, this requires $\mathbf{H}_d(\mathbf{r})$ is uniform. This is satisfied only in volumes limited by polynomial surfaces of order 2 or less: slabs, cylinders, ellipsoids (+paraboloids and hyperboloids).

J. C. Maxwell, Clarendon 2, 66-73 (1872)



Ellipsoids

$$N_x = \frac{1}{2} abc \int_0^\infty \left[(a^2 + \eta) \sqrt{(a^2 + \eta)(b^2 + \eta)(c^2 + \eta)} \right]^{-1} d\eta$$

General ellipsoid:
main axes (a,c,c)

$$N_x = \frac{\alpha^2}{1 - \alpha^2} \left[\frac{1}{\sqrt{1 - \alpha^2}} \operatorname{Asinh} \left(\frac{\sqrt{1 - \alpha^2}}{\alpha} \right) - 1 \right]$$

For prolate revolution ellipsoid:
(a,c,c) with $\alpha = c/a < 1$

$$N_y = N_z = \frac{1}{2} (1 - N_x)$$

$$N_x = \frac{\alpha^2}{\alpha^2 - 1} \left[1 - \frac{1}{\sqrt{\alpha^2 - 1}} \operatorname{Asin} \left(\frac{\sqrt{\alpha^2 - 1}}{\alpha} \right) \right]$$

For oblate revolution ellipsoid:
(a,c,c) with $\alpha = c/a > 1$

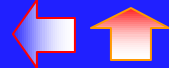
Cylinders

$$N_x = 0; \quad N_y = c/(b+c); \quad N_z = b/(b+c) \quad \text{For a cylinder along } x$$

J. A. Osborn, Phys. Rev. 67, 351 (1945).

For prisms, see: **A. Aharoni, J. Appl. Phys. 83, 3432 (1998)**

More general forms, FFT approach: **M. Beleggia et al., J. Magn. Magn. Mater. 263, L1-9 (2003)**



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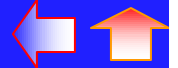
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Framework

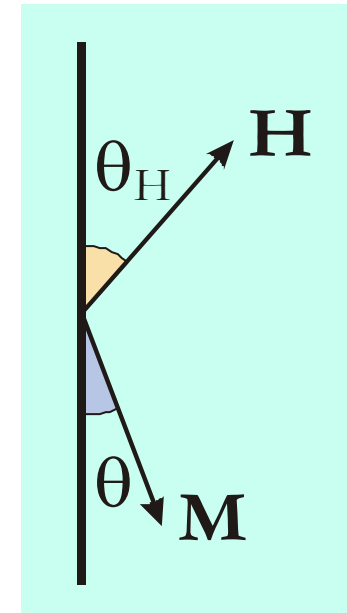
Approximation: $\vec{m}(\vec{r}) = \vec{M} = Cte$
(strong!)

$$E_{\text{tot}} = V [K_{\text{eff}} \sin^2 \theta - \mu_0 M_S H_{\text{ext}} \cos(\theta - \theta_H)]$$

$$K_{\text{eff}} = K_{\text{mc}} + K_d$$

Dimensionless units:

$$e = \sin^2(\theta) - 2h \cos(\theta - \theta_H) \quad \left(\begin{array}{l} e = E / VK \\ h = H / H_a \\ H_a = 2K / \mu_0 M_S \end{array} \right)$$



L. Néel, *Compte rendu Acad. Sciences* 224, 1550 (1947)

E. C. Stoner and E. P. Wohlfarth, *Phil. Trans. Royal. Soc. London* A240, 599 (1948)

IEEE Trans. Magn. 27(4), 3469 (1991) : reprint

Names used

- ↪ Uniform rotation / magnetization reversal
- ↪ Coherent rotation / magnetization reversal
- ↪ Macrospin etc.

$$e = \sin^2(\theta) + 2h \cos(\theta) \quad (\theta_H = 180^\circ)$$

Equilibrium states

$$\frac{\partial e}{\partial \theta} = 2 \sin \theta (\cos \theta - h) \quad \frac{\partial e}{\partial \theta} = 0 \Rightarrow \cos(\theta_m) = h$$

$$\theta \equiv 0 [\pi]$$

Stability

$$\frac{\partial^2 e}{\partial \theta^2} = 2 \cos 2\theta - 2h \cos \theta$$

$$= 4 \cos^2 \theta - 2 - 2h \cos \theta$$

$$\frac{\partial^2 e}{\partial \theta^2}(0) = 2(1 - h)$$

$$\frac{\partial^2 e}{\partial \theta^2}(\theta_m) = 2(h^2 - 1)$$

$$\frac{\partial^2 e}{\partial \theta^2}(\pi) = 2(1 + h)$$

Energy barrier

$$\Delta e = e(\theta_{\max}) - e(0)$$

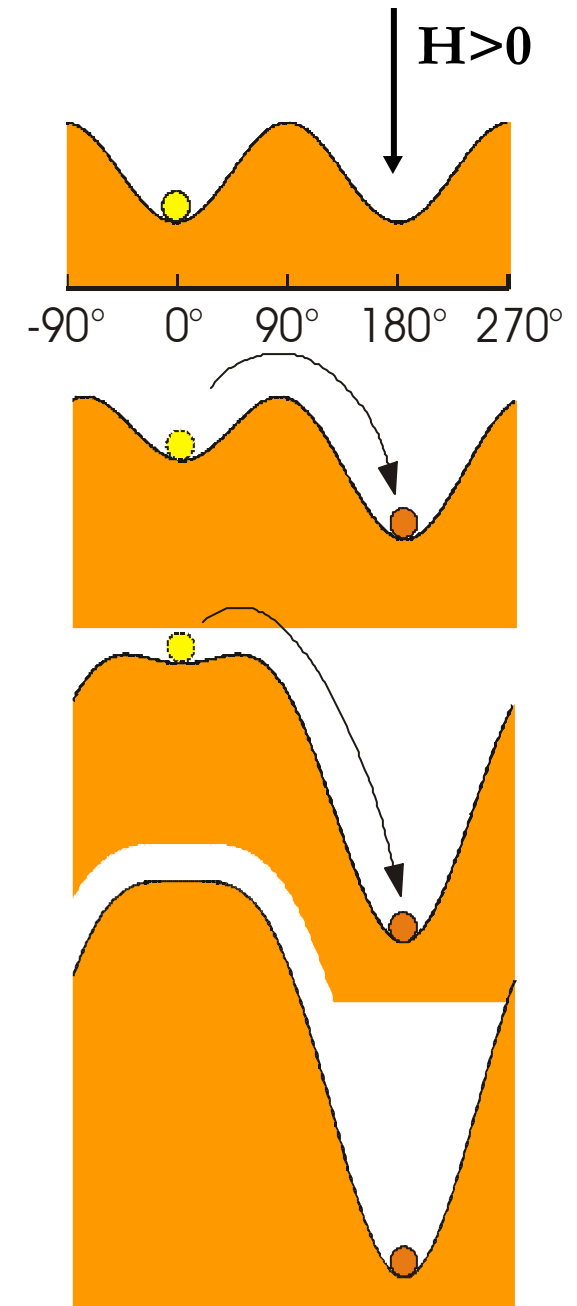
$$= 1 - h^2 + 2h^2 - 2h$$

$$= (1 - h)^2$$

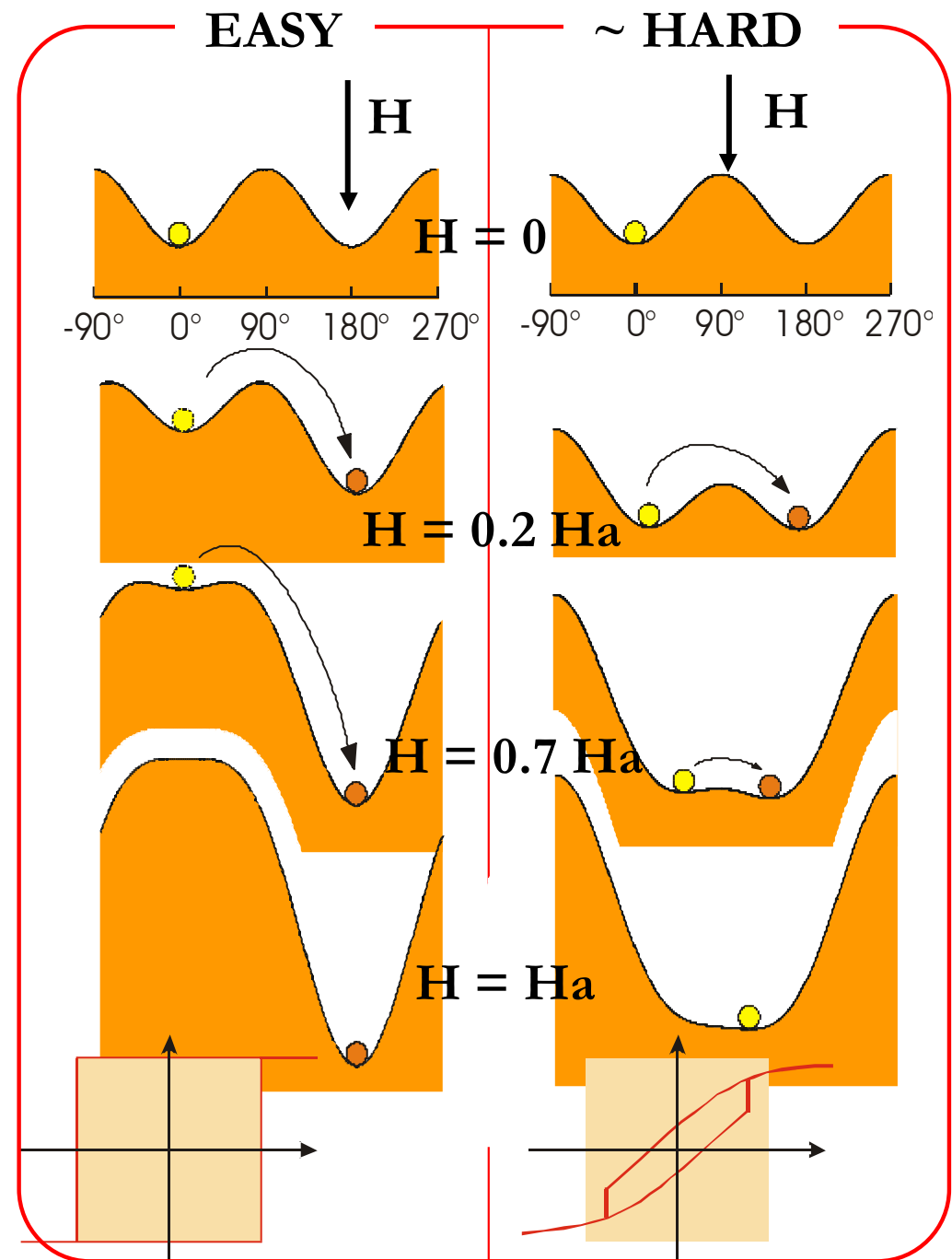
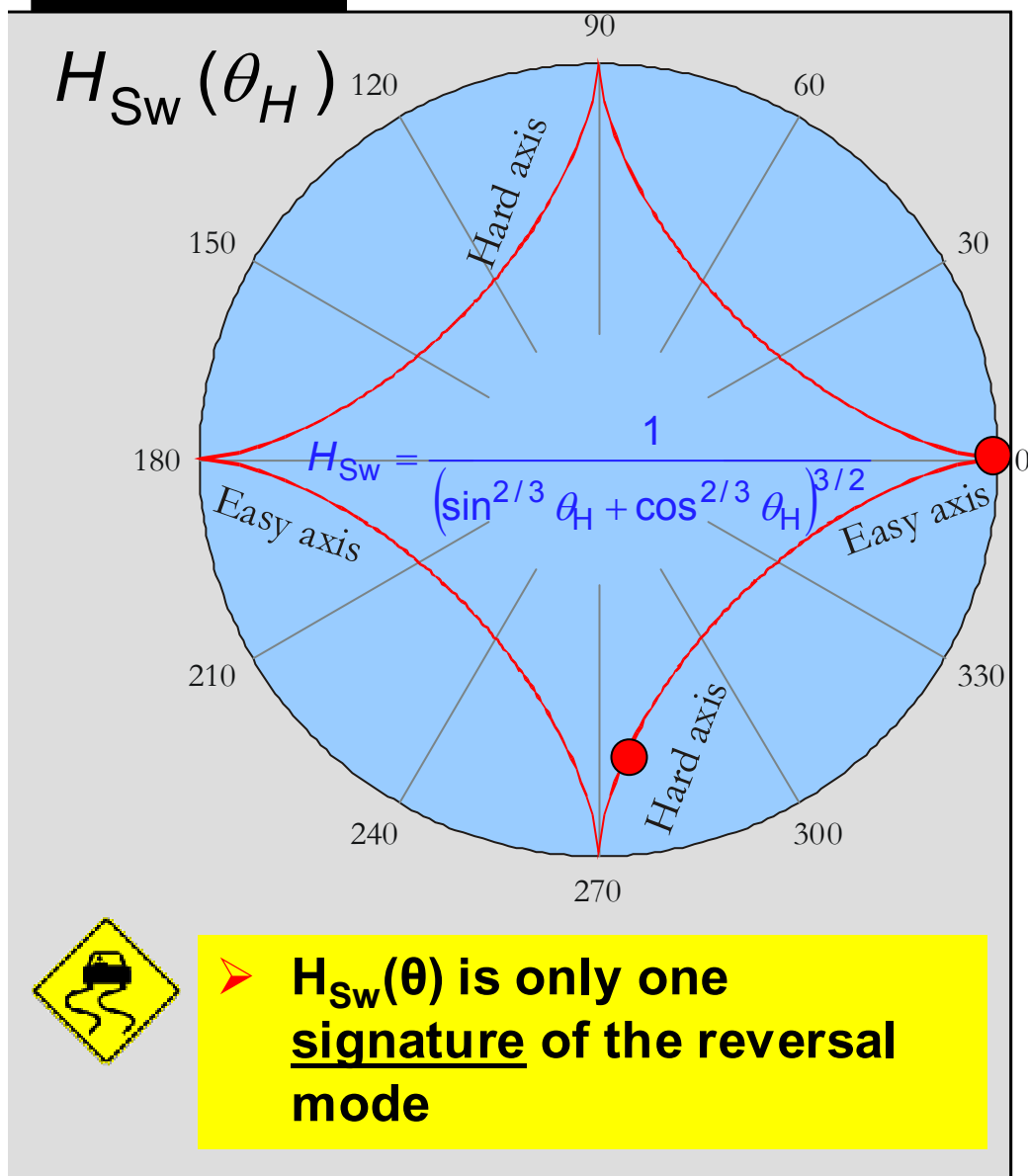
Switching

$$h = 1$$

$$H = H_a = 2K / \mu_0 M_s$$



'Astroid' curve



J. C. Slonczewski, Research Memo RM
003.111.224, IBM Research Center (1956)

Switching field = Reversal field

A value of field at which an irreversible (abrupt) jump of magnetization angle occurs.

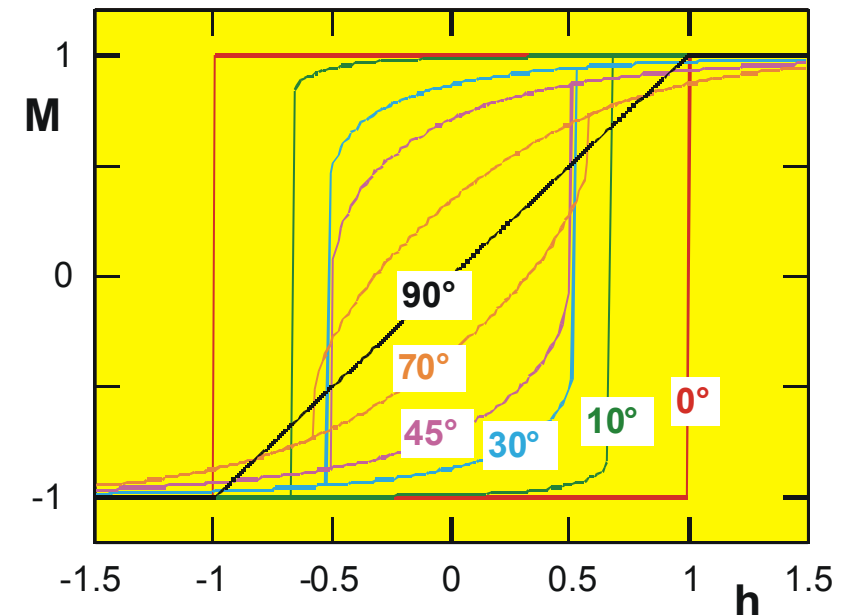
Can be measured only in single particles.

