

# Voyage au pays du Nanomagnétisme



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<http://neel.cnrs.fr>

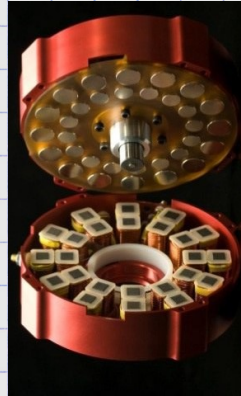


## Modern applications of magnetism

Where does 'nano' contribute ?

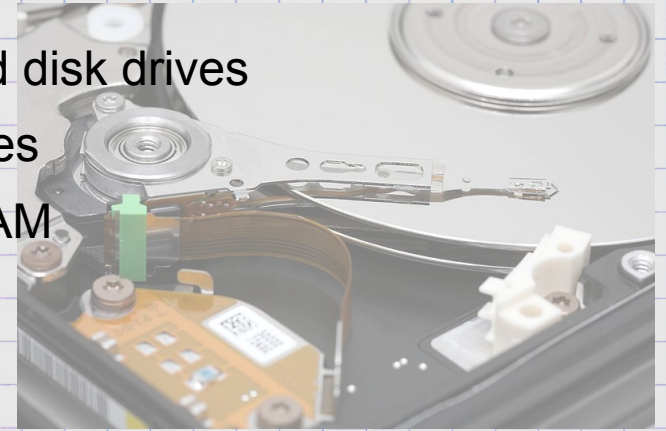
### Materials

- ⇒ Magnets  
(→ motors and generators)
- ⇒ Transformers
- ⇒ Magnetocaloric



### Data storage

- ⇒ Hard disk drives
- ⇒ Tapes
- ⇒ MRAM



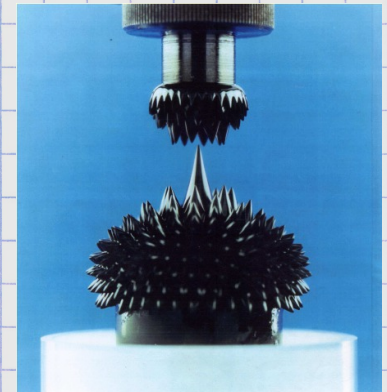
### Sensors

- ⇒ Compass
- ⇒ Field mapping
- ⇒ HDD read heads

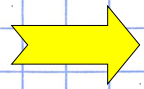


### Nanoparticles

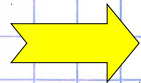
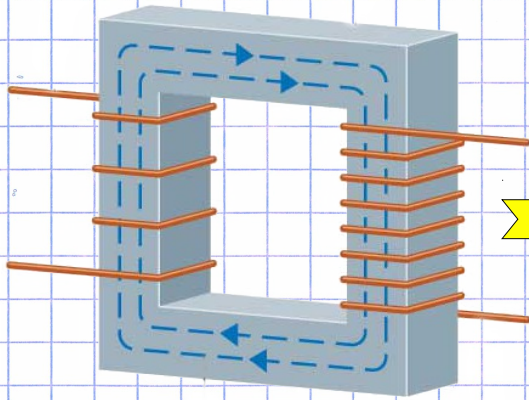
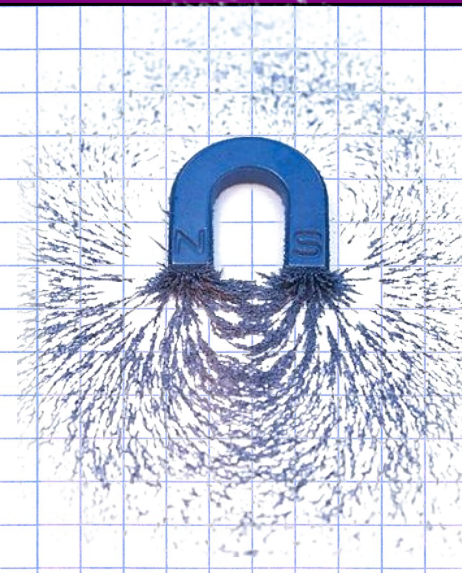
- ⇒ Ferrofluids
- ⇒ MRI contrast
- ⇒ Hyperthermia
- ⇒ Sorting & tagging



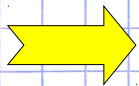
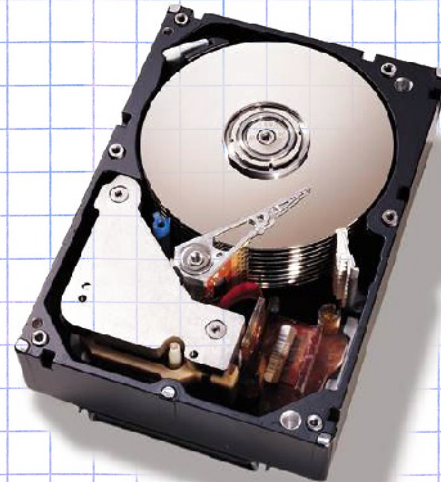




## 1. Fields, moments, materials



## 2. Magnetization processes



## 3. Low dimensions

Maxwell equation :  $\nabla \times \mathbf{B} = \mu_0 \mathbf{j}$

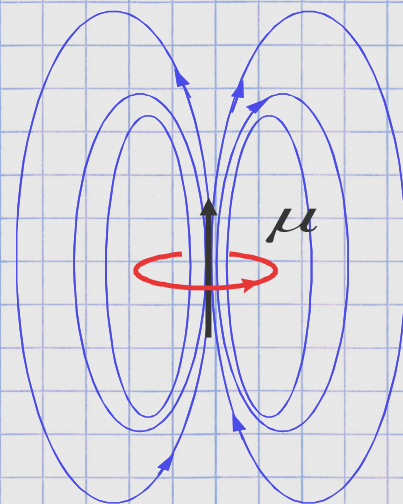
Electric currents produce magnetic fields

## Oersted field



$$B_\theta = \frac{\mu_0 I}{2\pi r}$$

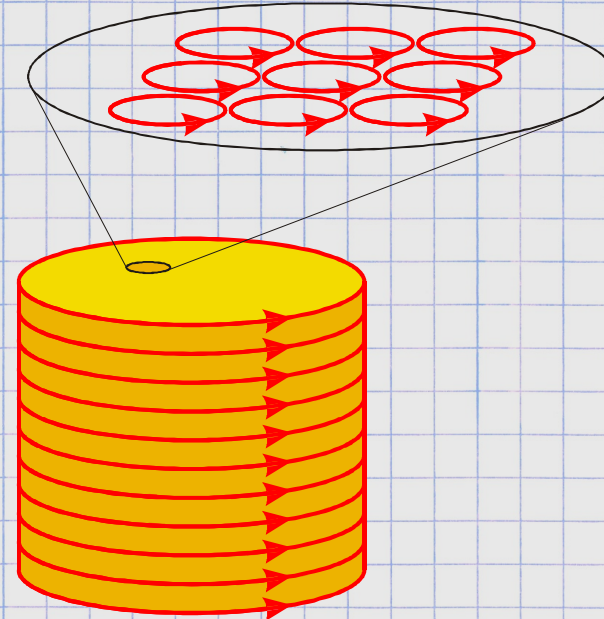
## Magnetic dipole



$$\mathbf{B} = \frac{\mu_0}{4\pi r^3} \times \left[ \frac{3}{r^2} (\boldsymbol{\mu} \cdot \mathbf{r}) \mathbf{r} - \boldsymbol{\mu} \right]$$

Magnetic dipole  $\text{A.m}^2$

## Magnetic material



Magnetization  $\text{A/m}$

Magnetic moment  $\text{A.m}^2$

$$\mathbf{B} = \mu_0 (\mathbf{H} + \mathbf{M})$$

Induction  $\mathbf{B}$ , Magnetic field  $\mathbf{H}$ , Magnetization  $\mathbf{M}$

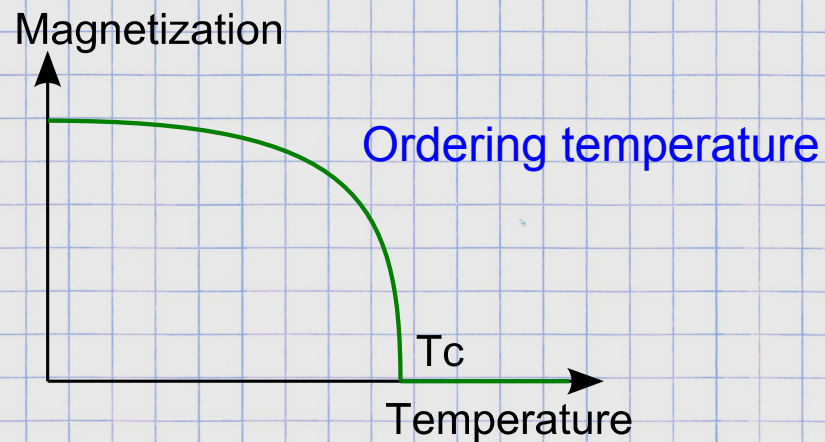




## Magnetic ordering

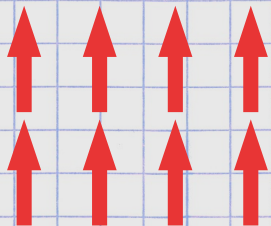
Magnetic exchange  
between microscopic moments

$$\mathcal{E} = -2 \sum_{i>j} J_{i,j} \mathbf{S}_i \cdot \mathbf{S}_j$$



### Ferromagnet

$$J_{i,j} > 0$$



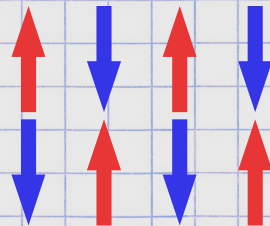
→ Fe

$$T_c = 1043 \text{ K}$$

$$M_s = 1.73 \times 10^6 \text{ A/m}$$

### Antiferromagnet

$$J_{i,j} < 0$$



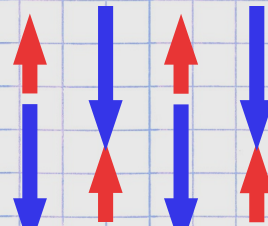
→ CoO

$$T_N = 292 \text{ K}$$

$$J = 3/2$$

### Ferrimagnet

$$J_{i,j} < 0$$



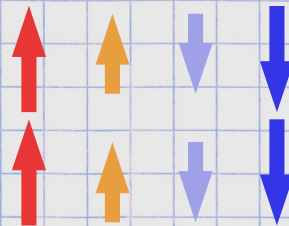
→ Fe<sub>3</sub>O<sub>4</sub>

$$T_c = 858 \text{ K}$$

$$M_s = 480 \text{ kA/m}$$

### Helical

$$J_1, J_2 \dots$$



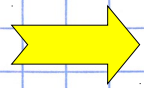
→ Dy

$$T \in 85 - 179 \text{ K}$$

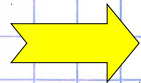
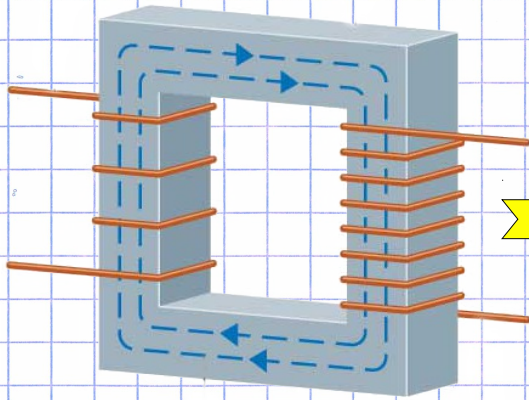
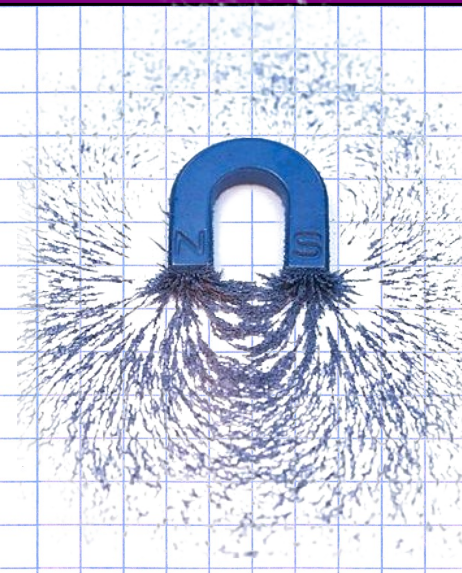
$$\mu = 10.4 \mu_B$$



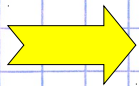
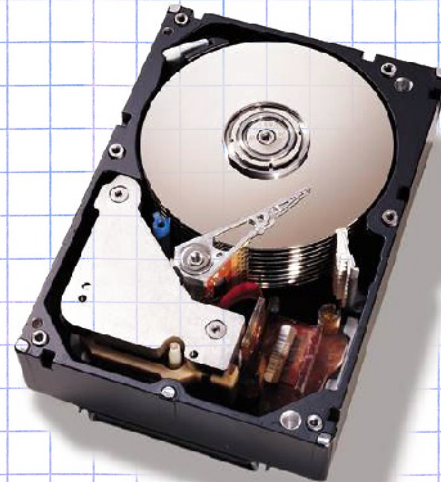




## 1. Fields, moments, materials



## 2. Magnetization processes



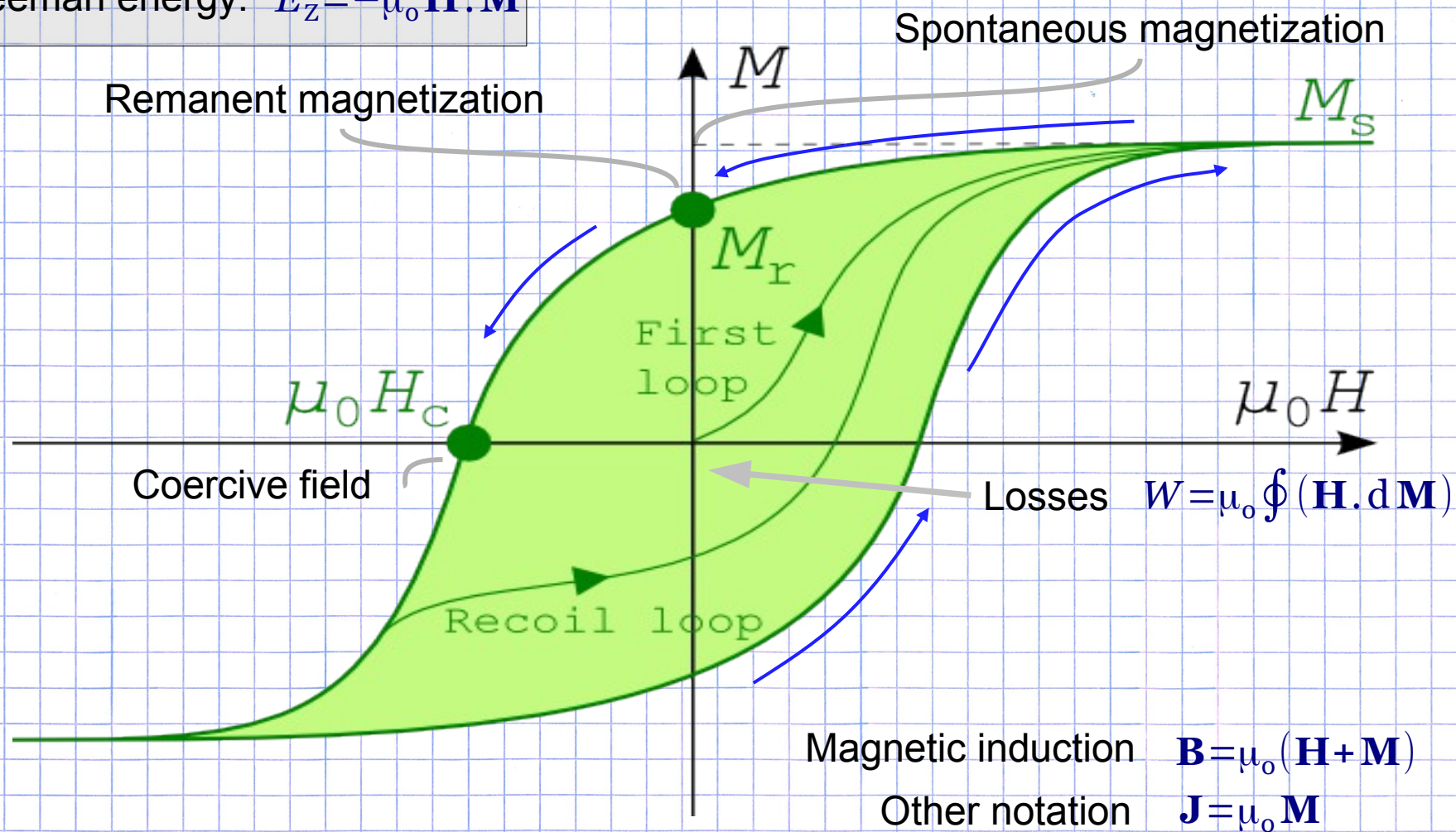
## 3. Low dimensions



Manipulation of magnetic materials:

→ Application of a magnetic field

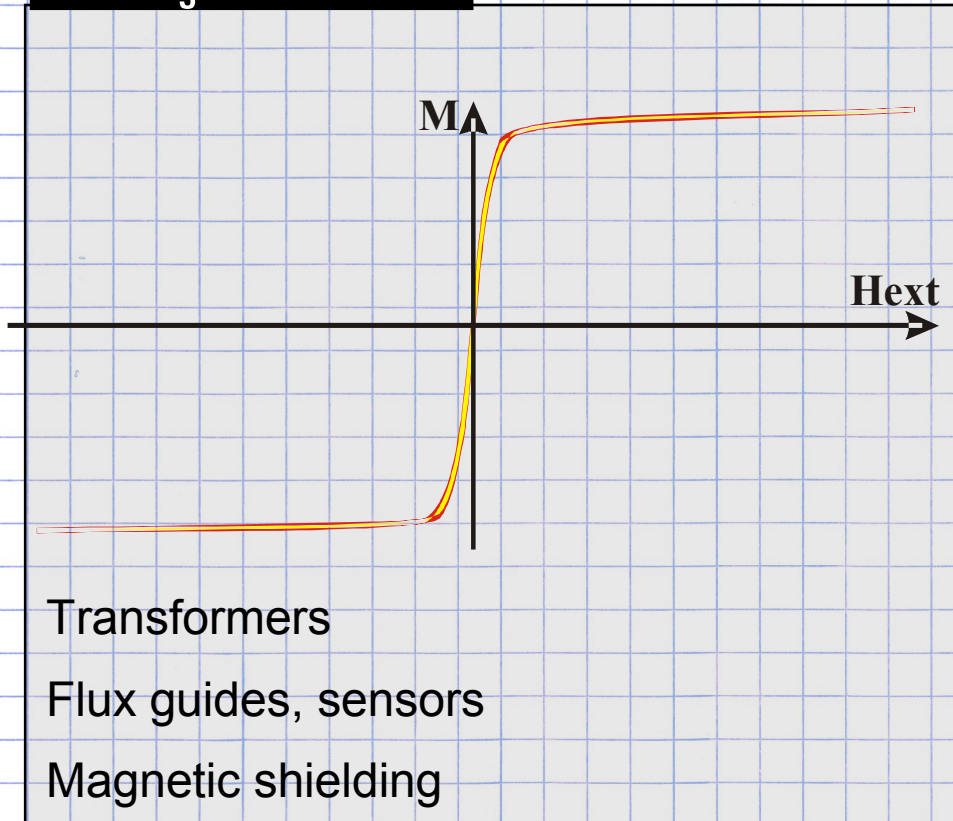
Zeeman energy:  $E_Z = -\mu_0 \mathbf{H} \cdot \mathbf{M}$



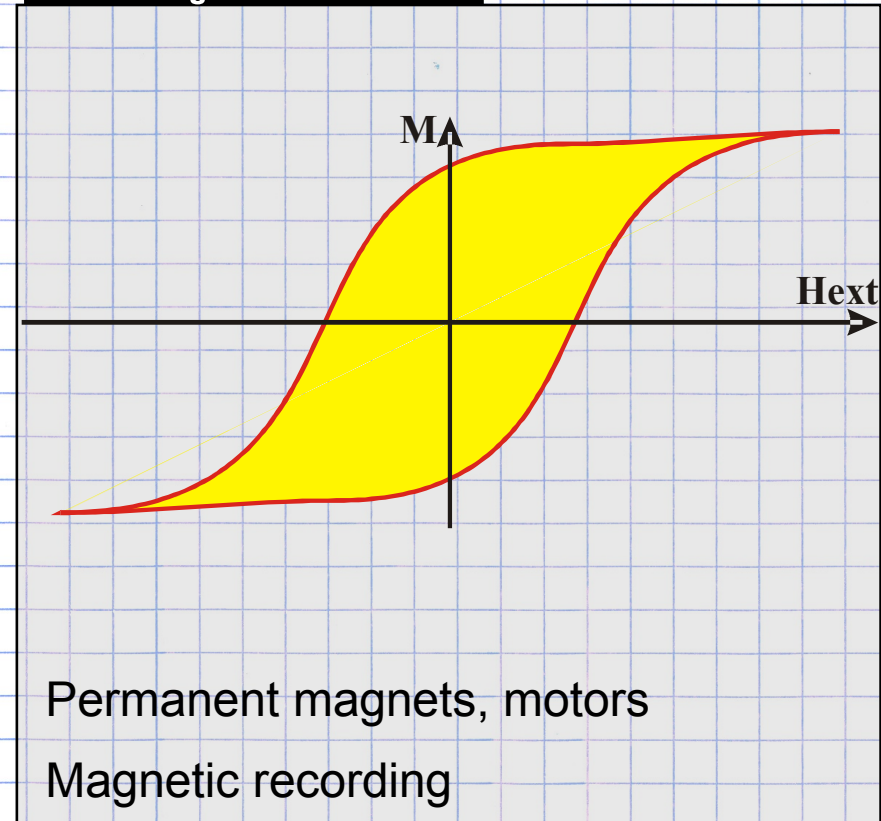




## Soft magnetic materials

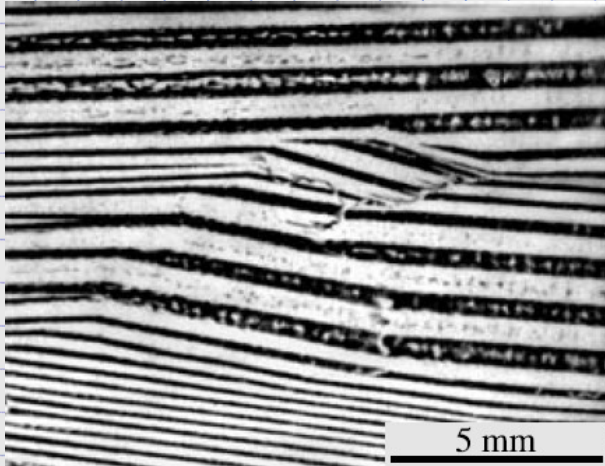


## Hard magnetic materials



## Bulk material

Numerous and complex magnetic domains

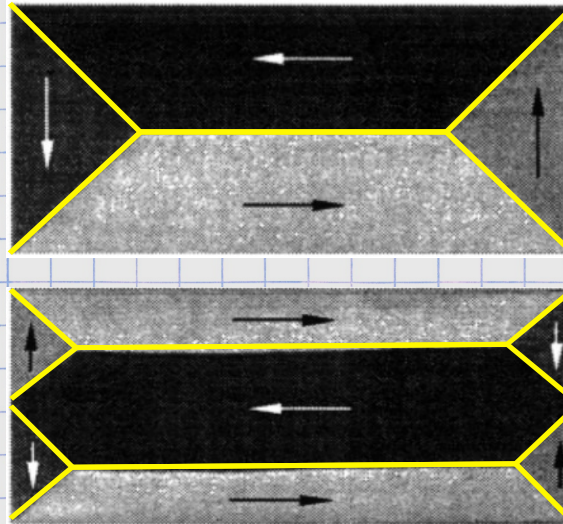


FeSi soft sheet

A. Hubert, *Magnetic domains*

## Mesoscopic scale

Small number of domains, simple shape

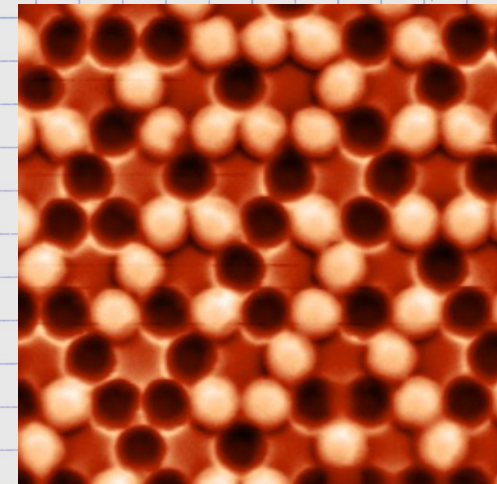


Microfabricated dots  
Kerr magnetic imaging

A. Hubert, *Magnetic domains*

## Nanometric scale

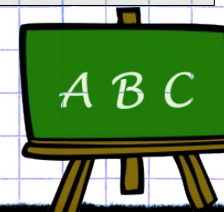
Magnetic single-domain



Nanofabricated dots  
MFM

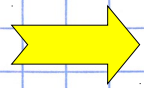
Sample courtesy :  
N. Rougemaille, I. Chioar

➡ Nanomagnetism ~ mesoscopic magnetism

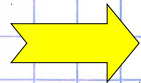
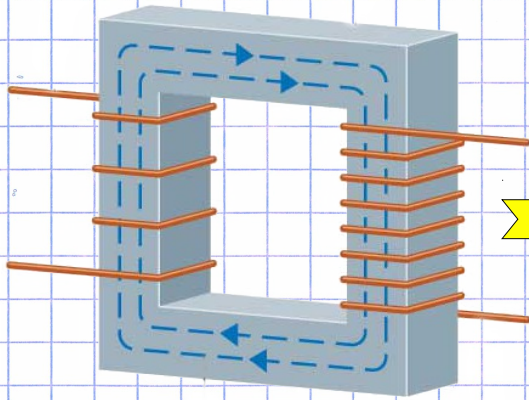
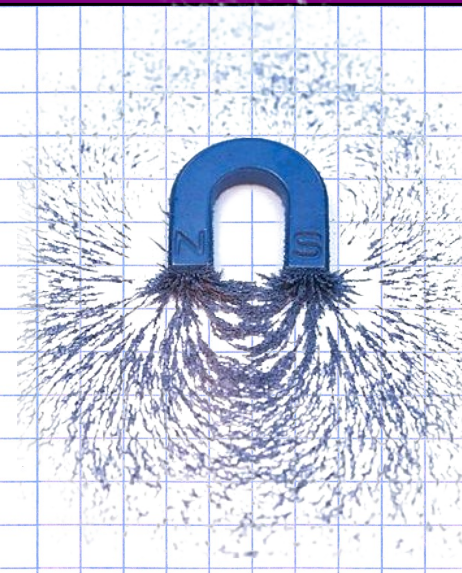


How small is 'Nano' ?