Coercive field

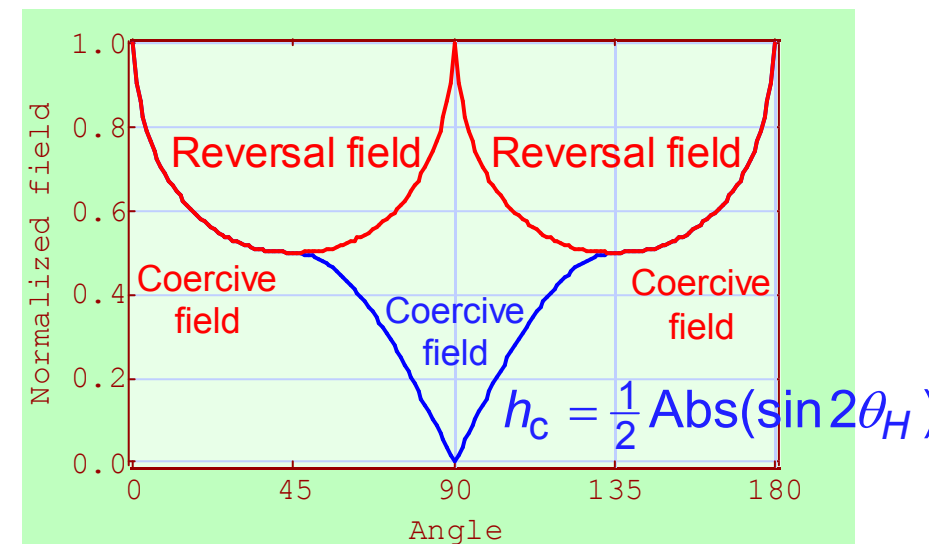
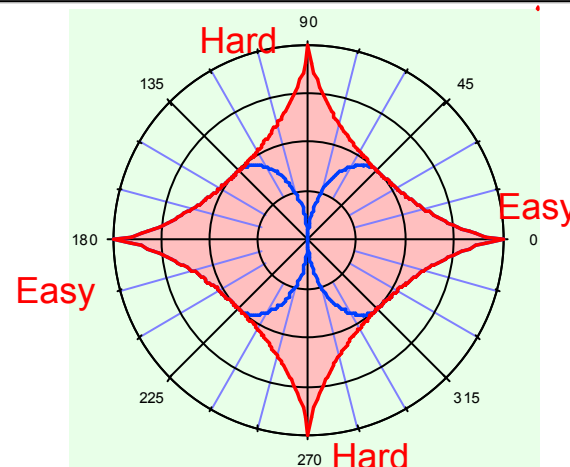
The value of field at which $\mathbf{M} \cdot \mathbf{H} = 0$ ($\theta = \theta_H \pm \pi/2$)

A quantity that can be measured in real materials (large number of 'particles').

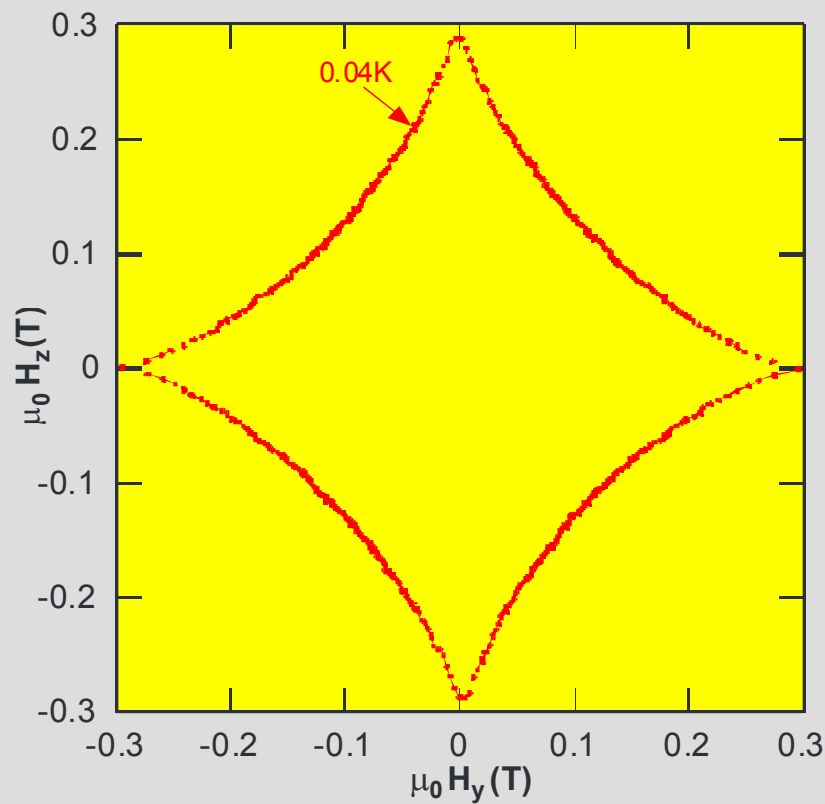
May be or may not be a measure of the mean switching field at the microscopic level



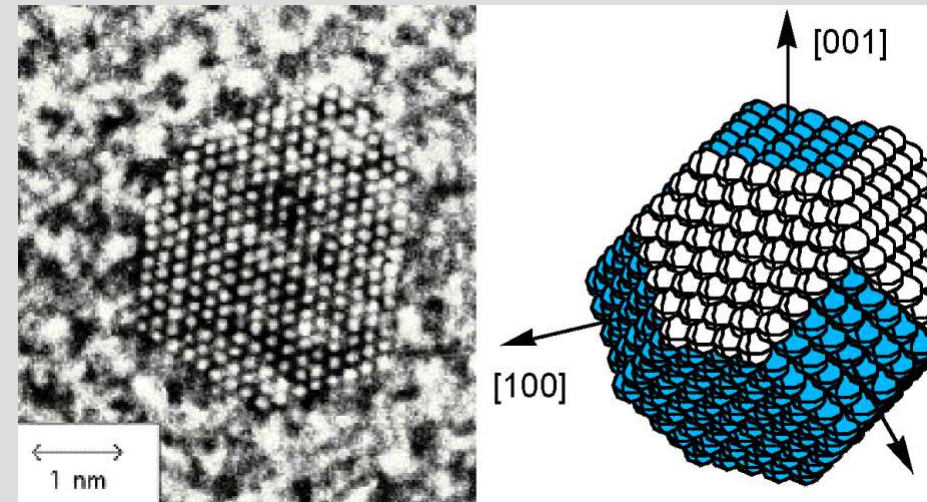
$$h_{Sw} = \frac{1}{(\sin^{2/3} \theta_H + \cos^{2/3} \theta_H)^{3/2}}$$



Experimental evidence

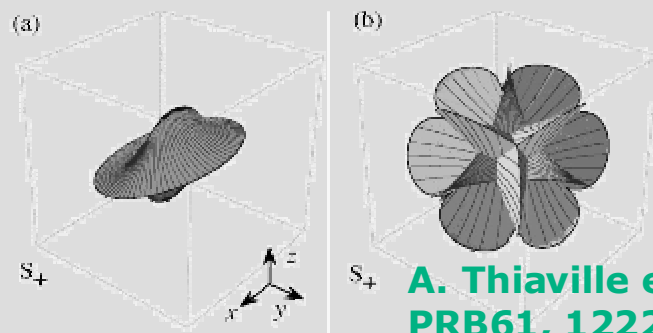


First evidence: W. Wernsdorfer et al., Phys. Rev. Lett. 78, 1791 (1997)

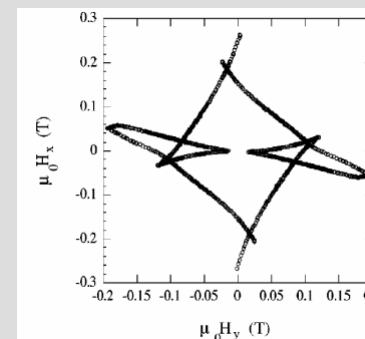


M. Jamet et al., Phys. Rev. Lett., 86, 4676 (2001)

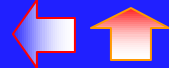
Extensions: 3D, arbitrary anisotropy etc.



A. Thiaville et al., PRB61, 12221 (2000)



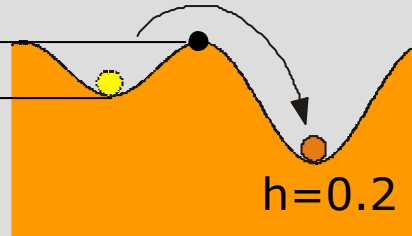
M. Jamet et al., PRB69, 024401 (2004)



Barrier height

$$\Delta e = e(\theta_{\max}) - e(0) = (1-h)^2$$

$$(h = \mu_0 M_S H / 2K)$$



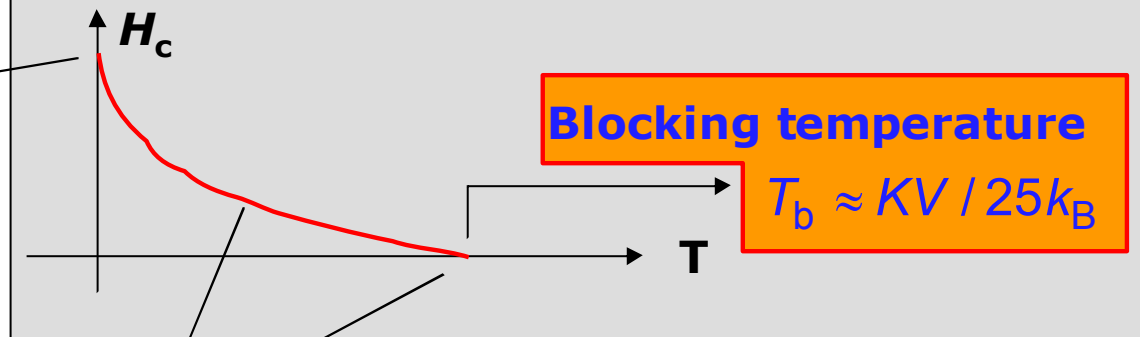
Thermal activation

Brown, Phys.Rev.130, 1677 (1963)

$$\tau = \tau_0 \exp\left(\frac{\Delta E}{k_B T}\right) \Rightarrow \Delta E = k_B T \ln(\tau / \tau_0)$$

Lab measurement : $\tau = 1\text{s}$ $\sim 25k_B T$

$$H_c = \frac{2K}{\mu_0 M_S} \left(1 - \sqrt{\frac{25k_B T}{KV}}\right)$$

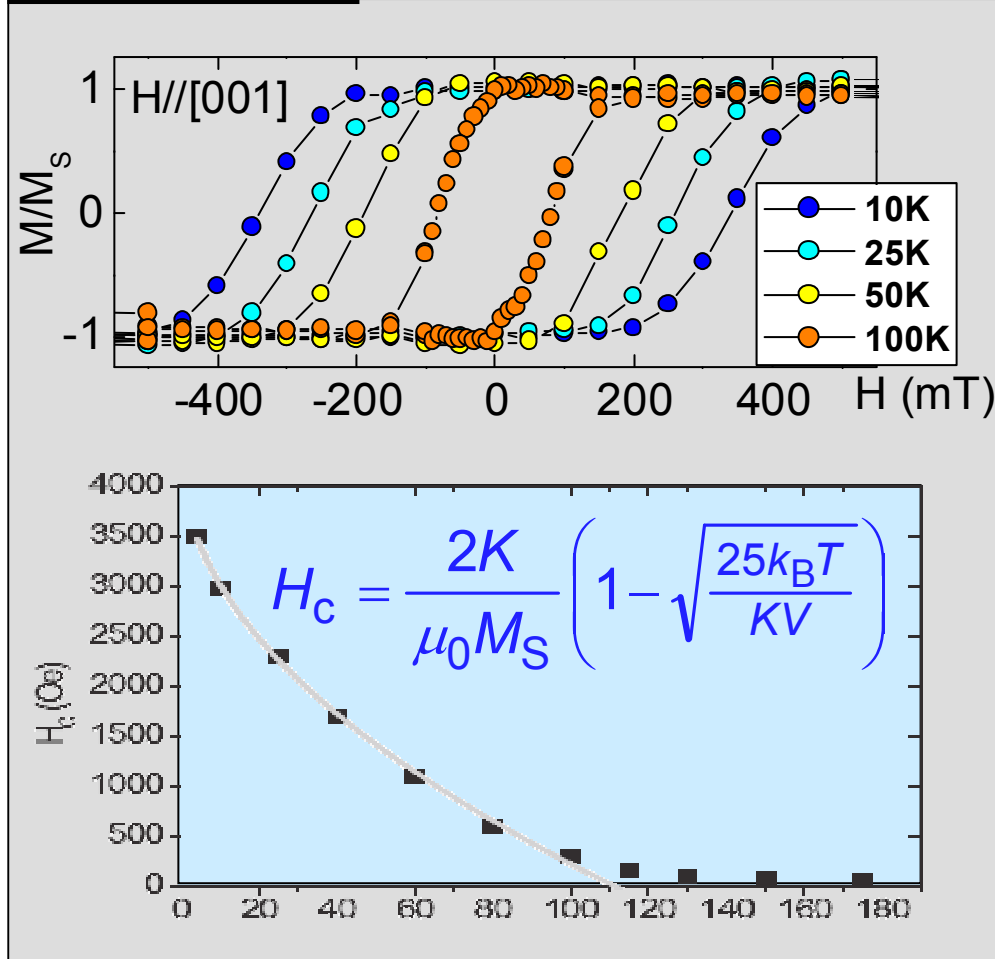


Information about
anisotropy density

Information about total
effective anisotropy

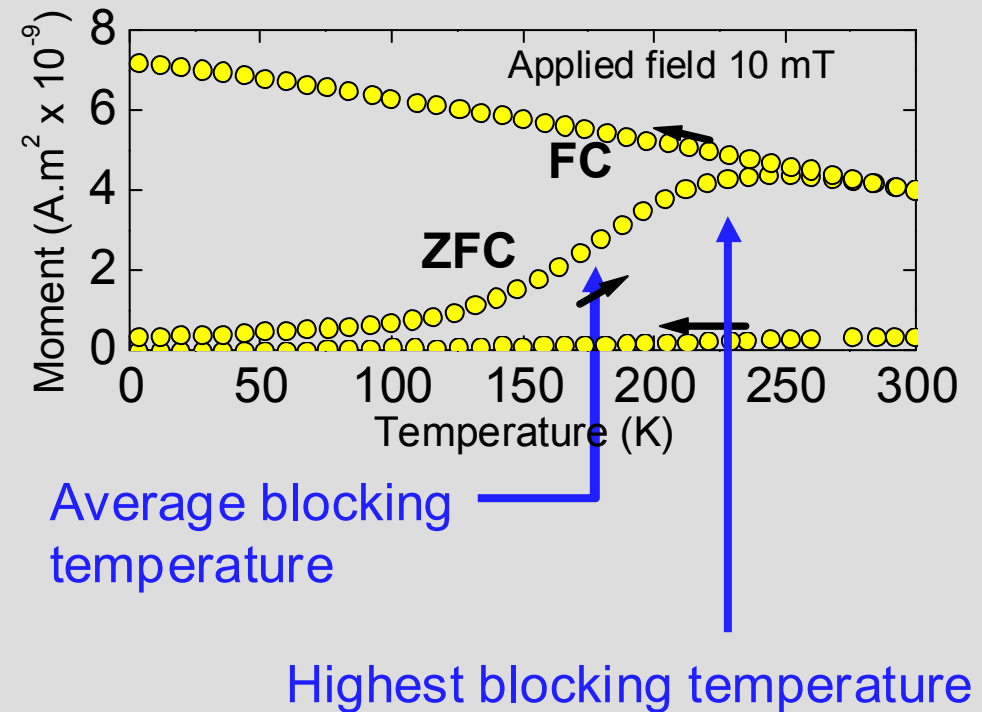
Notice, for magnetic recording : $t \approx 10^9\text{s}$ $KV_B \approx 40 - 60 k_B T$

Hysteresis loops



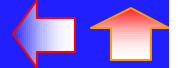
FC / ZFC

Field-cooled / Zero-field-cooled magnetization



Crude analysis

- ↪ $T = 0\text{K} > \text{effective anisotropy}$
- ↪ $T_b > \text{activation volume}$



0. Introduction

1. A word about dipolar energy

2. Single-domain: Stoner-Wohlfarth, superparamagnetism

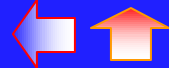
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5. Domain walls in stripes

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7. Inter-objects dipolar interactions

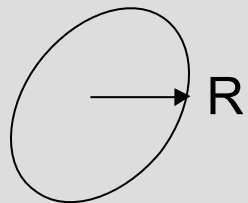


Upper bound for dipolar fields in 2D

Estimation of an upper range of dipolar field in a 2D system

$$\|H_d(R)\| \leq \oint \frac{2\pi r dr}{r^3} \quad \text{Integration}$$

Local dipole: $1/r^3$

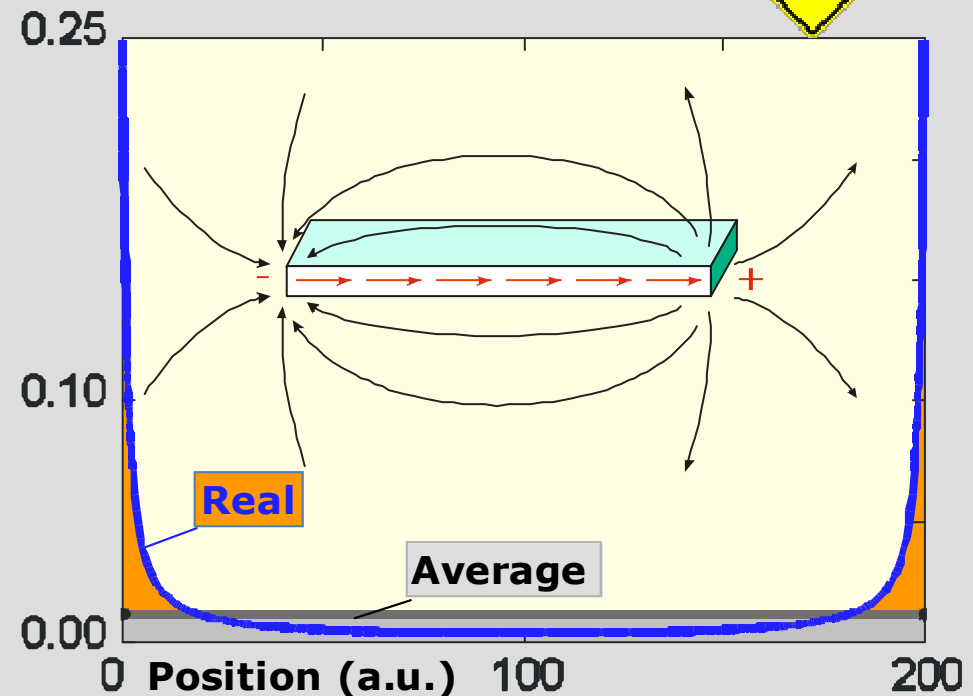
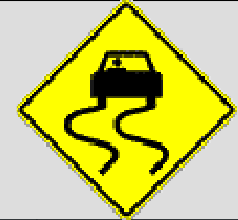


$$\|H_d(R)\| \leq Cte + 1/R$$

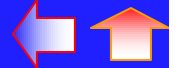
Convergence with finite radius
(typically thickness)

Non-homogeneity of dipolar fields in 2D

Example: flat stripe with thickness/height = 0.0125



- ➡ Dipolar fields are weak and short-ranged in 2D or even lower-dimensionality systems
- ➡ Dipolar fields can be highly non-homogeneous in anisotropic systems like 2D
- ➡ Consequences on dot's non-homogenous state, magnetization reversal, collective effects etc.



Configurational anisotropy: deviations from single-domain

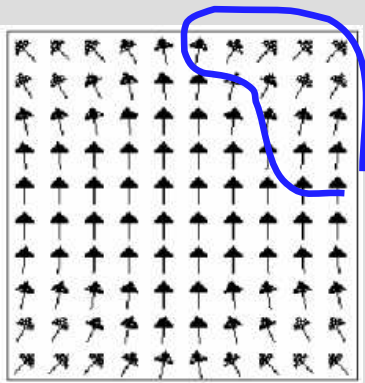
Strictly speaking, 'shape anisotropy' is of second order:

$$E_d = \frac{1}{2} \mu_0 (N_x M_x^2 + N_y M_y^2 + N_z M_z^2)$$

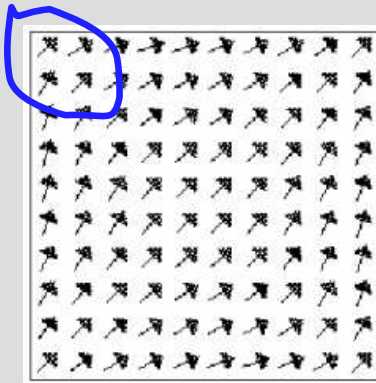
$$\text{2D: } E_{\text{tot}} = VK_d \sin^2 \theta$$

In real samples magnetization is never perfectly uniform: competition between exchange and dipolar

Num.Calc. (100nm)



Flower state
 $c/a > 2.7$



Leaf state
 $c/a < 2.7$

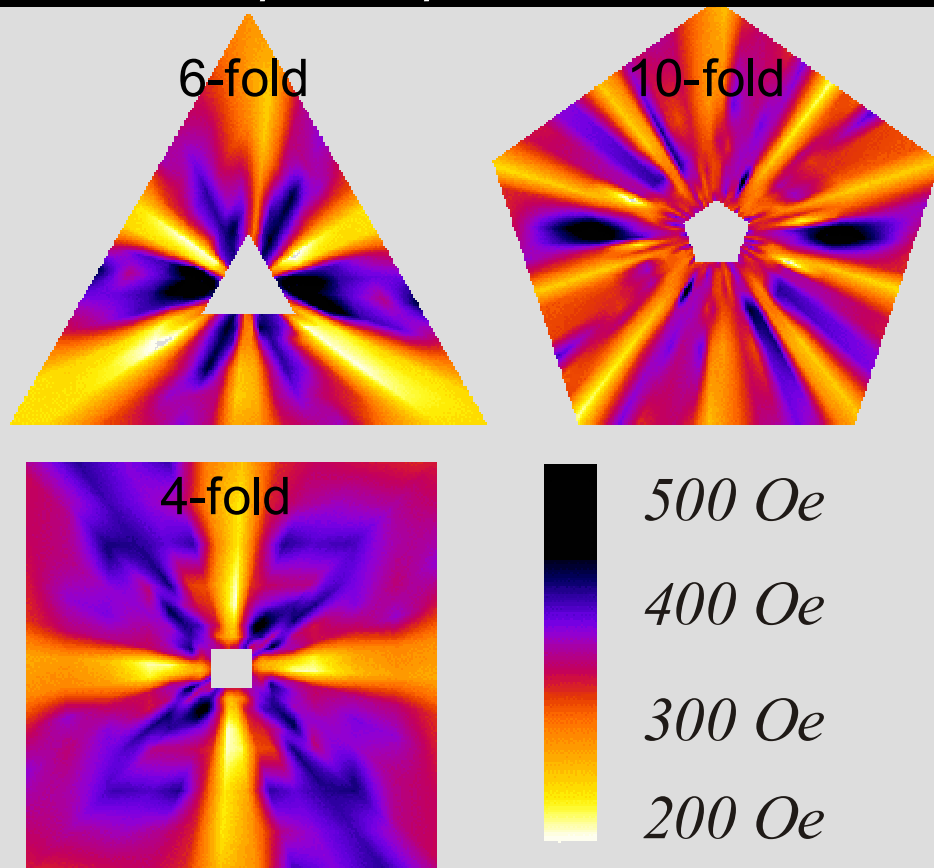
Configurational anisotropy
may be used to
stabilize stable configurations

↪ Higher order contributions to the anisotropy of the total energy

M. A. Schabes et al., JAP 64, 1347 (1988)

R.P. Cowburn et al., APL 72, 2041 (1998)

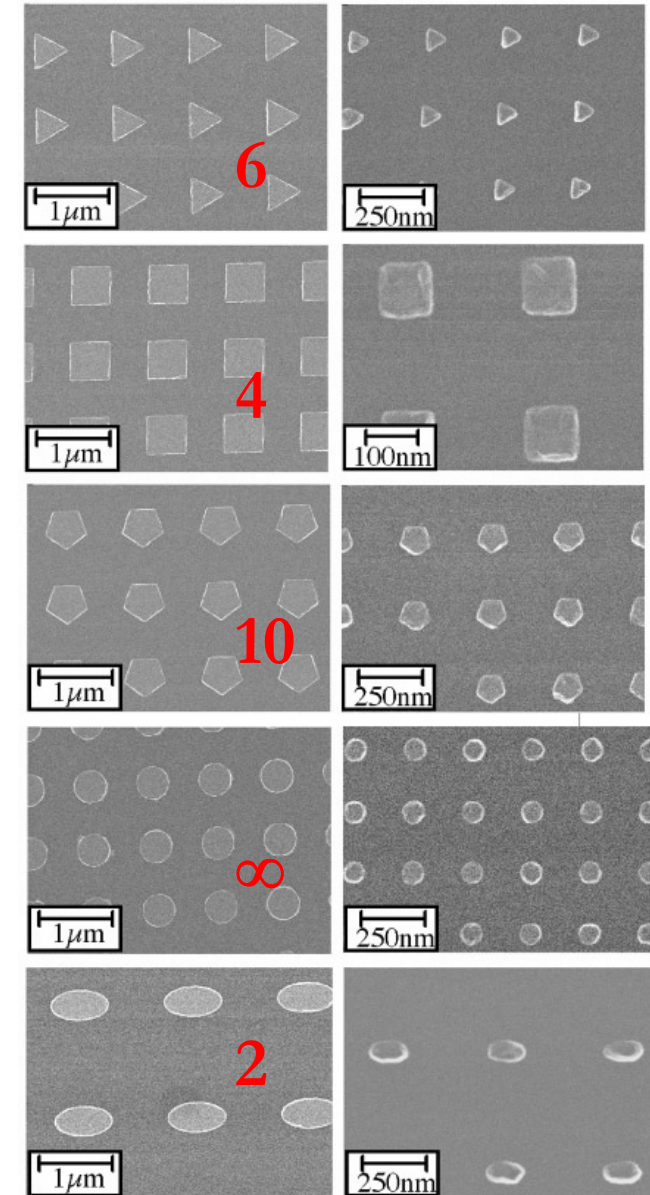
Polar plot of experimental configurational anisotropy with various symmetry



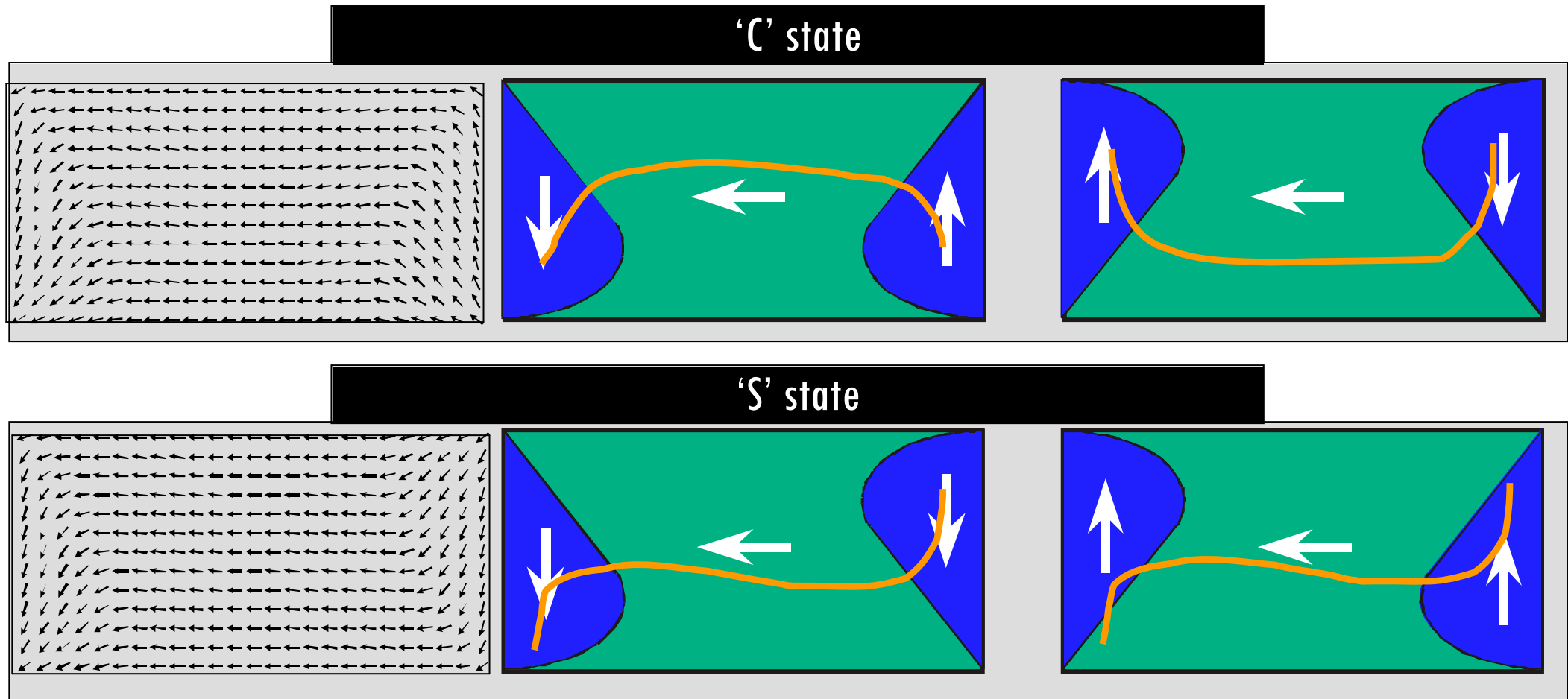
Color code: strength of anisotropy in a given direction

Radius: size of measured pattern

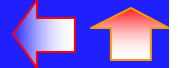
Direction: direction of measurement



R.P. Cowburn, J.Phys.D:Appl.Phys.33, R1-R16 (2000)

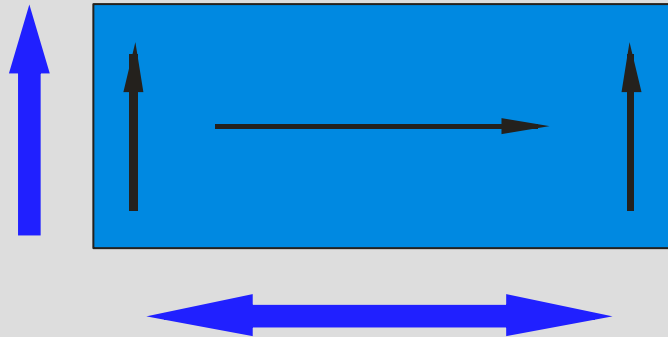


➤ At least 8 nearly-equivalent ground-states for a rectangular dot
 ➤ Issue for the reproducibility of magnetization reversal



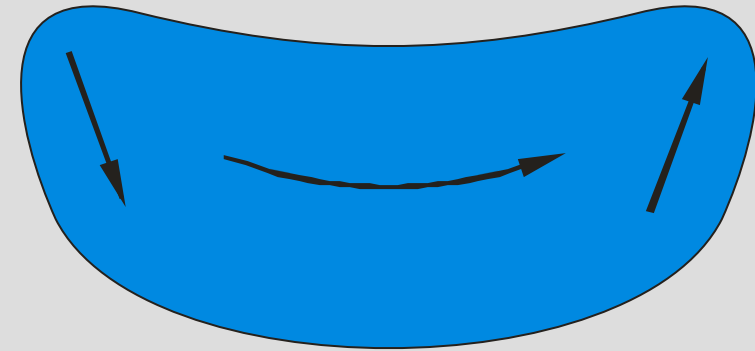
Preparation of 'S' state

Transverse field to keep
end domains aligned
parallel to each other



Longitudinal field to
reverse the magnetization

Preparation of 'C' state



End domains aligned mainly
antiparallel owing to a
dipolar shape effect

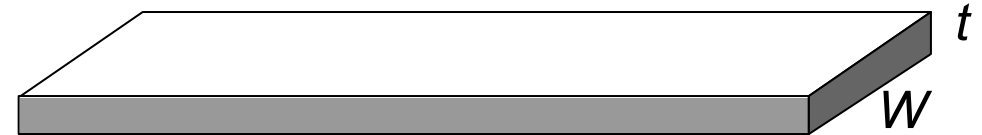
Purpose

➡ Avoid the formation of 180° domain walls during magnetization reversal

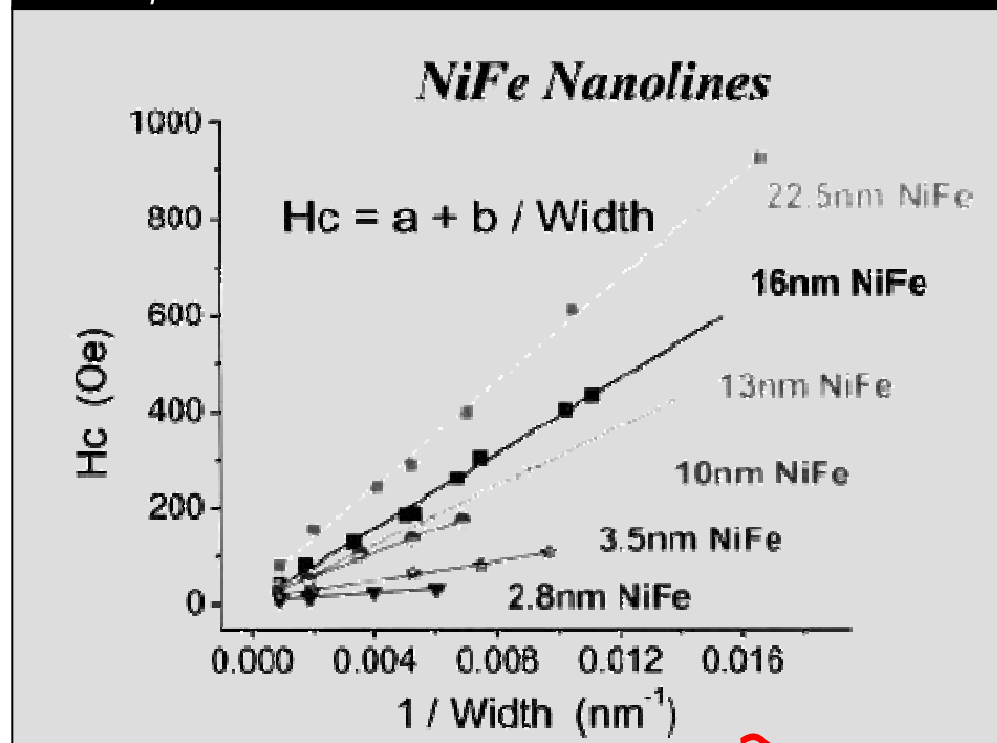


Hypotheses $\Rightarrow$ Soft magnetic material

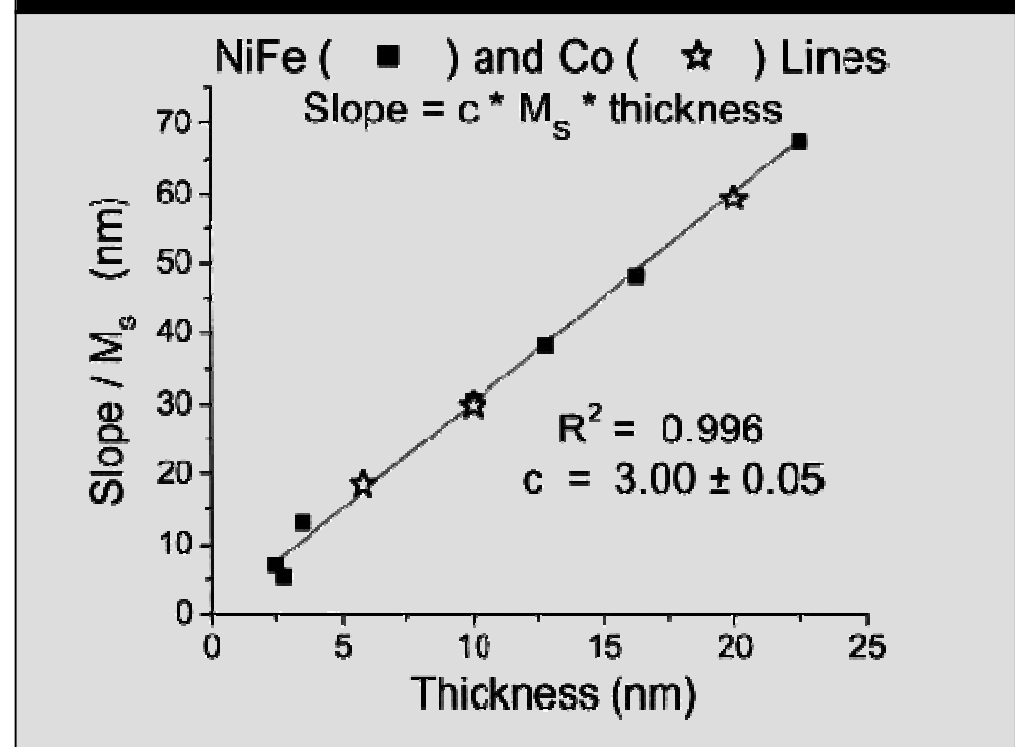
$\Rightarrow$ Not too small neither too large nanostructures