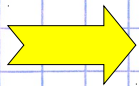
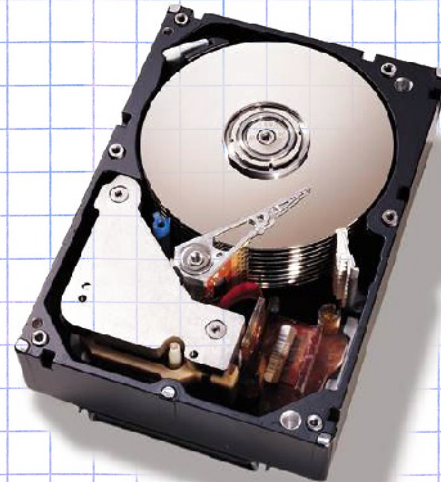




## 1. Fields, moments, materials



## 2. Magnetization processes



## 3. Low dimensions



## Magnetization

Magnetization vector **M**  $\longrightarrow$

Can vary in time and space.

$$\mathbf{M} = \begin{pmatrix} M_x \\ M_y \\ M_z \end{pmatrix} = M_s \begin{pmatrix} m_x \\ m_y \\ m_z \end{pmatrix}$$

Modulus is constant  $\longrightarrow$   
(hypothesis in micromagnetism)

$$m_x^2 + m_y^2 + m_z^2 = 1$$



Mean-field approach possible:  $M_s = M_s(T)$

## Exchange interaction

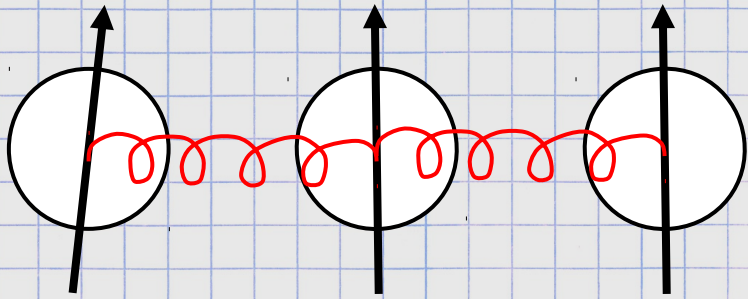
Atomistic view :  $\mathcal{E} = -2 \sum_{i>j} J_{i,j} \mathbf{S}_i \cdot \mathbf{S}_j$  (total energy)

Micromagnetic view :  $\mathbf{S}_i \cdot \mathbf{S}_j = S^2 \cos \theta_{i,j} \approx S^2 (1 - \theta_{i,j}^2 / 2)$

$$E = A (\nabla \cdot \mathbf{m})^2 \quad (\text{energy per unit volume})$$

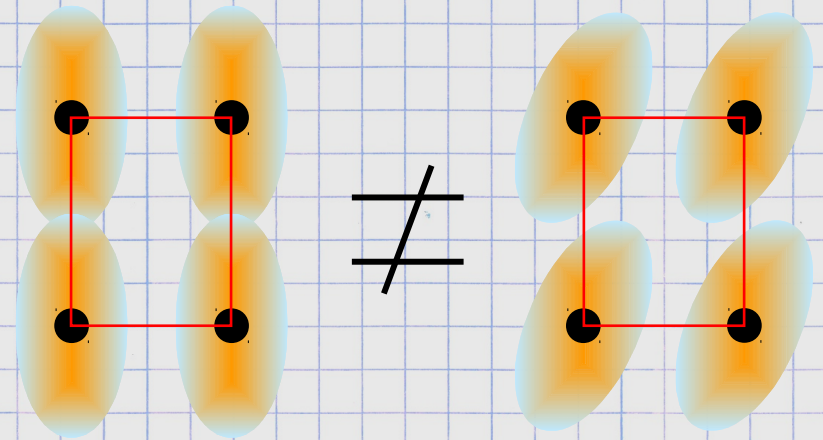


## Exchange energy



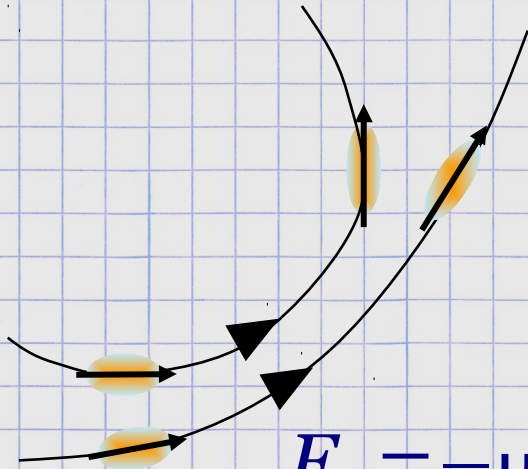
$$E_{\text{ex}} = A (\nabla \cdot \mathbf{m})^2$$

## Magnetocrystalline anisotropy energy



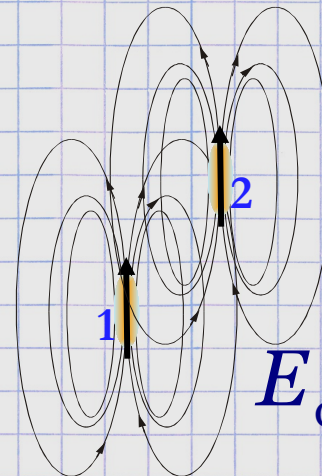
$$E_{\text{mc}} = K \sin^2 \theta$$

## Zeeman energy



$$E_d = -\mu_0 \mathbf{M} \cdot \mathbf{H}$$

## Dipolar energy



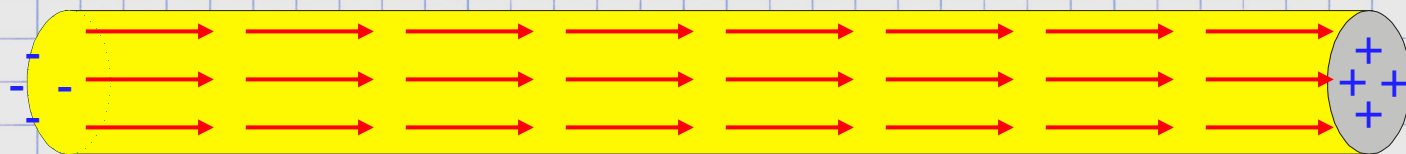
$$E_d = -\frac{1}{2} \mu_0 \mathbf{M} \cdot \mathbf{H}_d$$

**Magnetic charges** Maxwell equation  $\rightarrow \text{div}(\mathbf{H}_d) = -\text{div}(\mathbf{M})$

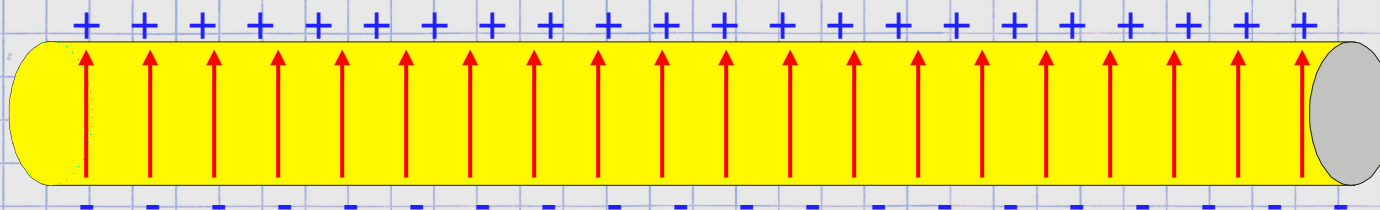
$\rho(\mathbf{r}) = -M_s \text{div}[\mathbf{m}(\mathbf{r})]$   $\rightarrow$  volume density of magnetic charges

$\sigma(\mathbf{r}) = M_s \mathbf{m}(\mathbf{r}) \cdot \mathbf{n}(\mathbf{r})$   $\rightarrow$  surface density of magnetic charges

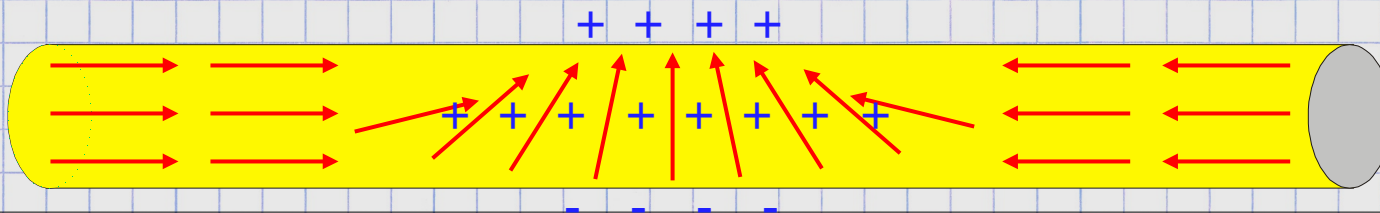
## Examples of magnetic « charges »



Notice: no charges and  $\mathcal{E}=0$  for infinite cylinder



Charges on surfaces



Surface and volume charges

## Take-away message

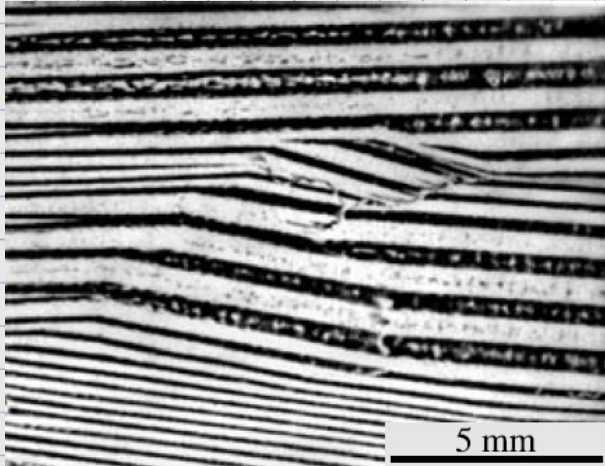
$\Rightarrow$  Dipolar energy favors alignment of magnetization with longest direction of sample





## Bulk material

Numerous and complex magnetic domains

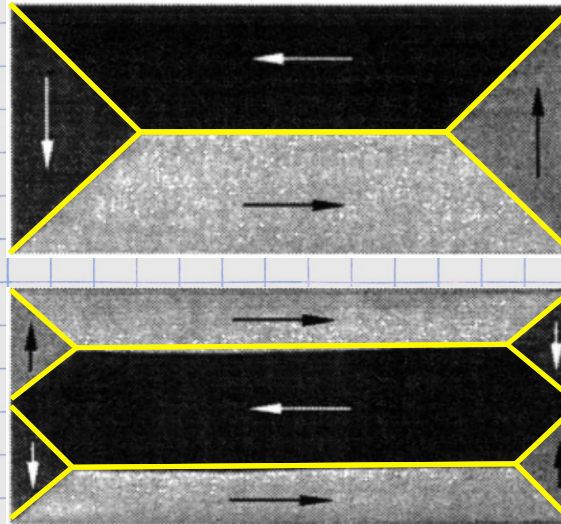


FeSi soft sheet

A. Hubert, *Magnetic domains*

## Mesoscopic scale

Small number of domains, simple shape

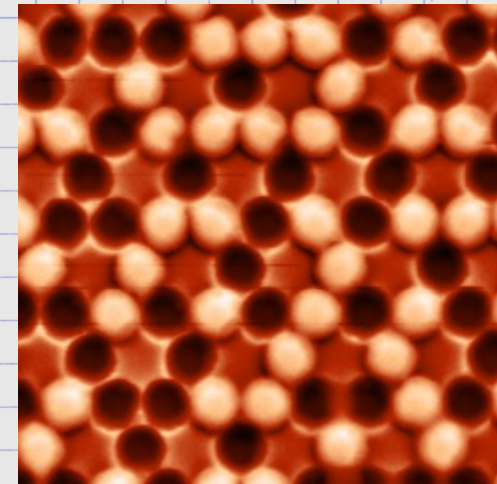


Microfabricated dots  
Kerr magnetic imaging

A. Hubert, *Magnetic domains*

## Nanometric scale

Magnetic single-domain



Nanofabricated dots  
MFM

Sample courtesy :  
N. Rougemaille, I. Chioar

↪ Nanomagnetism ~ mesoscopic magnetism



## Anisotropy exchange length

$$E = A(\partial_x \theta)^2 + K \sin^2 \theta$$

Exchange  
→ J/m

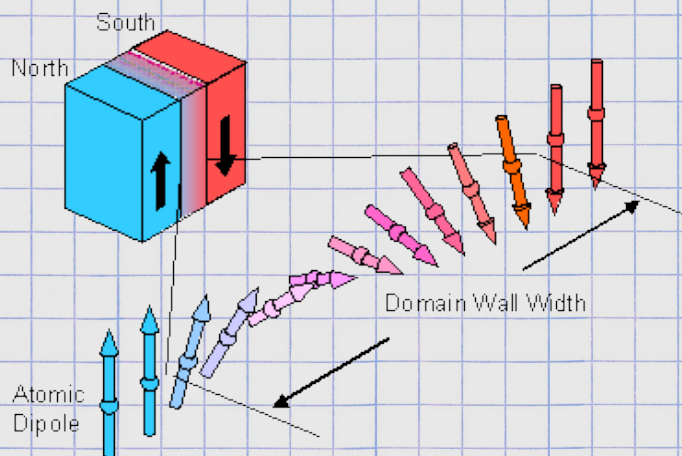
Anisotropy  
→ J/m<sup>3</sup>

Anisotropy exchange length:

$$\Delta_u \approx 1 \text{ nm} \rightarrow \Delta_u \geq 100 \text{ nm}$$

Hard

Soft



Often called *Bloch parameter*  
or *domain-wall width*

## Dipolar exchange length

$$E = A(\partial_x \theta)^2 + K_d \sin^2 \theta$$

Exchange  
→ J/m

Dipolar energy  
→ J/m<sup>3</sup>

$$K_d = \frac{1}{2} \mu_0 M_s^2$$

Dipolar exchange length:

$$= \sqrt{2A/\mu_0} M_s^2$$

$$\Delta_d \approx 3-10 \text{ nm}$$

Single-domain critical size  
relevant for nanoparticles  
made of soft magnetic material



Often called *Exchange length*

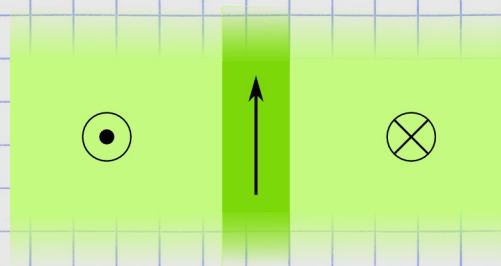
Notice:

Other length scales: with field etc.





## Bloch domain wall in the bulk (2D)



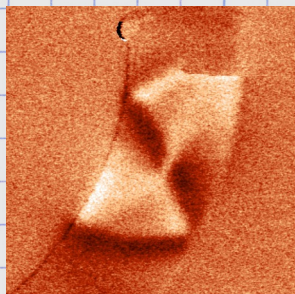
- ⇒ No magnetostatic energy
- ⇒ Width  $\Delta_u = \sqrt{A/K}$
- ⇒ Areal energy  $\gamma_w = 4\sqrt{AK}$



Other angles & anisotropy

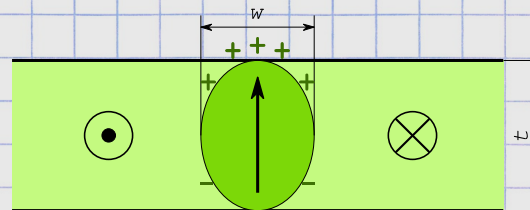
F. Bloch, Z. Phys. 74, 295 (1932)

## Constrained walls (eg : in stripes)

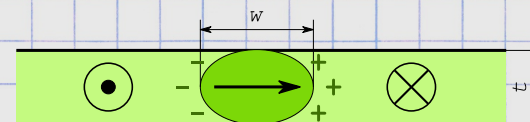


Permalloy  
(15nm)  
Strip 500nm

## Domain walls in thin films (2D → 1D)

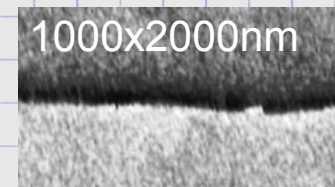
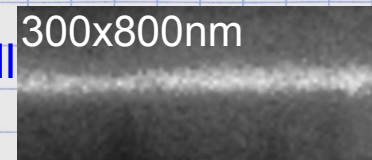