$H_c \sim 1/\text{Width}$



$H_c \sim M_s * \text{Thickness}$



$$H_c = a + 3M_s \frac{t}{W}$$

$\sim$ Lateral demagnetizing coefficient of the stripe



W. C. Uhlig & J. Shi,
Appl. Phys. Lett. 84, 759 (2004)

Magnetization is pinned at sharp ends

Numerical micromagnetic calculation

J.G. Zhu

6672 J. Appl. Phys., Vol. 87, No. 9, 1 May 2000

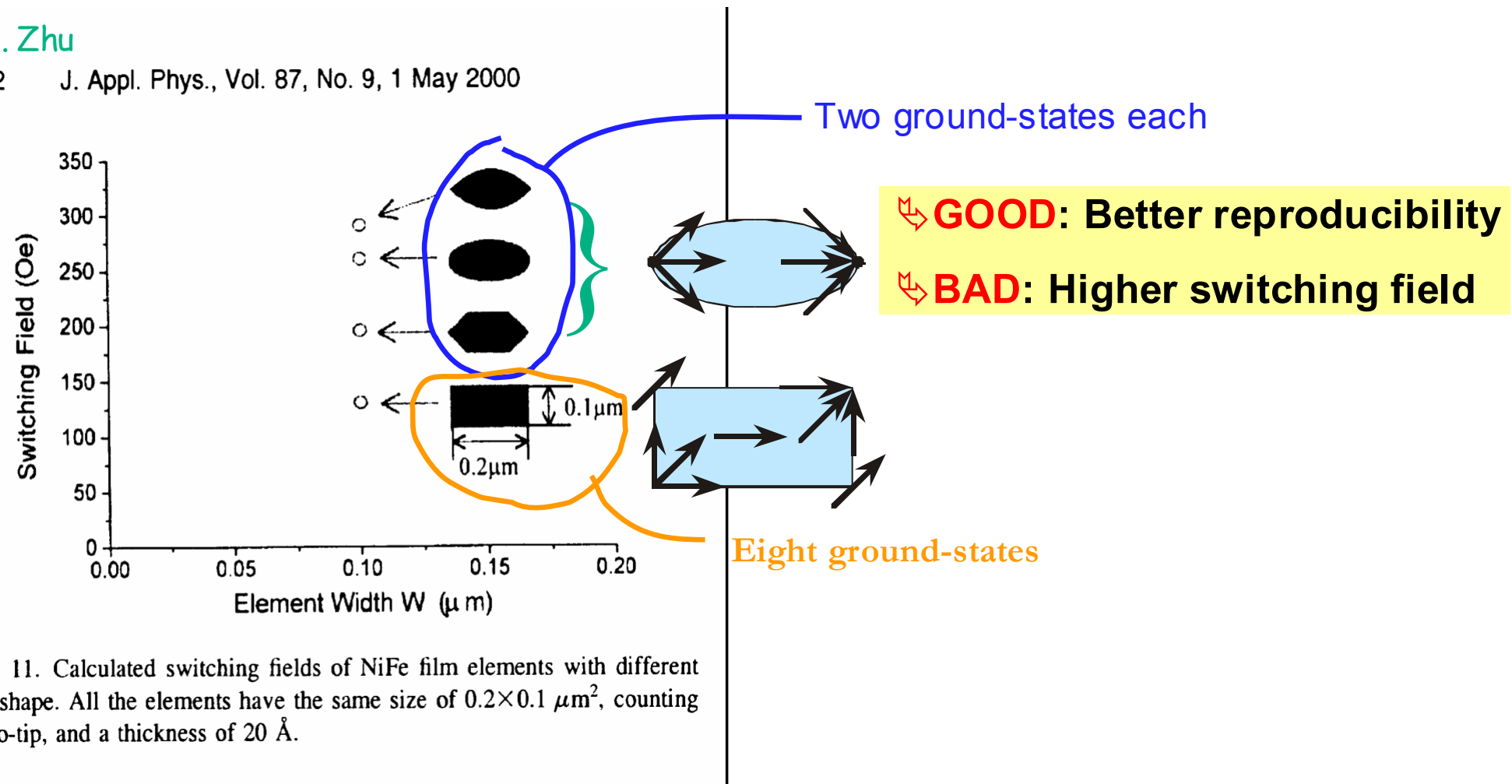
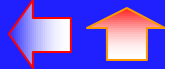


FIG. 11. Calculated switching fields of NiFe film elements with different end shape. All the elements have the same size of $0.2 \times 0.1 \mu\text{m}^2$, counting tip-to-tip, and a thickness of $20 \text{ \AA}$.

Essentially Equivalent Topological Properties



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3. Near-single domain: edge states, magnetization reversal

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Hypothesis

Van den Berg model

Infinitely soft material ($K=0$) $e_{mc} = 0$

2D geometry (neglect thickness)

Zero external magnetic field $e_z = 0$

Size $\gg$ all magnetic length scales (wall width)

$e_{ex} \longrightarrow 0$

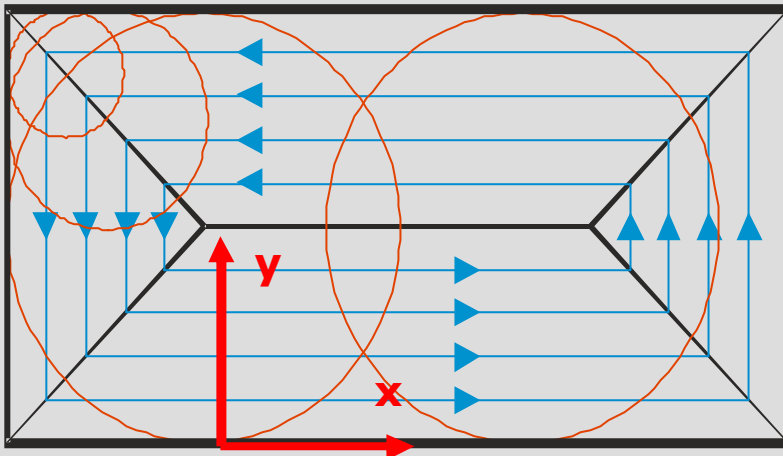
Solution

Looking for a solution with : $e_d = 0$

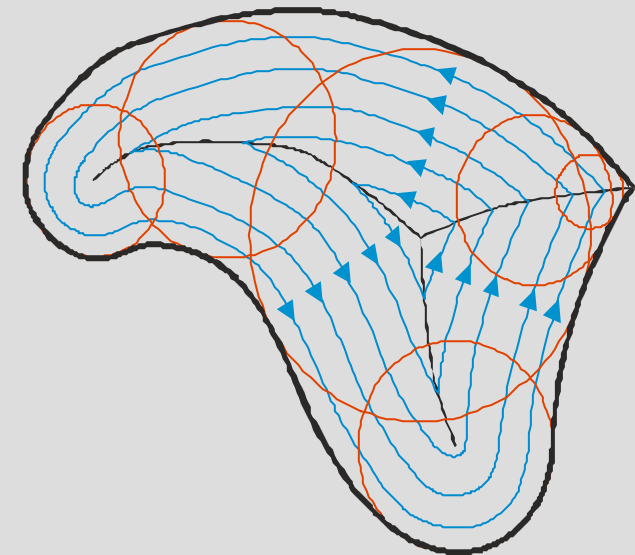
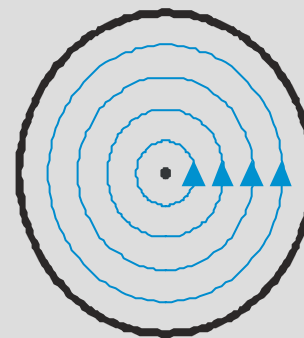
$-\text{div} \mathbf{M} = 0$ (no volume charges)

« Flux closure »

$\mathbf{M} \cdot \mathbf{n} = 0$ (no surface charges)



$$\text{div} \mathbf{M} = \frac{\partial M_x}{\partial x} + \frac{\partial M_y}{\partial y}$$

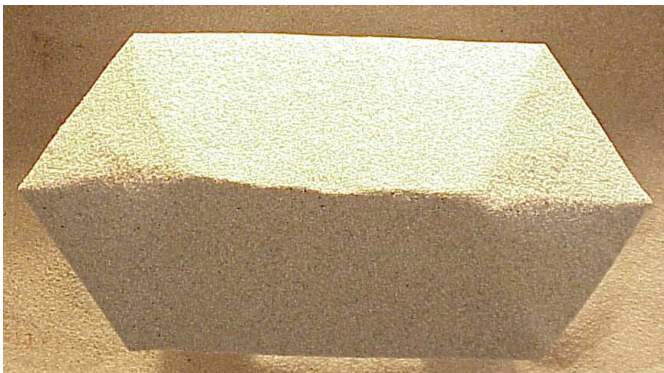
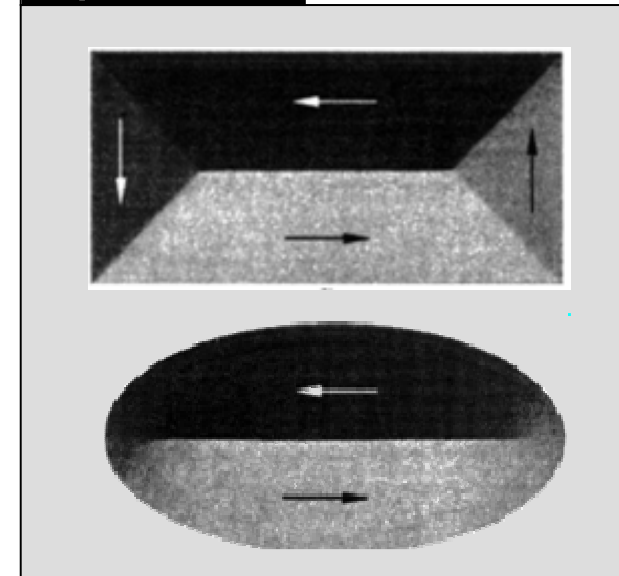


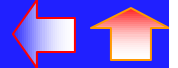
H. A. M. Van den Berg, *J. Magn. Magn. Mater.* 44, 207 (1984)

Sandpiles for simulating flux-closure patterns



Experiments





Generalization for non-zero field

The domains with magnetization parallel to the applied field are favored

P. Bryant et al., *Appl. Phys. Lett.* 54, 78 (1989)

See further extension to field arbitrarily-close to the saturation field:

A. DeSimone, R. V. Kohn, S. Müller, F. Otto & R. Schäfer, Two-dimensional modeling of soft ferromagnetic films, *Proc. Roy. Soc. Lond. A* 457, 2983-2991 (2001)

A. DeSimone, R. V. Kohn, S. Müller & F. Otto, A reduced theory for thin-film micromagnetics, *Comm. Pure Appl. Math.* 55, 1408-1460 (2002)

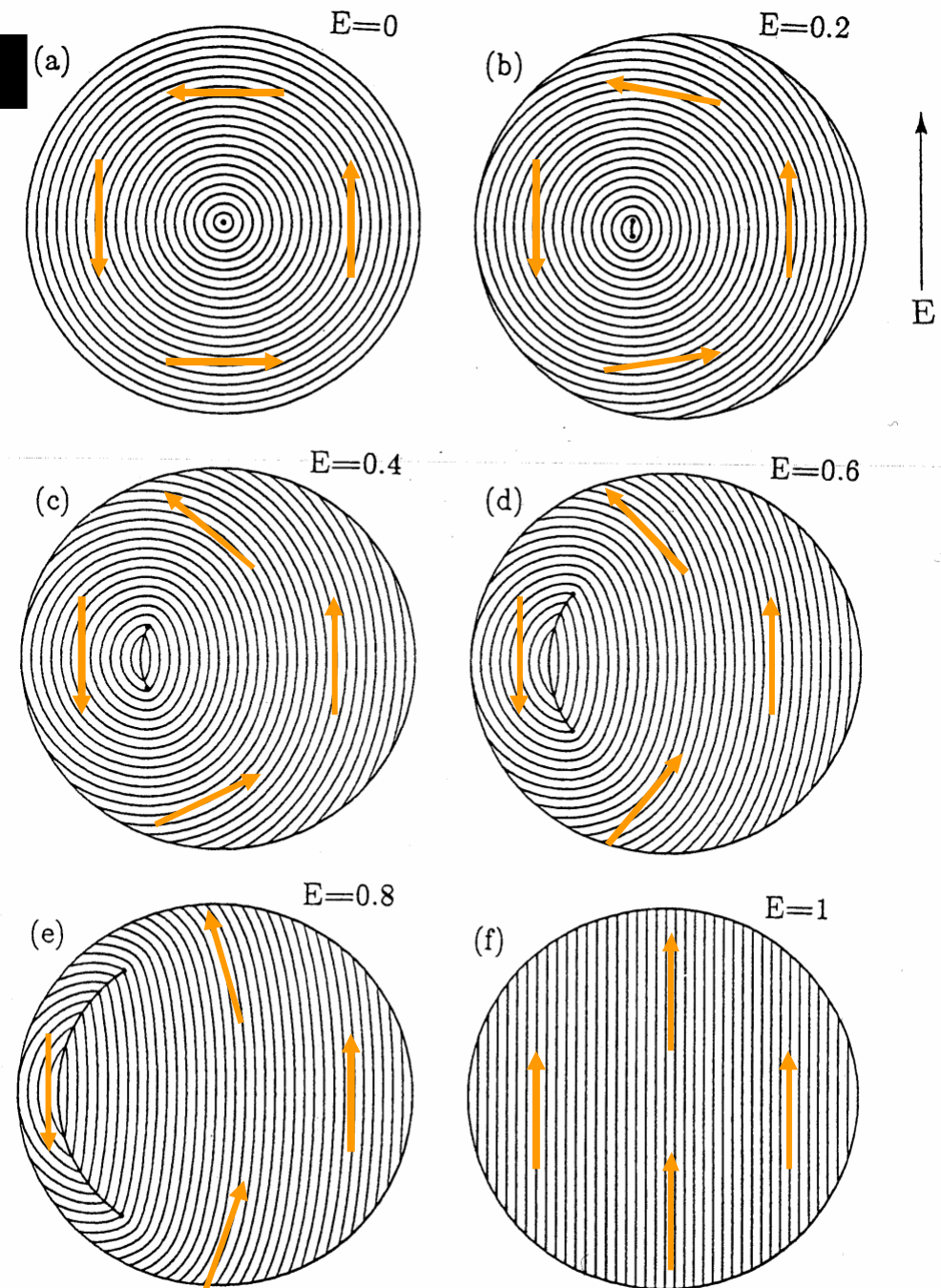
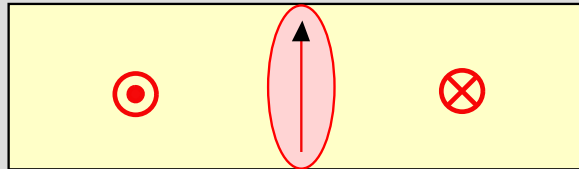


Figure 3

Bloch versus Néel wall

Crude model: wall is a uniformly-magnetized cylinder with an ellipsoid base

Bloch wall

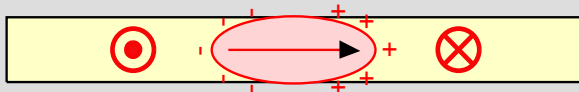


$$E_d = K_d \frac{W}{2t}$$

Thickness t

Wall width W

Néel wall

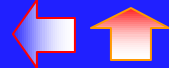


$$E_d = K_d \frac{t}{2W}$$

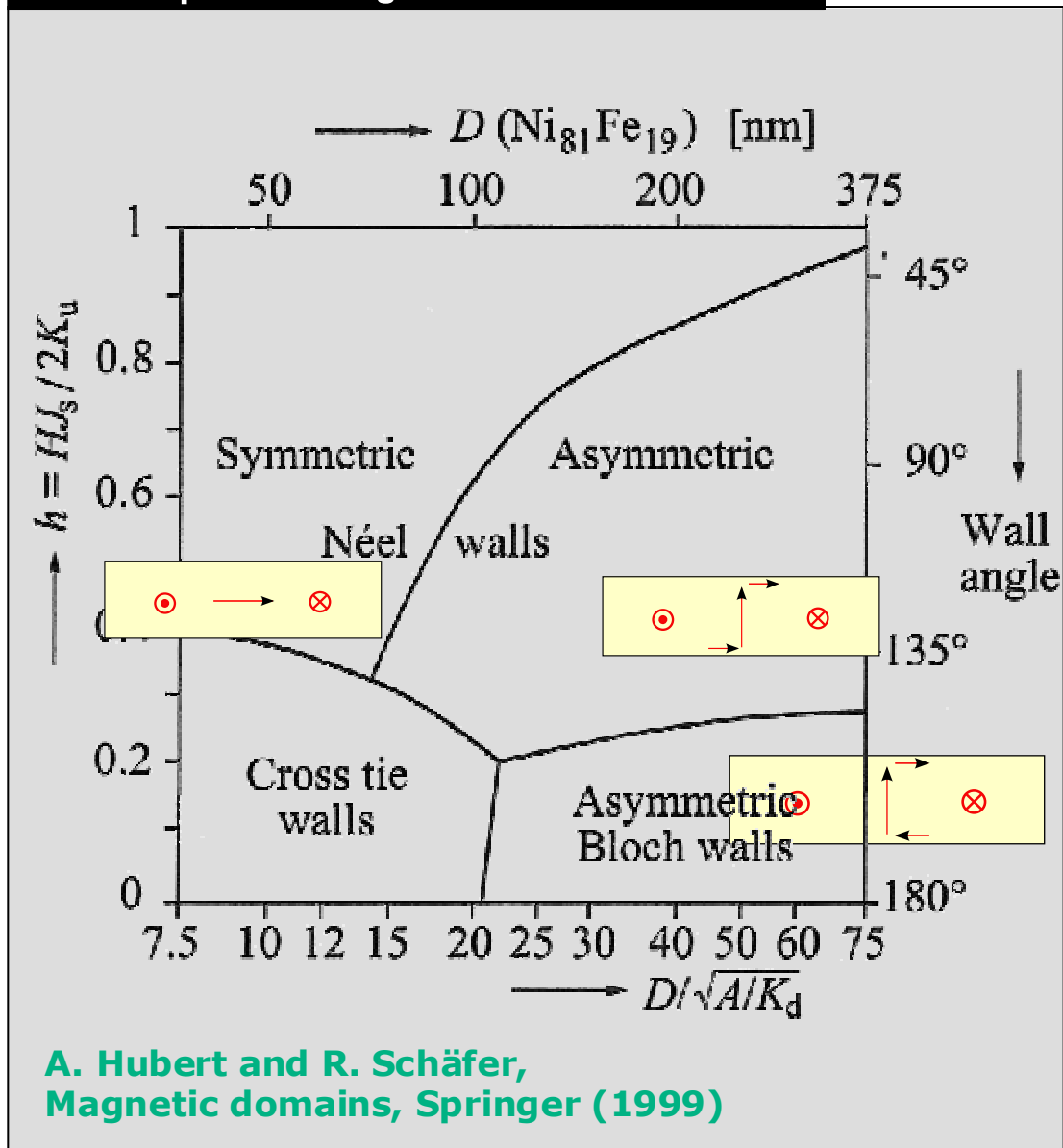
L. Néel, *Énergie des parois de Bloch dans les couches minces*,
C. R. Acad. Sci. 241, 533-536 (1955)

Conclusion

- At low thickness (roughly $t \approx W$) Bloch domain walls are expected to turn their magnetization in-plane > Néel wall
- Model needs to be refined
- Domain walls not changed for films with perpendicular magnetization



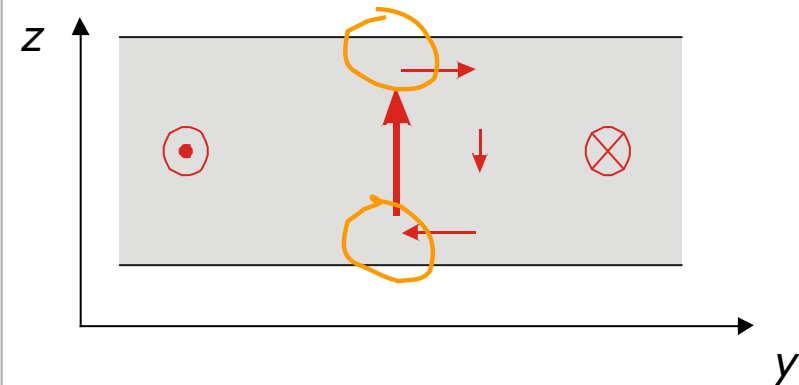
Refined phase diagram of domain walls



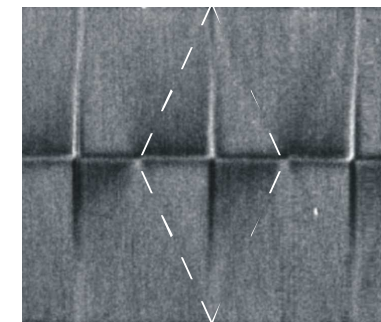
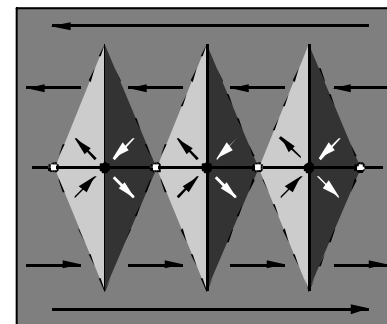
Néel caps occur atop Bloch walls to reduce surface and volume magnetic charges

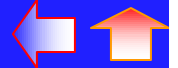
$$\mathbf{M} \cdot \mathbf{n} = 0$$

$$-\text{div} \mathbf{M} = -\frac{\partial M_x}{\partial x} - \frac{\partial M_y}{\partial y} - \frac{\partial M_z}{\partial z}$$

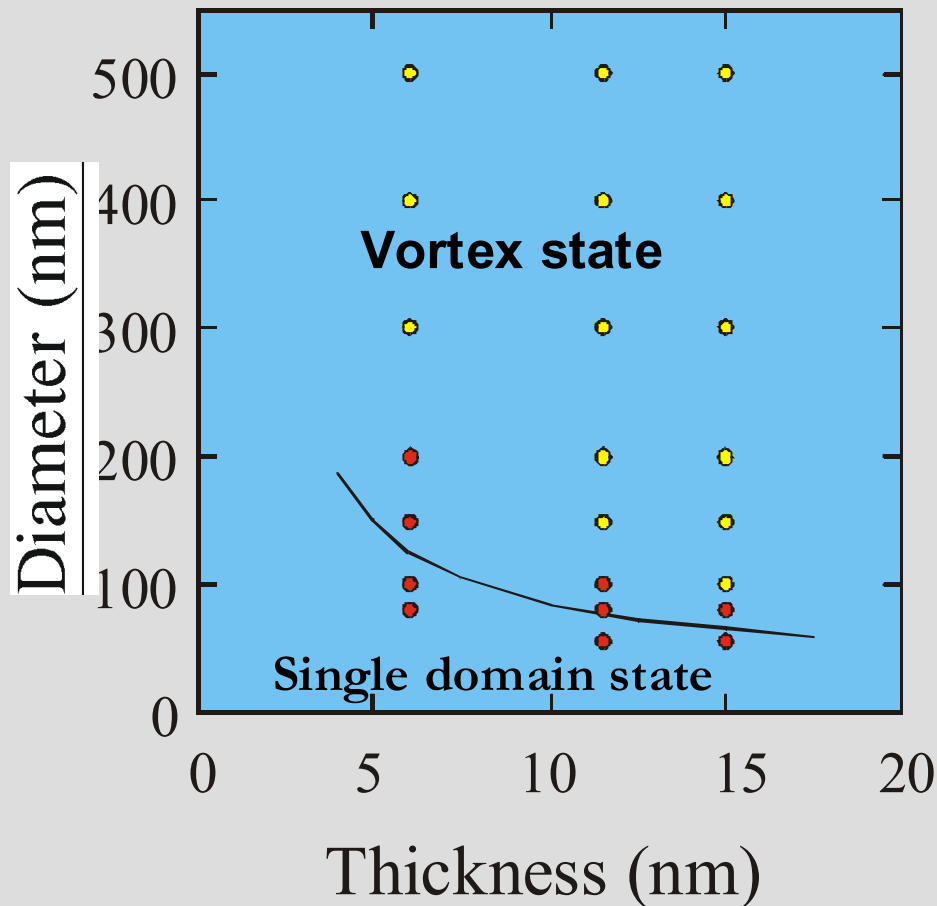


From Néel walls to cross-tie walls



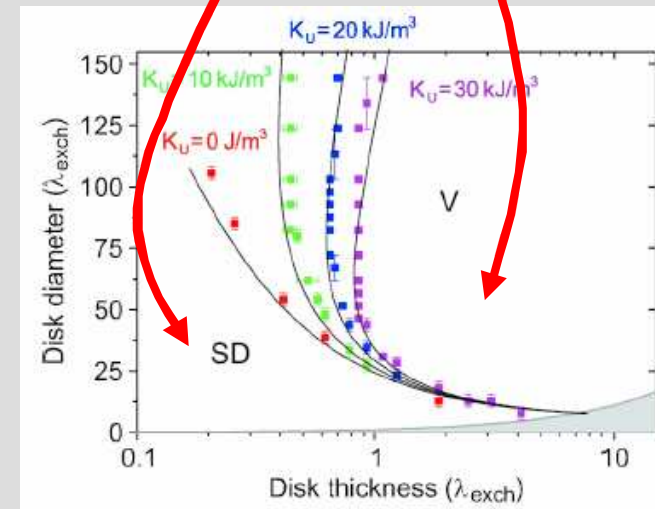
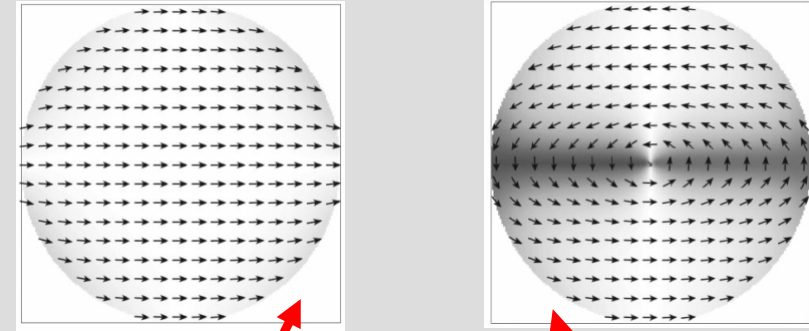


Experiments



R.P. Cowburn,
J.Phys.D:Appl.Phys.33, R1-R16 (2000)

Theory / Simulation



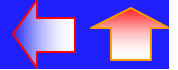
Zero-field
cross-over

$$t.D \approx 20 \lambda_{\text{ex}}^2$$

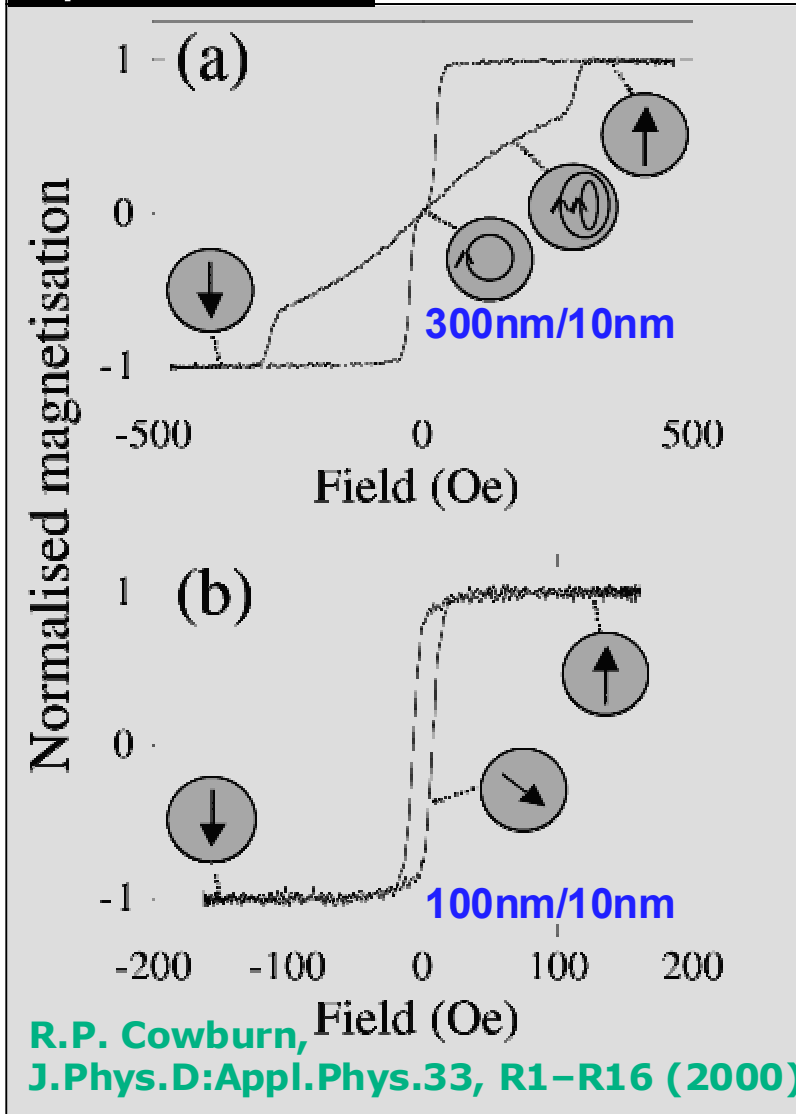


P.-O. Jubert & R. Allenspach,
PRB 70, 144402/1-5 (2004)

- ↪ Vortex state (flux-closure) dominates at large thickness and/or diameter
- ↪ The size limit for single-domain is much larger than the exchange length
- ↪ Experimentally the vortex may be difficult to reach close to the transition (hysteresis)

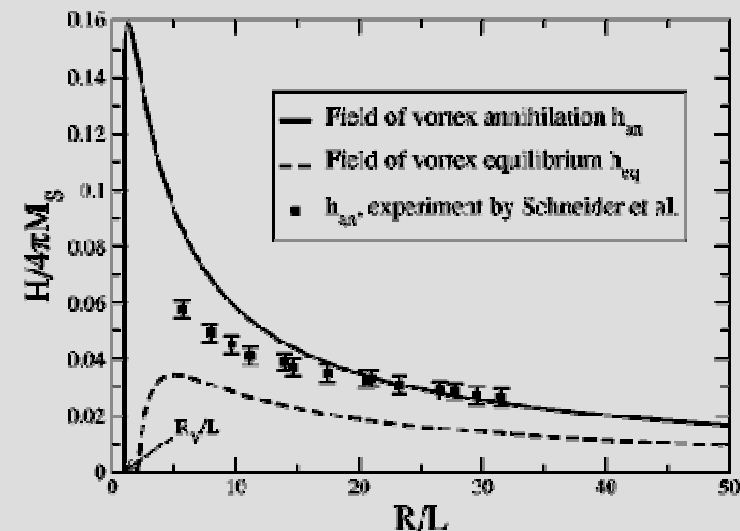
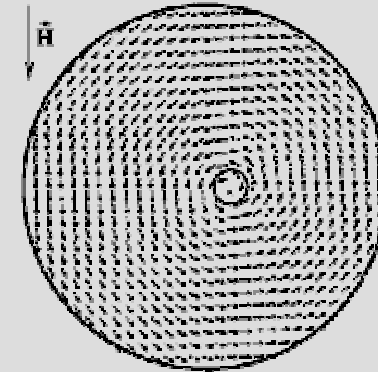


Experiments



Theory / Simulations

Displaced vortex model



Calculation of the equilibrium line and the annihilation line

K. Y. Guslienko & K. L. Metlov, PRB 63, 100403(R) (2001)

- Typical loops for flux-closure states
- Energy of the vortex state can be computed from the anhyseretic above-loop area.

Closure domains (flat)

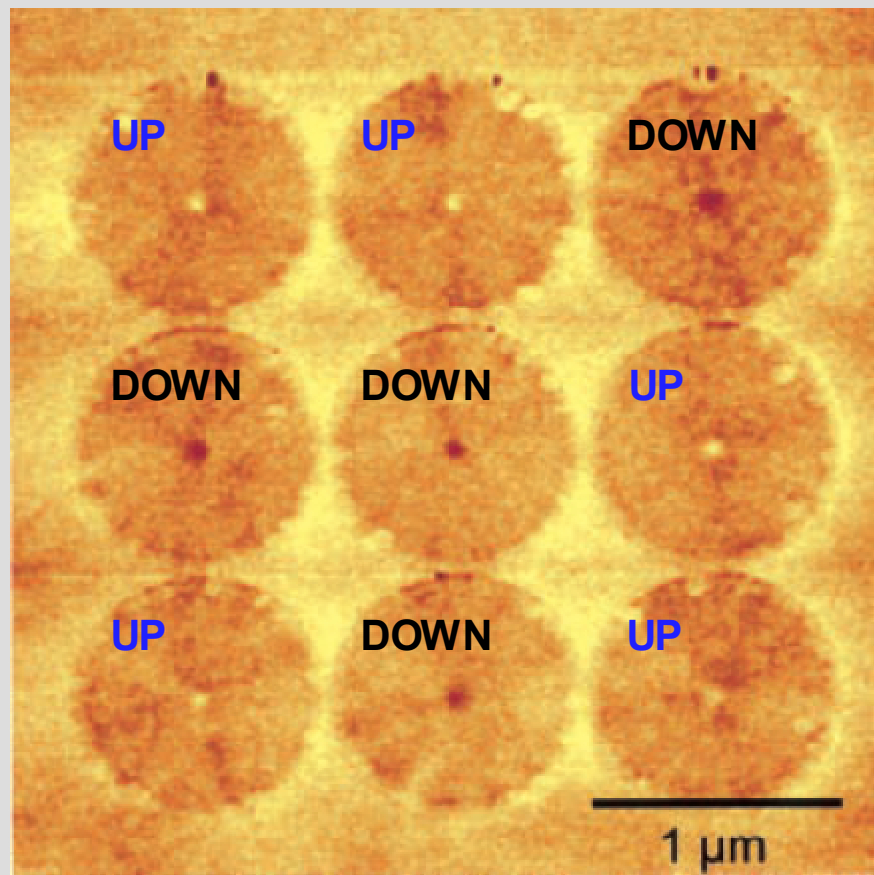


Fig. 2. MFM image of an array of permalloy dots 1 μm in diameter and 50 nm thick.