Bloch wall  
 $t \gtrsim w$



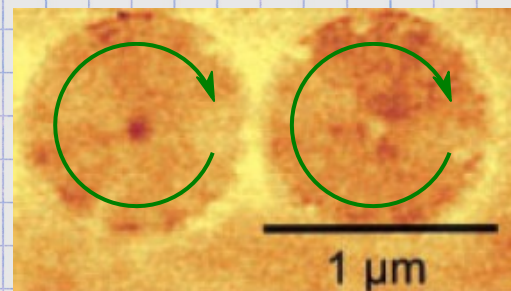
Néel wall  
 $t \lesssim w$

- ⇒ Contains magnetostatic energy
- ⇒ No exact analytics



L. Néel, C. R. Acad. Sciences 241, 533 (1956)

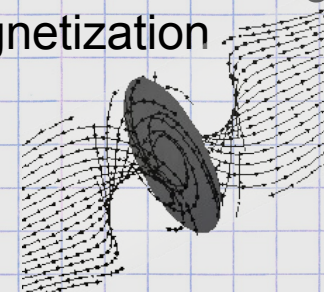
## Magnetic vortex (1D → 0D)



T. Shinjo et al.,  
Science 289, 930 (2000)

## Bloch point (0D)

- ⇒ Point with vanishing magnetization



W. Döring, J. Appl. Phys. 39, 1006 (1968)

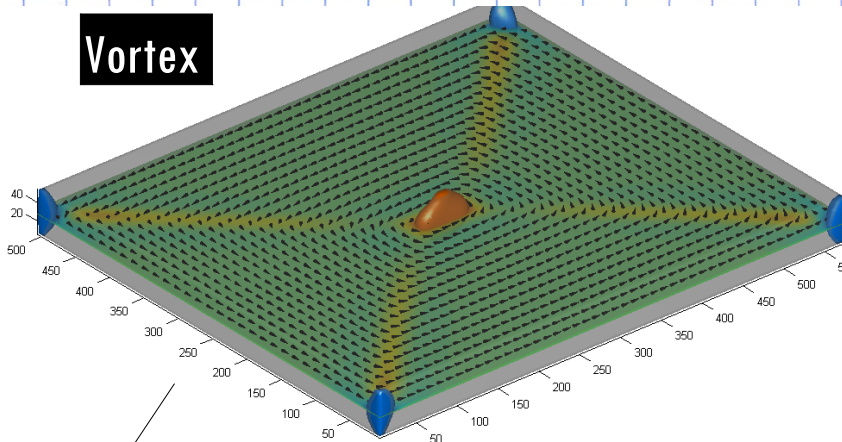


- ➡ **1. Low-dimensional structures in nanomagnetism**
- ➡ **2. What could come next for magnetism in data storage ?**
- ➡ **3. An example of academic study towards 'next'**

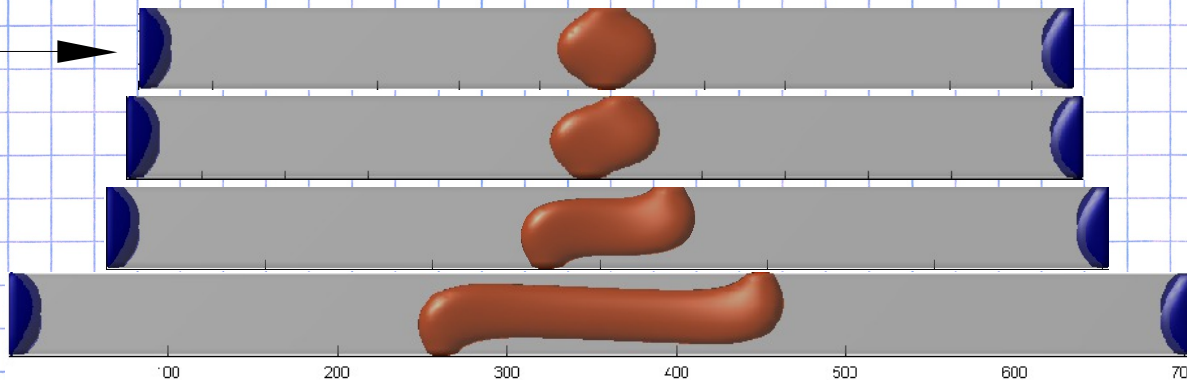
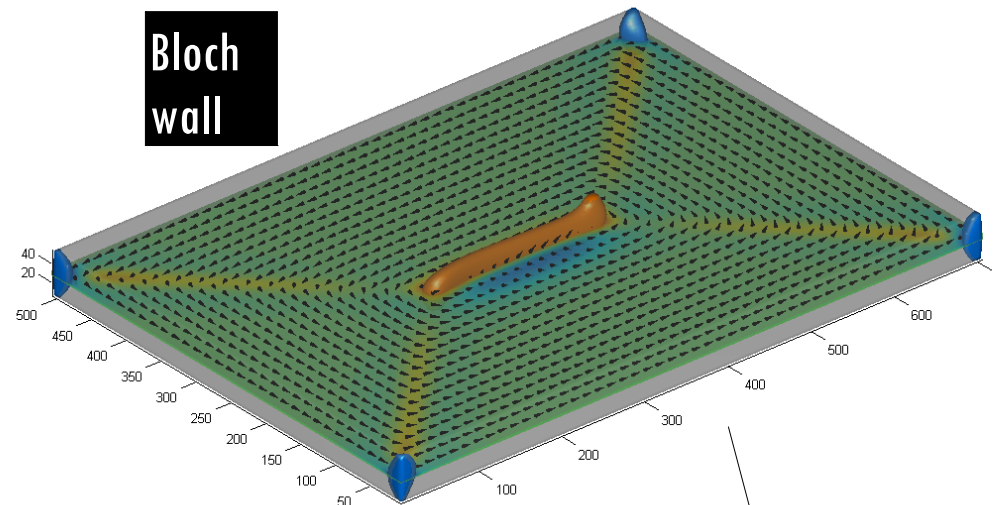




**Vortex**



**Bloch wall**

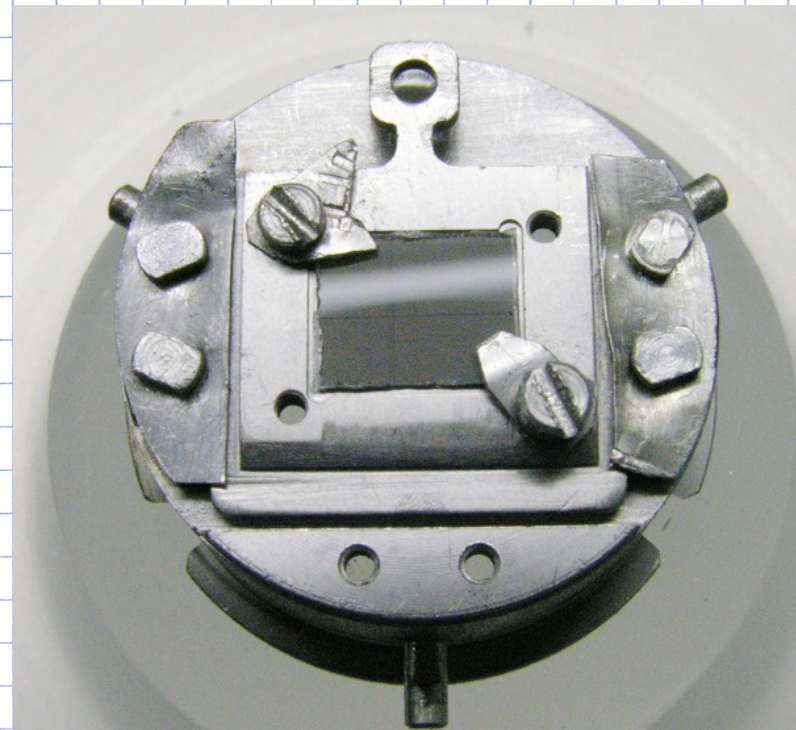
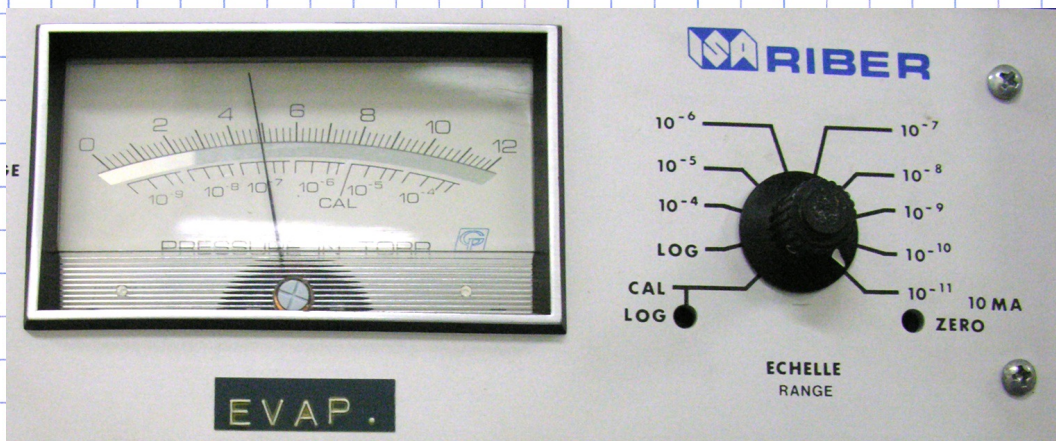
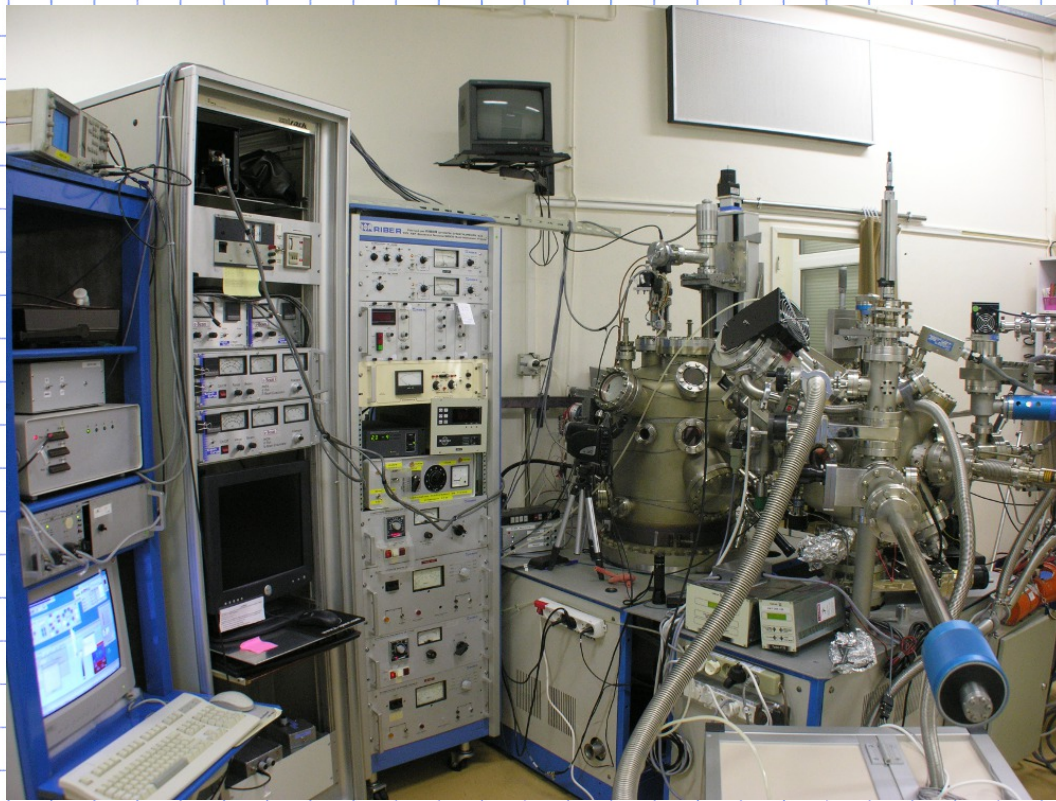