The central magnetic vortex can be magnetized up or down using a perpendicular field

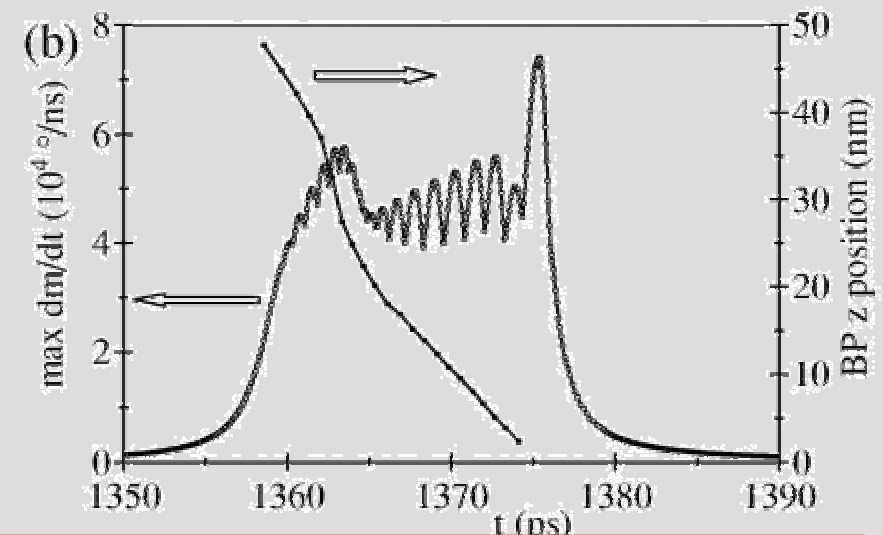
T. Shinjo et al., *Science* **289**, 930 (2000)

T. Okuno et al., *JMMM* **240**, 1 (2002)

Theory and simulation

Micromagnetic simulation

A. Thiaville et al., *Phys. Rev. B* **67**, 094410 (2003)



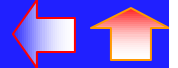
Requires a Bloch point:

**Not well described
in micromagnetism**



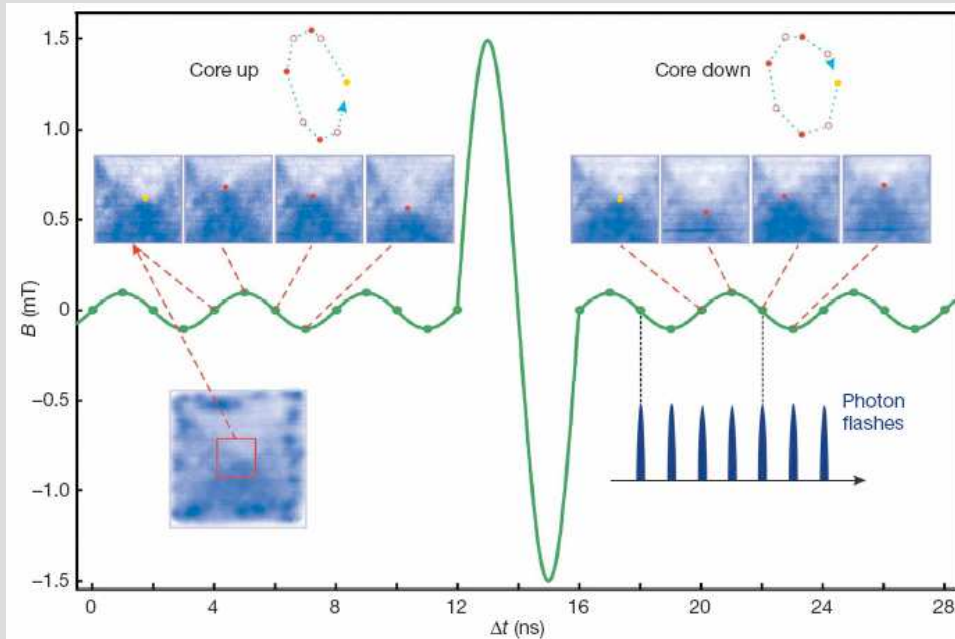
First theoretical insight in Bloch points

W. Döring, *J. Appl. Phys.* **39**, 1006 (1968)



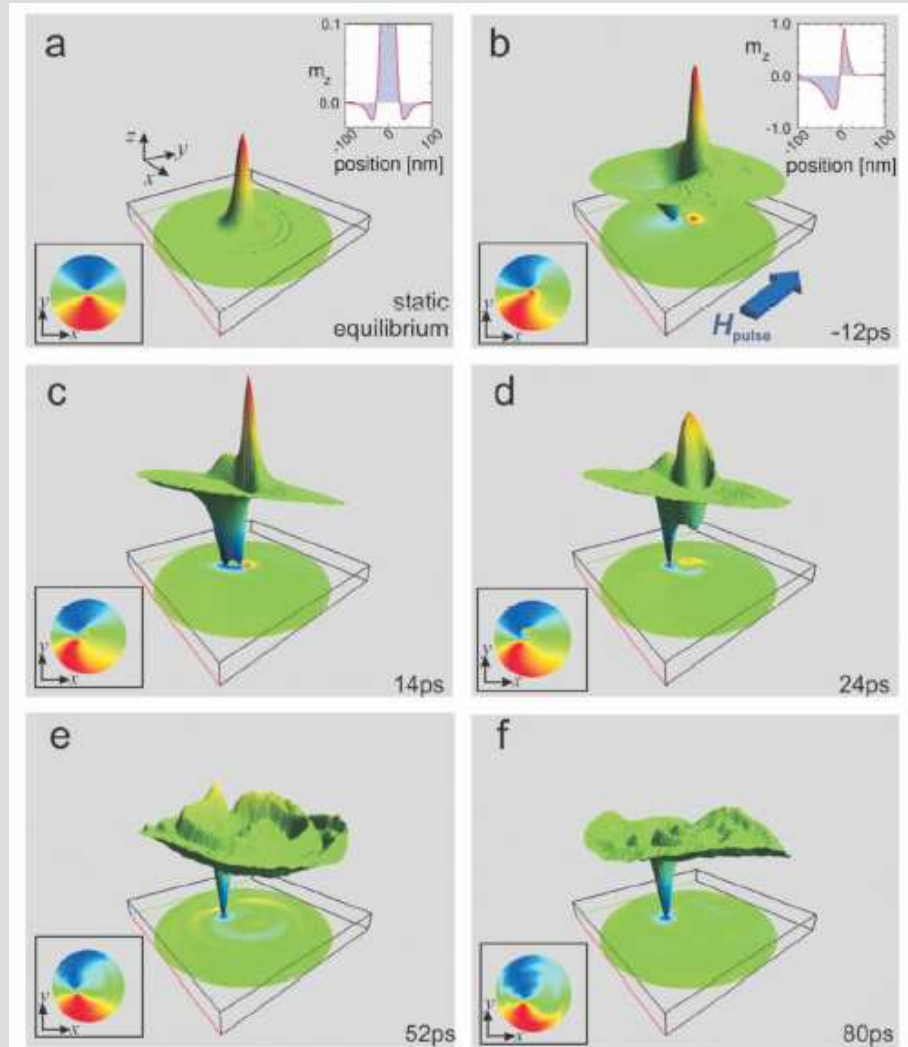
Magnetic vortex core reversal by excitation with short bursts of an alternating field

**B. Van Waeyenberg et al.,
Nature 444, 461 (2007)**

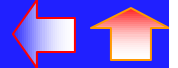


Resonant phenomenon

**R. Hertel et al.,
Phys. Rev. Lett. 98, 117201 (2007)**



Non-resonant phenomenon



0. Introduction

1. A word about dipolar energy

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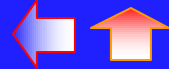
3. Near-single domain: edge states, magnetization reversal

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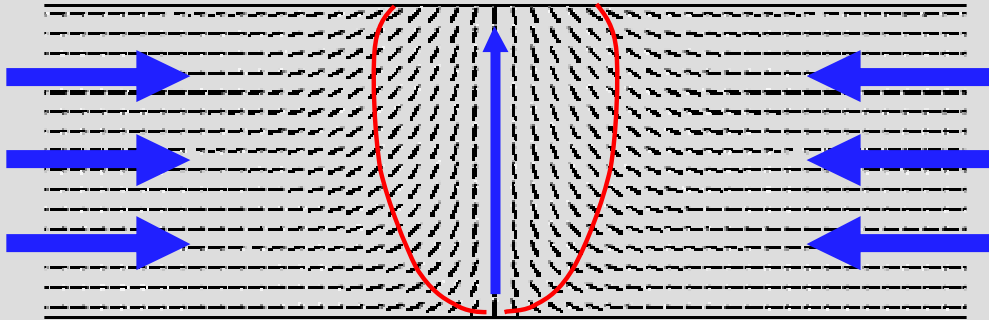
6. Summary on magnetic length scales

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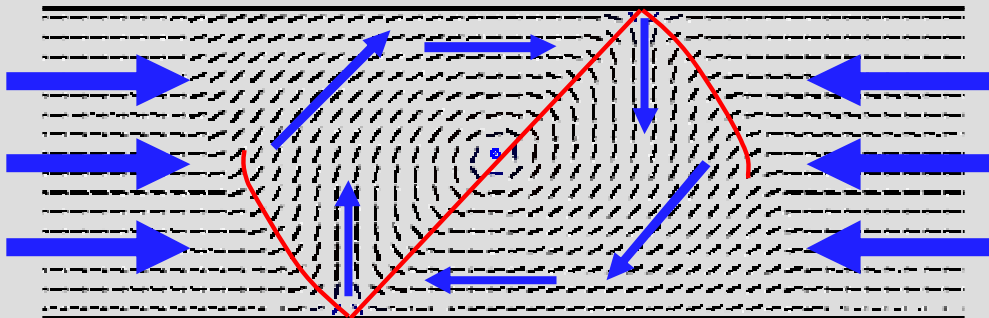


Transverse versus vortex wall

Thin and narrow stripes



Thick and large stripes



Transition for: $t.W \approx 75\lambda_{ex}^2$



R. McMichael & M. Donahue,
IEEE Trans. Mag. 33, 4167 (1997)

Handwavy argument

Energy of transverse wall:

Area x Demag. coeff.

$$\frac{t}{W} W^2 = tW$$

Energy of vortex

Constant to first approx.

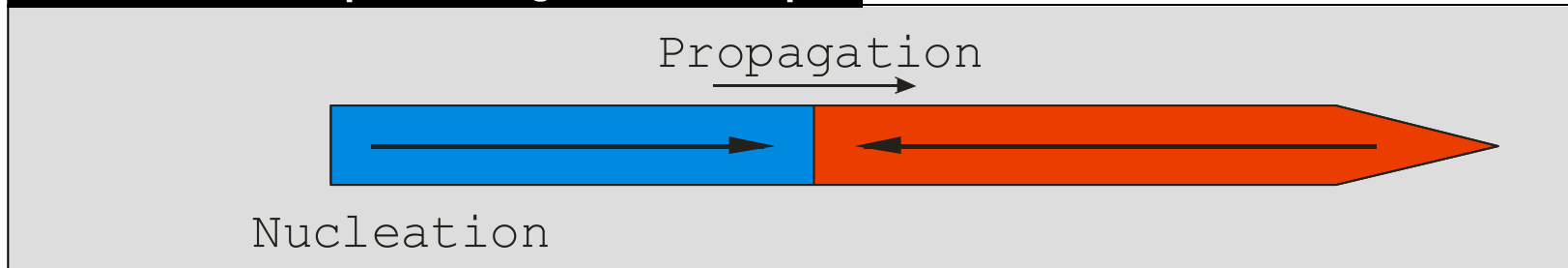
Cross-over for $t.W \approx Cte$

Refinement

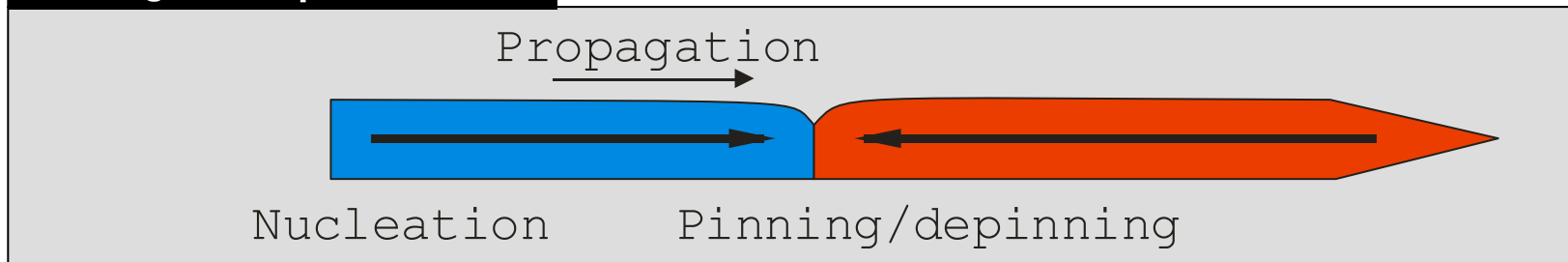
Precision, step size,
assymetric transverse wall

Y. Nakatani, A. Thiaville & J. Miltat,
J. Magn. Magn. Mater. 290-291, 750 (2005)

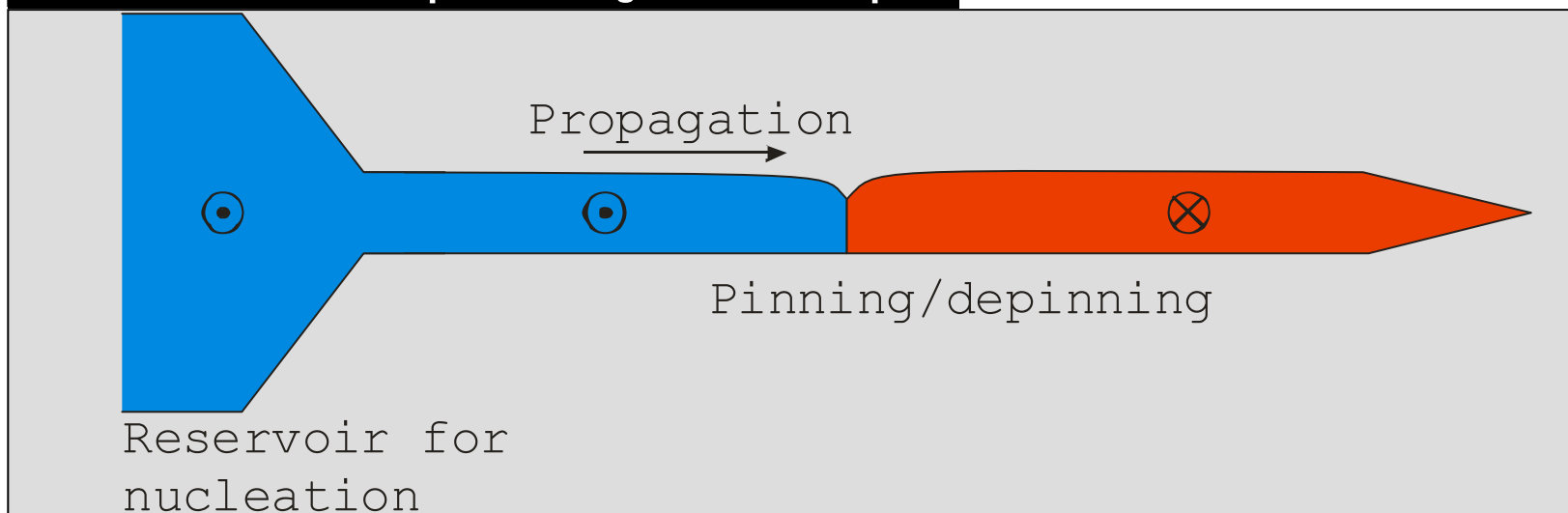
Nucleation in in-plane magnetized stripes