A. Masseboeuf et al., Phys. Rev. Lett. 104, 127204 (2010)

↪ Elongated dots → Breaking of symmetry (2nd order transition) → Order parameter



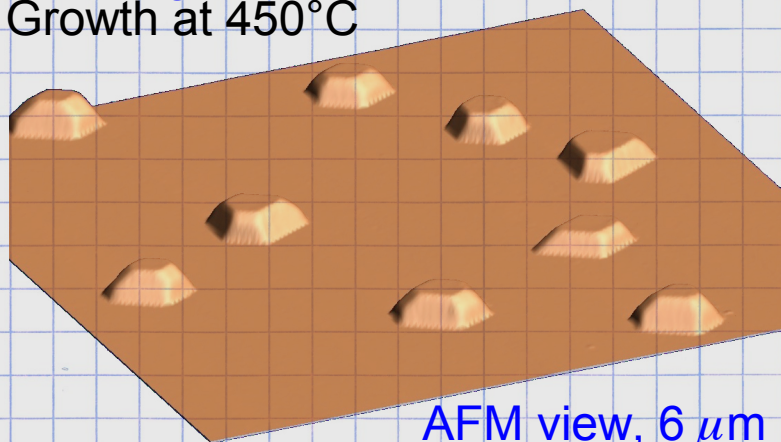
# How does an ultra-high vacuum setup for epitaxy (single-crystal) growth look like ?



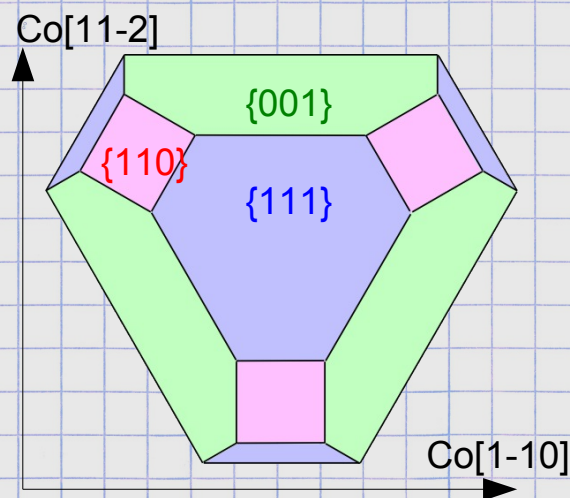


## Growth and structure

Stacking: Al<sub>2</sub>O<sub>3</sub>(11-20) \ W[10nm] \ Co \ Au  
Growth at 450°C



AFM view, 6 μm FoV

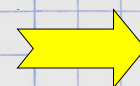
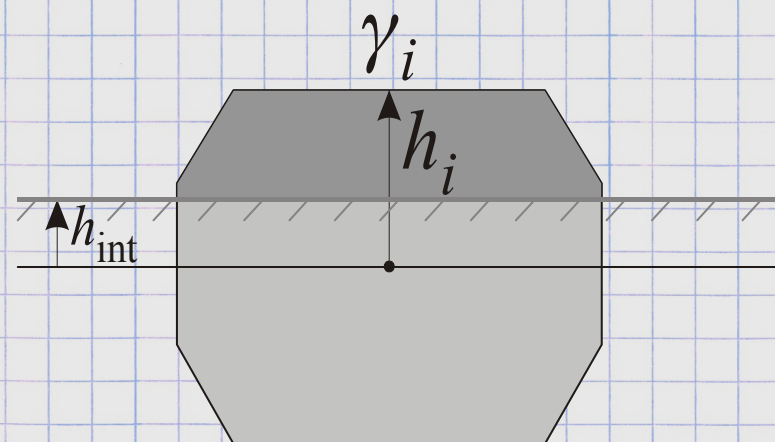


O. Fruchart et al., J. Phys. : Condens. Matter 25, 496002 (2013)

## Wulff Kaishev's theorem

Supported crystal (growth on surfaces)

$$\frac{\gamma_i}{h_i} = \frac{\gamma_S - \gamma_{\text{int}}}{h_{\text{int}}} = \text{Constant}$$