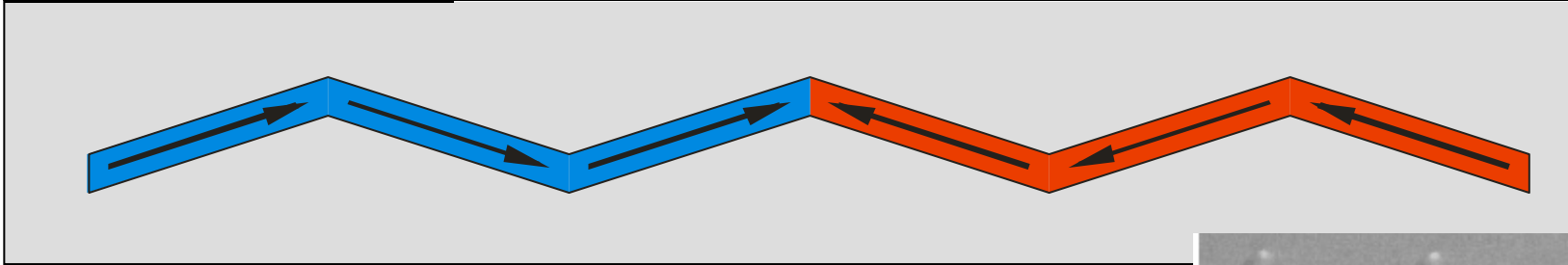
Pinning in stripes: notches



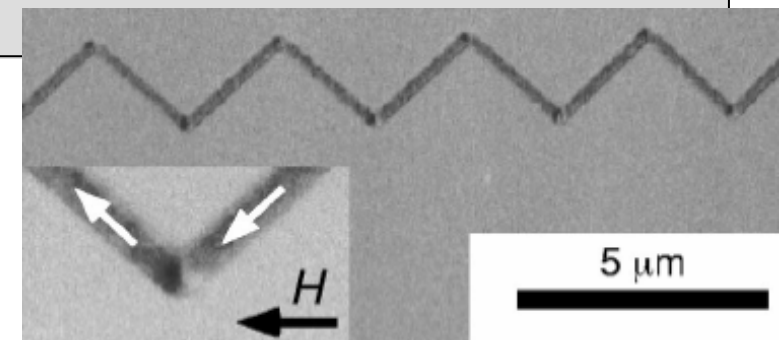
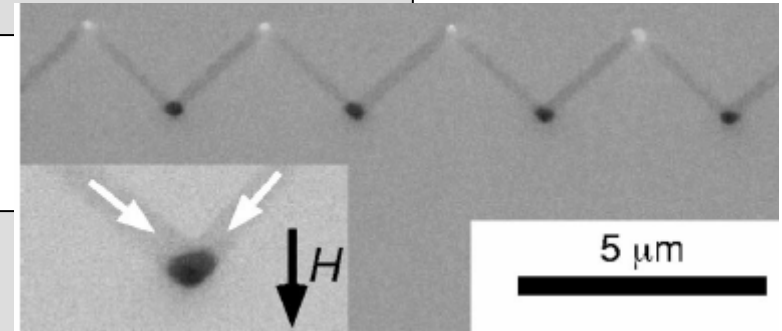
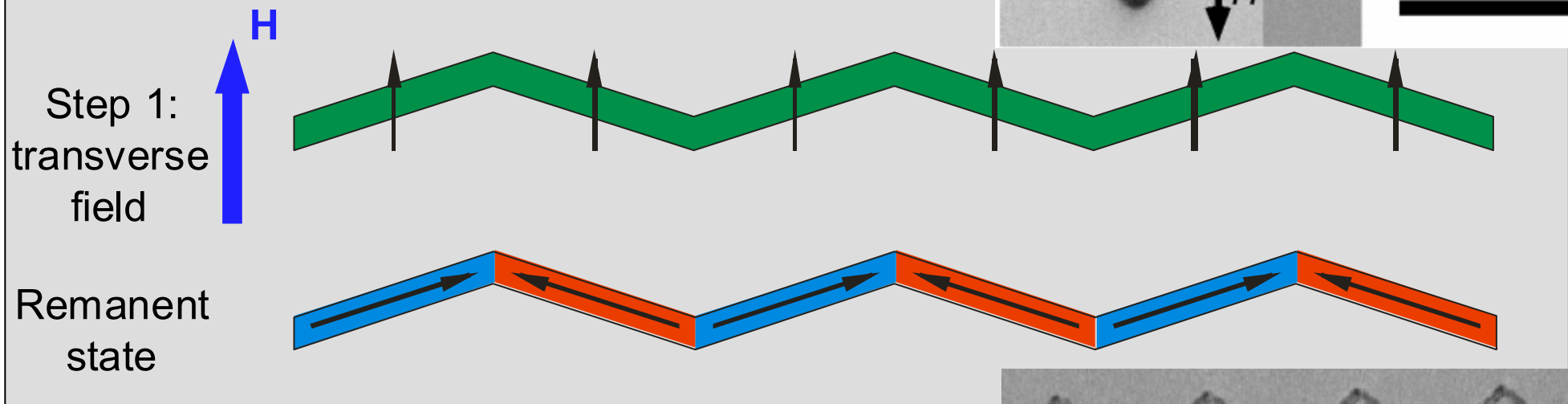
Nucleation in out-of-plane magnetized stripes



Geometrical pinning

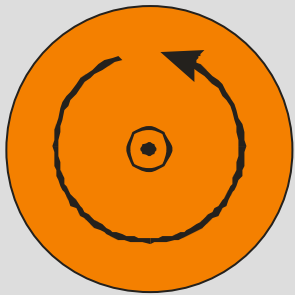


Preparation for in-plane anisotropy

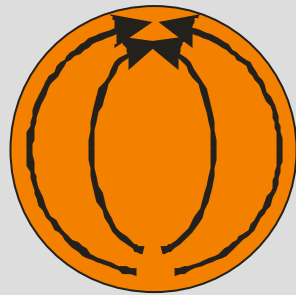


T. Taniyama et al., APL76, 613 (2000)

Disks



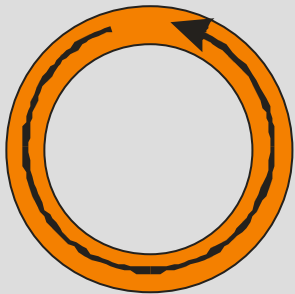
Vortex state



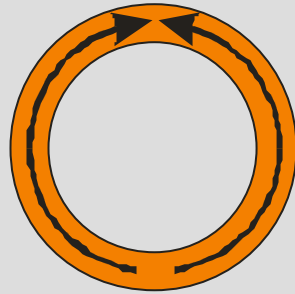
Near single-domain
(leaf state)

← Large thickness t
Large diameter D

Rings



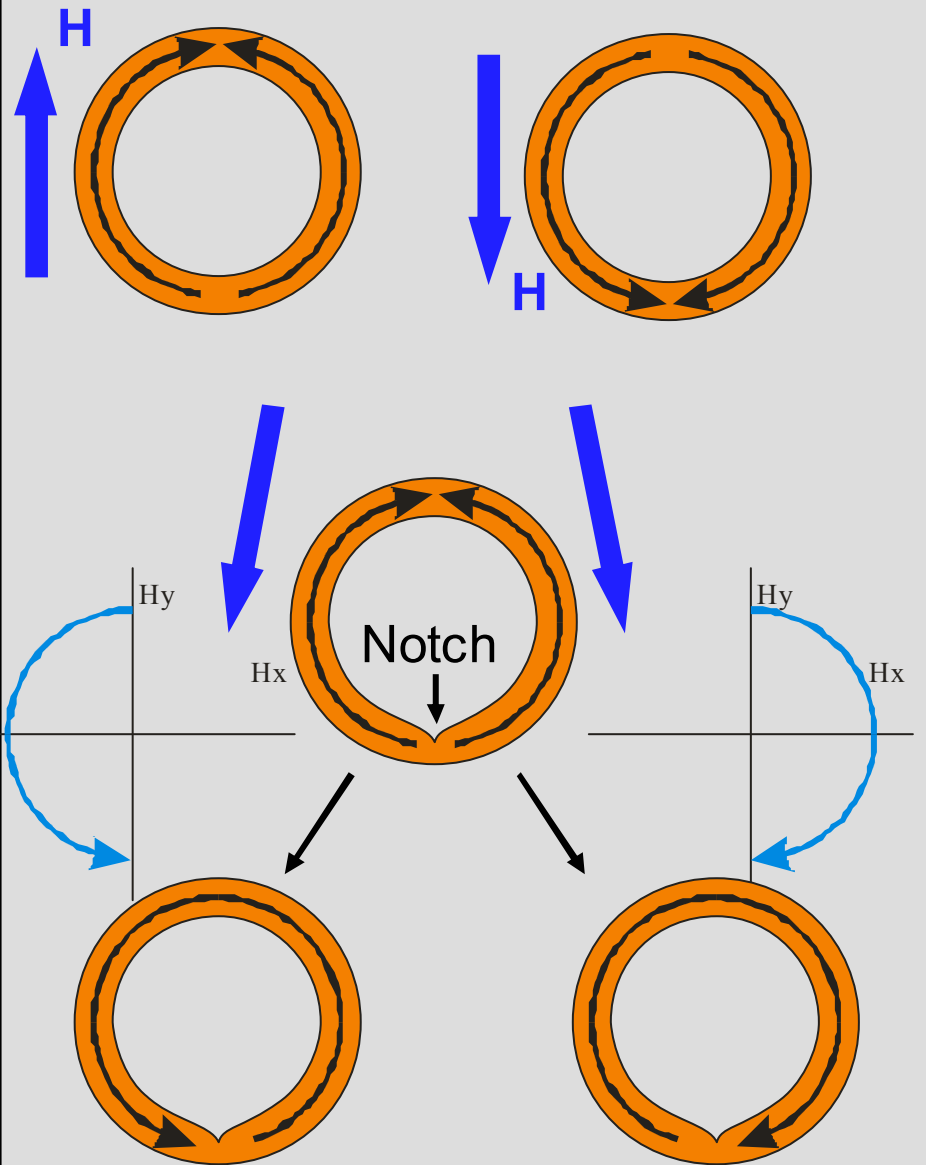
Vortex state



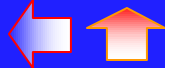
Onion state

Stability less dependent on geometry
(no vortex energy)

Control of ring states



Ex: M. Kläui et al., APL78, 3268 (2001)



0. Introduction

1. A word about dipolar energy

2. Single-domain: Stoner-Wohlfarth, superparamagnetism

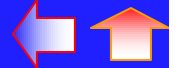
3. Near-single domain: edge states, magnetization reversal

4. Flux-closure domains and vortices

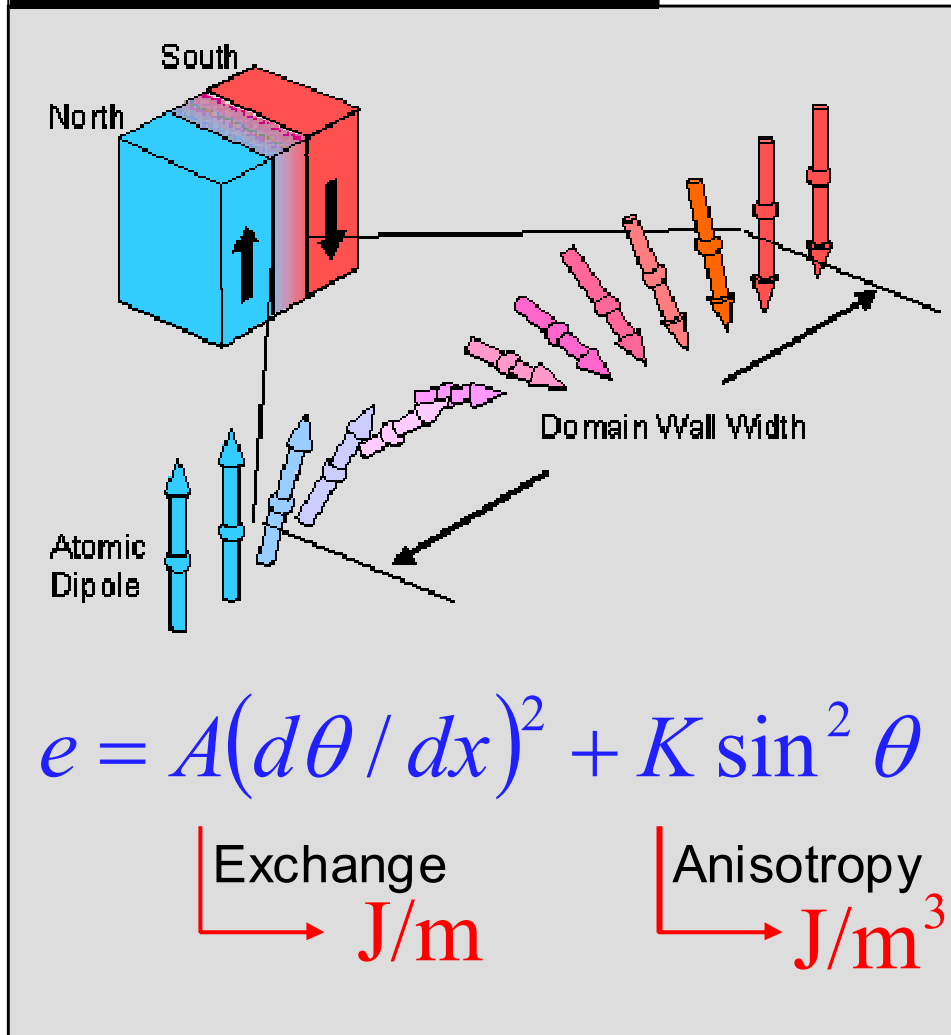
5. Domain walls in stripes

6. Summary on magnetic length scales

7. Inter-objects dipolar interactions



Typical length scale:
Bloch wall width λ_B



Numerical values

$$\Lambda = \sqrt{A/K} \quad \text{Bloch wall parameter}$$

$$\lambda_B = \pi \sqrt{A/K} \quad \text{Bloch wall width}$$

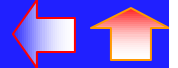
$$\lambda_B = 2 - 3 \text{ nm} \longrightarrow \lambda_B \geq 100 \text{ nm}$$

Hard

Soft



There are several other definitions are used for measuring the width of walls, implying 2 or other prefactor



Typical length scale:

Exchange length λ_{ex}

$$e = A(d\theta/dx)^2 + K_d \sin^2 \theta$$

$$\begin{array}{|l} \text{Exchange} \\ \text{J/m} \end{array} \quad \begin{array}{|l} \text{Dipolar energy} \\ \text{J/m}^3 \end{array}$$

$$\begin{aligned} \lambda_{\text{ex}} &= \sqrt{A/K_d} \\ &= \sqrt{2A/\mu_0 M_s^2} \end{aligned}$$

$$\lambda_{\text{ex}} = 3 - 10 \text{ nm}$$

Critical size relevant for nanoparticles made of soft magnetic material: vortex etc.

$$D_c \approx \pi \sqrt{3} \lambda_{\text{ex}}$$

Generalization for various shapes

$$D_c \approx \pi \sqrt{6A/(N\mu_0)M_s^2}$$

Critical size for hard magnets

$$D_c \approx 6E_w / K_d \approx 2.5Q\lambda_B$$

$$E_w \approx 4\sqrt{AK} \text{ for hard magnetic materials}$$

Quality factor Q

$$e = -K \sin^2 \theta + K_d \sin^2 \theta$$

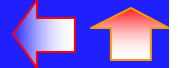
$$\begin{array}{|l} \text{m.c.} \\ \text{J/m} \end{array} \quad \begin{array}{|l} \text{Dipolar energy} \\ \text{J/m}^3 \end{array}$$

$$Q = K / K_d$$

Relevant e.g. for stripe domains in thin films with perpendicular magnetocrystalline anisotropy

Notice:

Other length scales: with field etc.



0. Introduction

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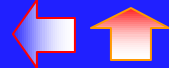
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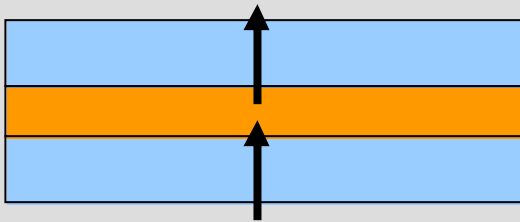


Stacked dots : dipolar

In-plane magnetization



Out-of-plane magnetization



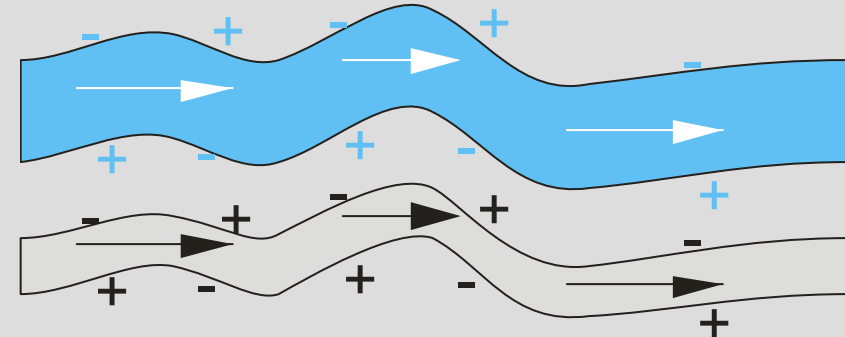
Hint:

An upper bound for the dipolar coupling is the self demagnetizing field

Notice: similar situation as for RKKY coupling

Stacked dots : orange-peel coupling

In-plane magnetization



Always parallel coupling

L. Néel, C. R. Acad. Sci. 255, 1676 (1962)

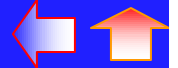
(valid only for thick films)

**J. C. S. Kools et al.,
J. Appl. Phys. 85, 4466 (1999)**
(valid for any film)

Out-of-plane magnetization

May be parallel or antiparallel

J. Moritz et al., Europhys. Lett. 65, 123 (2004)



Models for arrays of single-domain planar rectangular dots

E. Y. Tsymbal, Theory of magnetostatic coupling in thin-film rectangular magnetic elements, Appl. Phys. Lett. 77, 2740 (2000)

R. Álvarez-Sánchez et al., Analytical model for shape anisotropy in thin-film nanostructured arrays: Interaction effects, J. Magn. Magn. Mater. 307, 171-177 (2006)

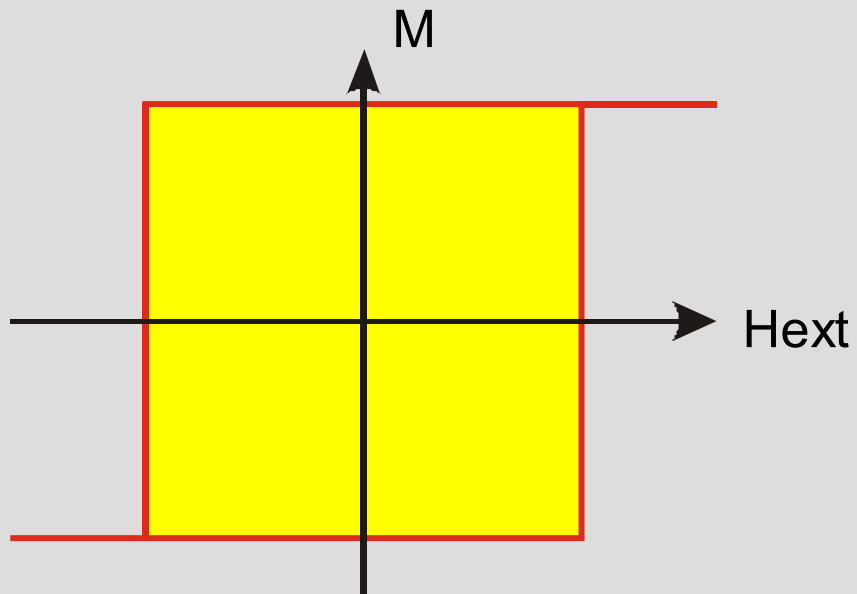
Models for arrays of elements of arbitrary shapes

M. Beleggia and M. De Graef, On the computation of the demagnetization tensor field for an arbitrary particle shape using a Fourier space approach, J. Magn. Magn. Mater. 263, L1-9 (2003)

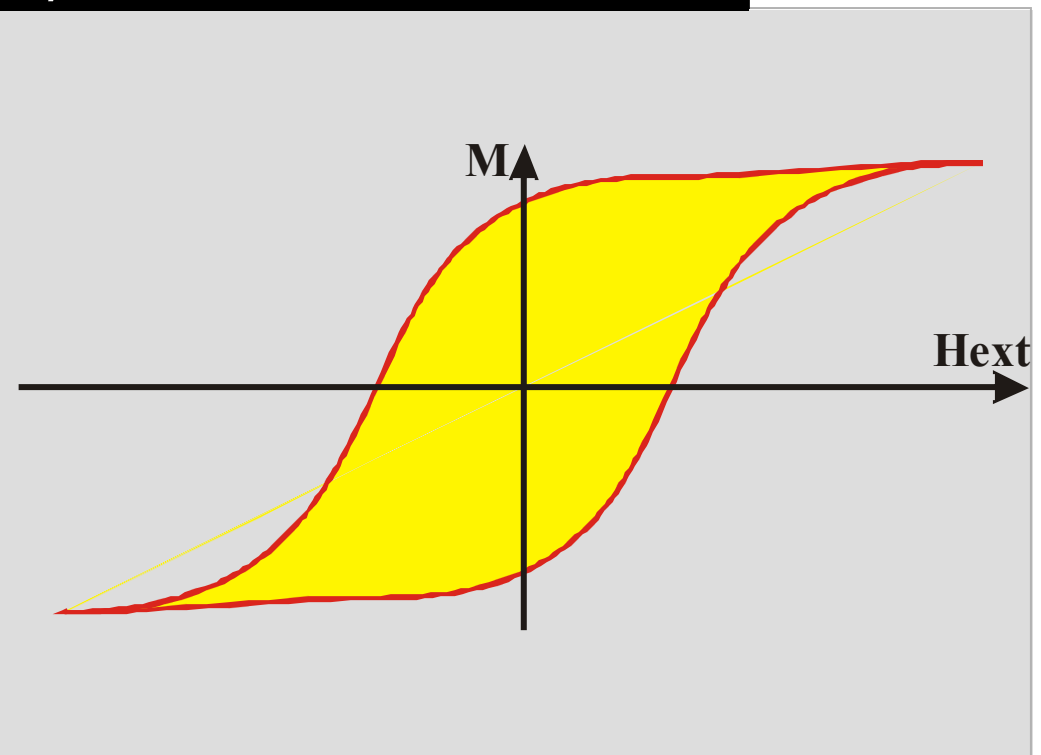
E.Y. Vedmedenko, N. Mikuszeit, H. P. Oepen and R. Wiesendanger, Multipolar Ordering and Magnetization Reversal in Two-Dimensional Nanomagnet Arrays, Phys. Rev. Lett. 95, 207202 (2005)

N. Mikuszeit, E. Y. Vedmedenko & H. P. Oepen, Multipole interaction of polarized single-domain particles, J. Phys. Condens. Matter 16, 9037-9045 (2005)

Expected hysteresis loop for macrospins

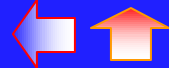


Hysteresis for assemblies of dots

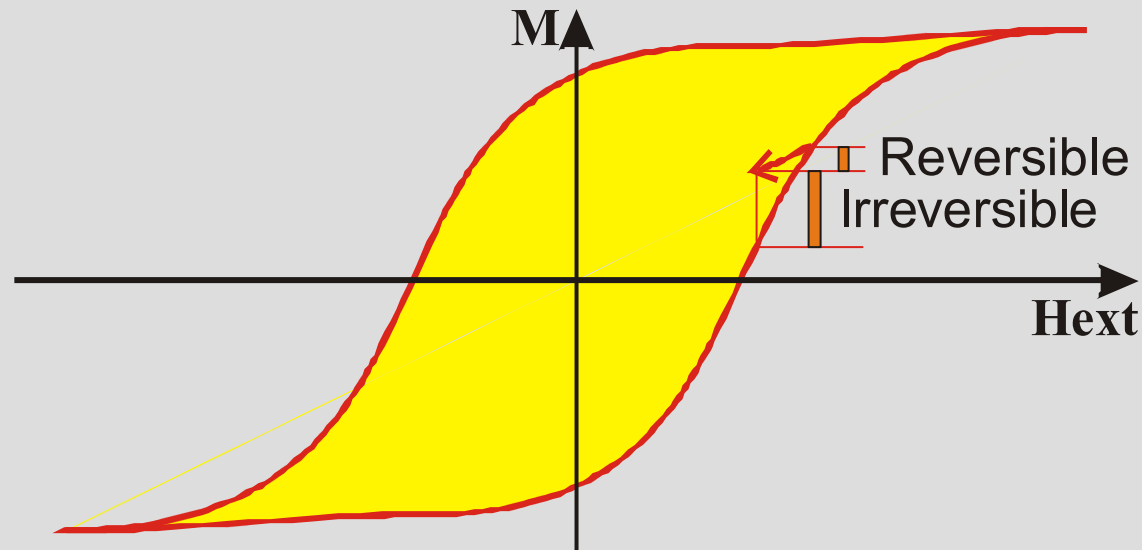


Possible effects

- Distribution of coercive fields
- (Dipolar) interactions



Distribution of properties

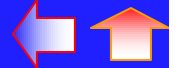


$$\rho(H_r) = \left. \frac{dm}{dH} \right|_{\text{irreversible}}$$

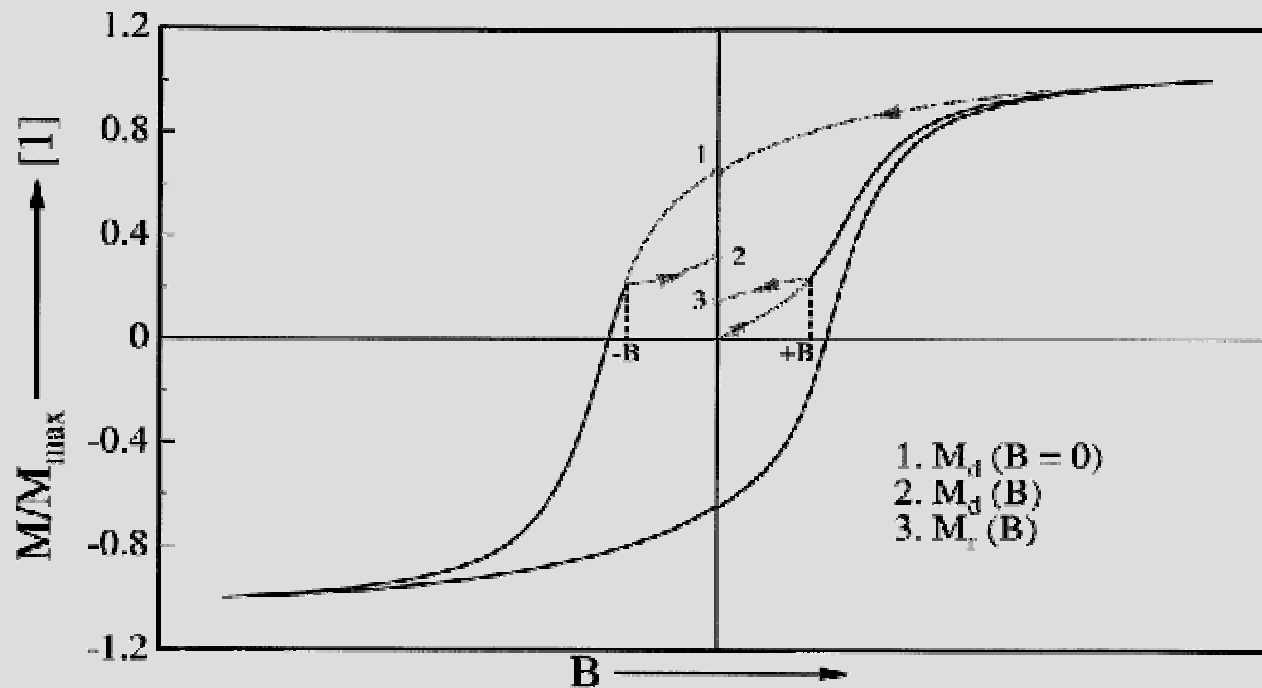
$H_c(T)$ for a given population of the distribution can be studied at a given stage of the reversal (10%, 20% etc.)

Example (among many others): O. Fruchart et al., Phys. Rev. B 57, 2596-2606 (1998)

**Effect of distributions and dipolar interactions
are sometimes difficult to disentangle**



Henkel plots



O. Henkel,
Phys. Stat. Sol. 7, 919 (1964)

S. Thamm et al.,
JMMM184, 245 (1998)

Fig. 1. Explanation of how to measure the two different remanent magnetisations M_r and M_d .

Measure of dipolar interactions

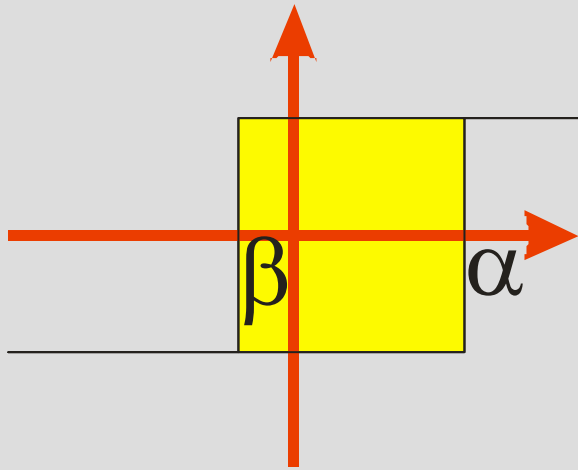
$$\Delta M_H(x) = M_d(x) - [1 - 2M_r(x)]$$

- Long experiments (ac demagnetization)
- Better physical meaning than Preisach

Preisach model

G. Biorci et al., *Il Nuov. Cim. VII*, 829 (1958)

I. D. Mayergoyz, *Mathematical models of hysteresis*, Springer (1991)

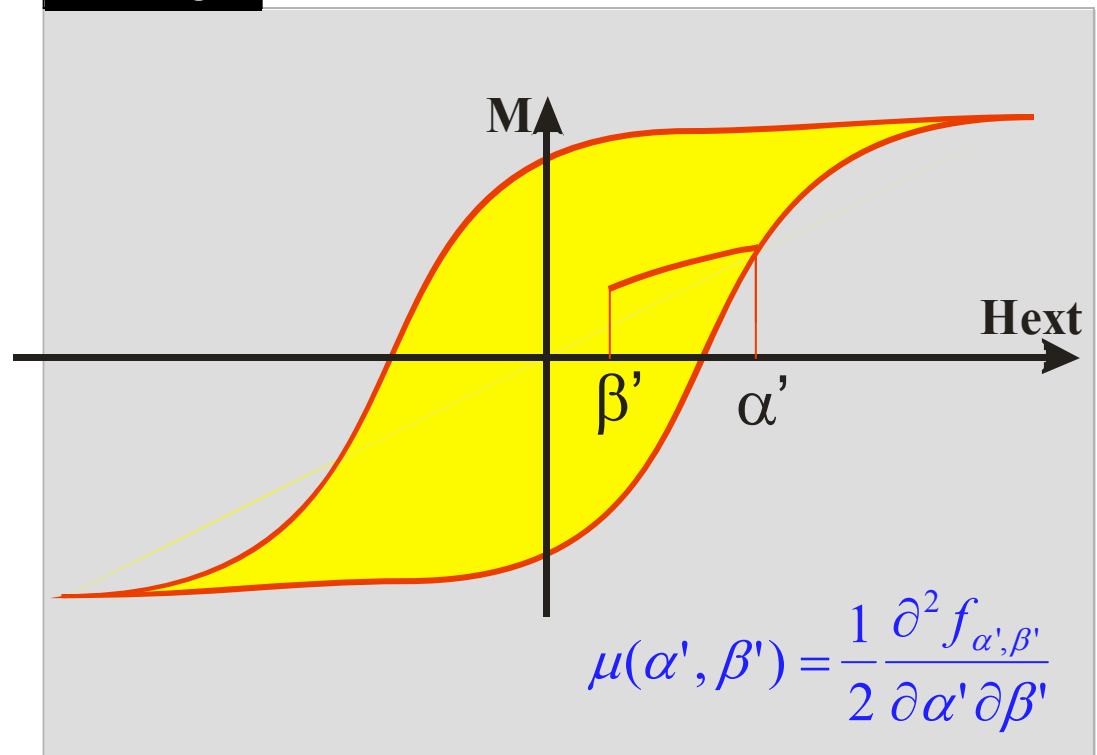


↪ Distribution function

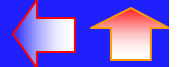
$\mu(\alpha, \beta)$ with $\alpha > \beta$

↪ No true link between real particles and μ

Solving



- Time-consuming experiments (1D set of hysteresis curves)
- Better suited to bulk materials with strong interactions



Not covered in this lecture

Dimensional effects

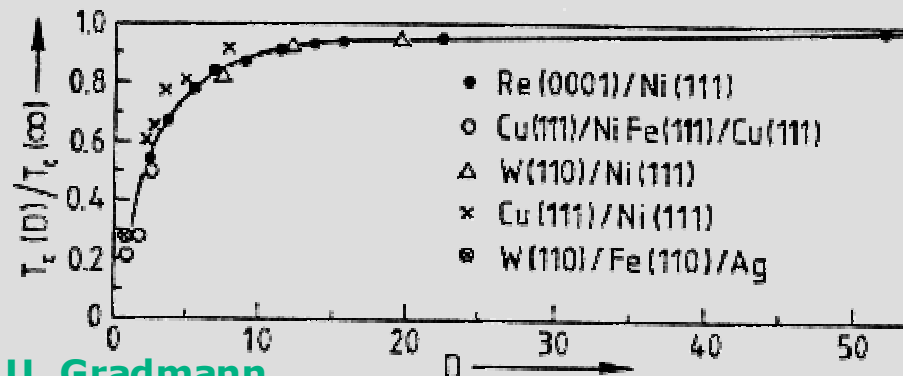
Not covered in this lecture

Relevant length scale: inter-atomic distance, Fermi wavelength etc. $\approx 1\text{nm}$

Mostly relevant for thin films or self-organized nanostructures at surfaces

Effect on magnetization at interfaces

- ⇒ Change of ground-state interface M_s due to hybridization (often an increase)
- ⇒ Enhanced decay of magnetization due to a lower mean number of neighbors



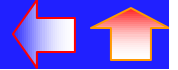
U. Gradmann,
Handbook of Magn. Mater. Vol.7, ch.1 (1993)

U. Gradmann, Handbook of Magn. Mater. Vol.7, ch.1 (1993)

Interface magnetic anisotropy

- ⇒ Origin: breaking of symmetry at interfaces
L. Néel, J. Phys. Radium 15, 15 (1954)
- ⇒ Phenomenology: often a $1/t$ dependence of the density of anisotropy
W. A. Jesser et al., Phys. Stat. Sol. 19, 95 (1967)
C. Chappert and P. Bruno., JAP64, 5736 (1988)
- ⇒ Consequence: possibility of films with perpendicular magnetization
U. Gradmann and J. Müller,
Phys. Status Solidi 27, 313 (1968)

See OF lecture: ESM 2003, Brasov, Romania



- [1] **Magnetic domains**, A. Hubert, R. Schäfer, Springer (1999)
- [2] J.I. Martin et coll., **Ordered magnetic nanostructures: fabrication and properties**, J. Magn. Magn. Mater. **256**, 449-501 (2003).
- [3] R. Skomski, **Nanomagnetics**, J. Phys.: Cond. Mat. **15**, R841–896 (2003).
- [4] O. Fruchart, A. Thiaville, **Magnetism in reduced dimensions**, C. R. Physique **6**, 921 (2005) [Topical issue, Spintronics].
- [5] O. Fruchart, **Couches minces et nanostructures magnétiques**, Techniques de l'Ingénieur, E2 150/E2 151.
- [6] G. Chaboussant, **Nanostructures magnétiques**, Techniques de l'Ingénieur, revue 10-9 (RE51) (2005)
- [7] Lecture notes from undergraduate lectures, plus various slides:
<http://perso.neel.cnrs.fr/olivier.fruchart>
 * European School on Magnetism 2003: **low-dimensional magnetism**
 * European School on Magnetism 2007: **magnetization reversal, basics and nanostructures**