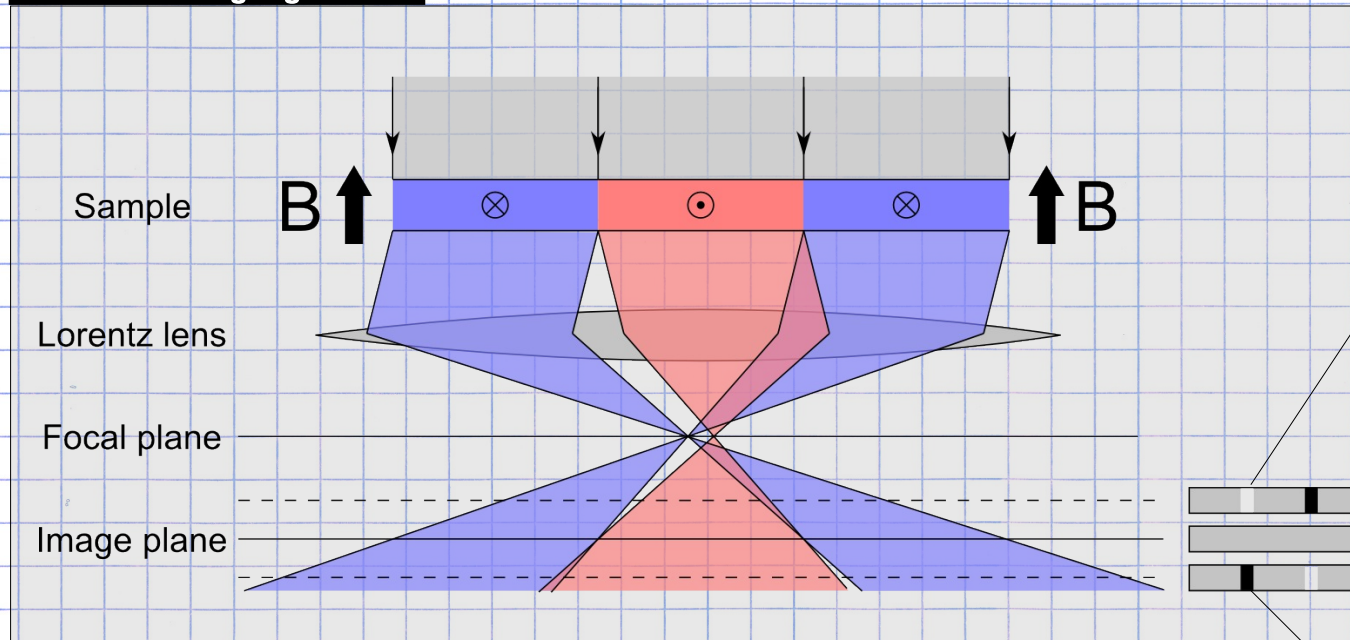


Truncated crystal

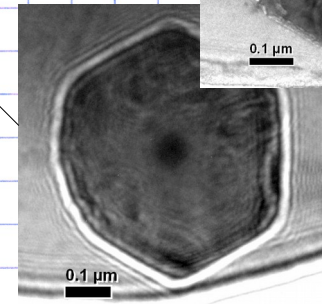
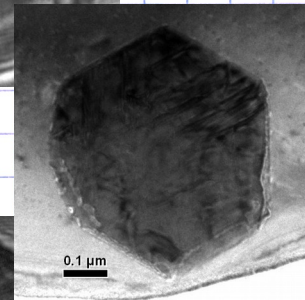
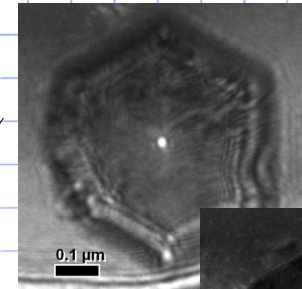
P. Müller and R. Kern, Surf. Sci. 457, 229 (2000)  
(and incl. ref.)



## Fresnel imaging mode



Self-assembled  
fcc Co dots  
(vortex state)



↪ Sensitive mainly to in-plane components of magnetization integrated over the sample's thickness

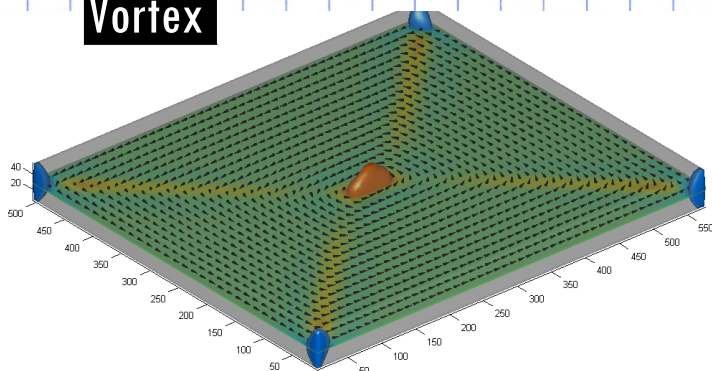


**Pascale Bayle-Guillemaud (INAC)**  
**Aurélien Masseboeuf et al. (INAC → CEMES)**

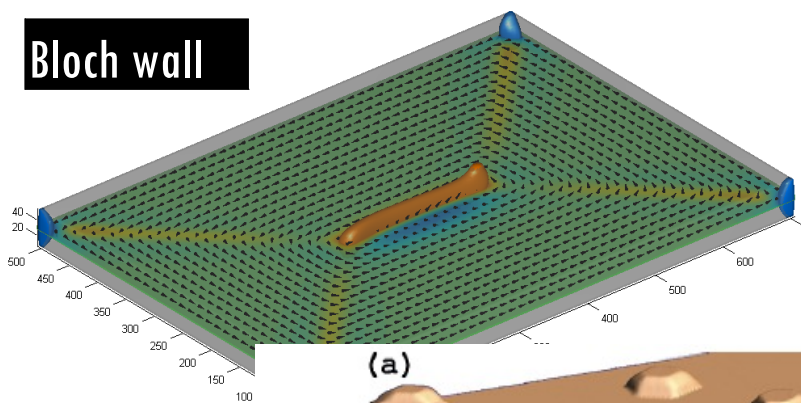




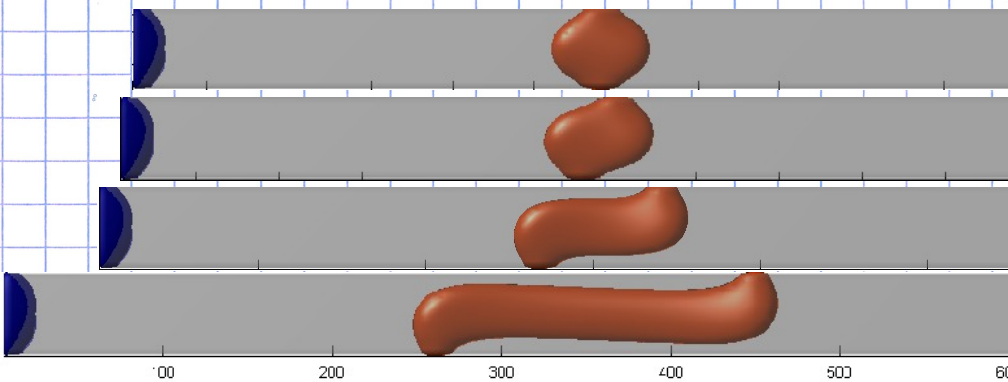
Vortex



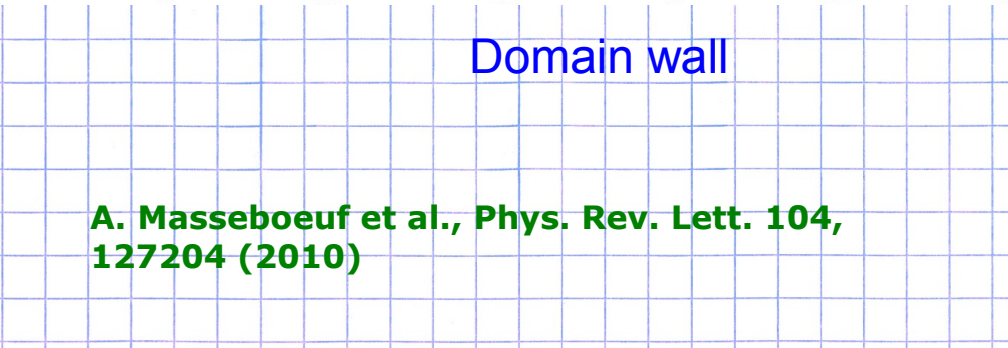
Bloch wall



Vortex

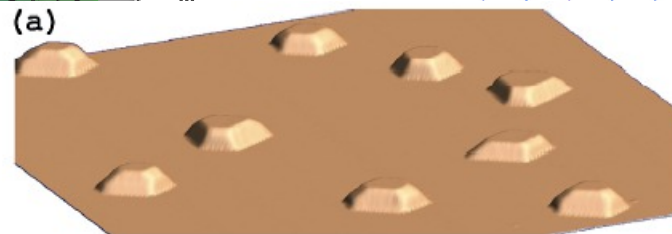


Domain wall

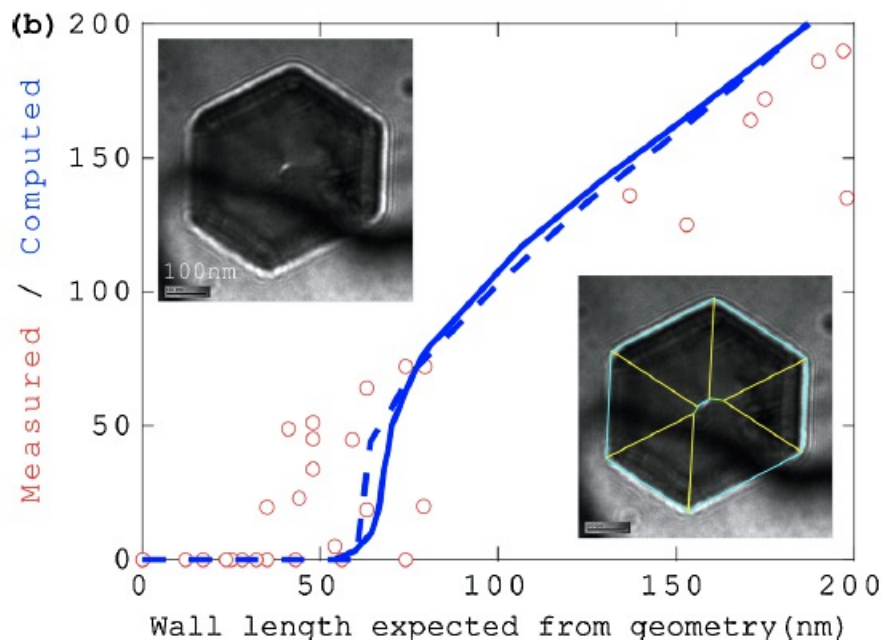


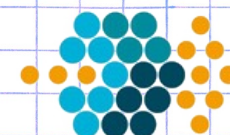
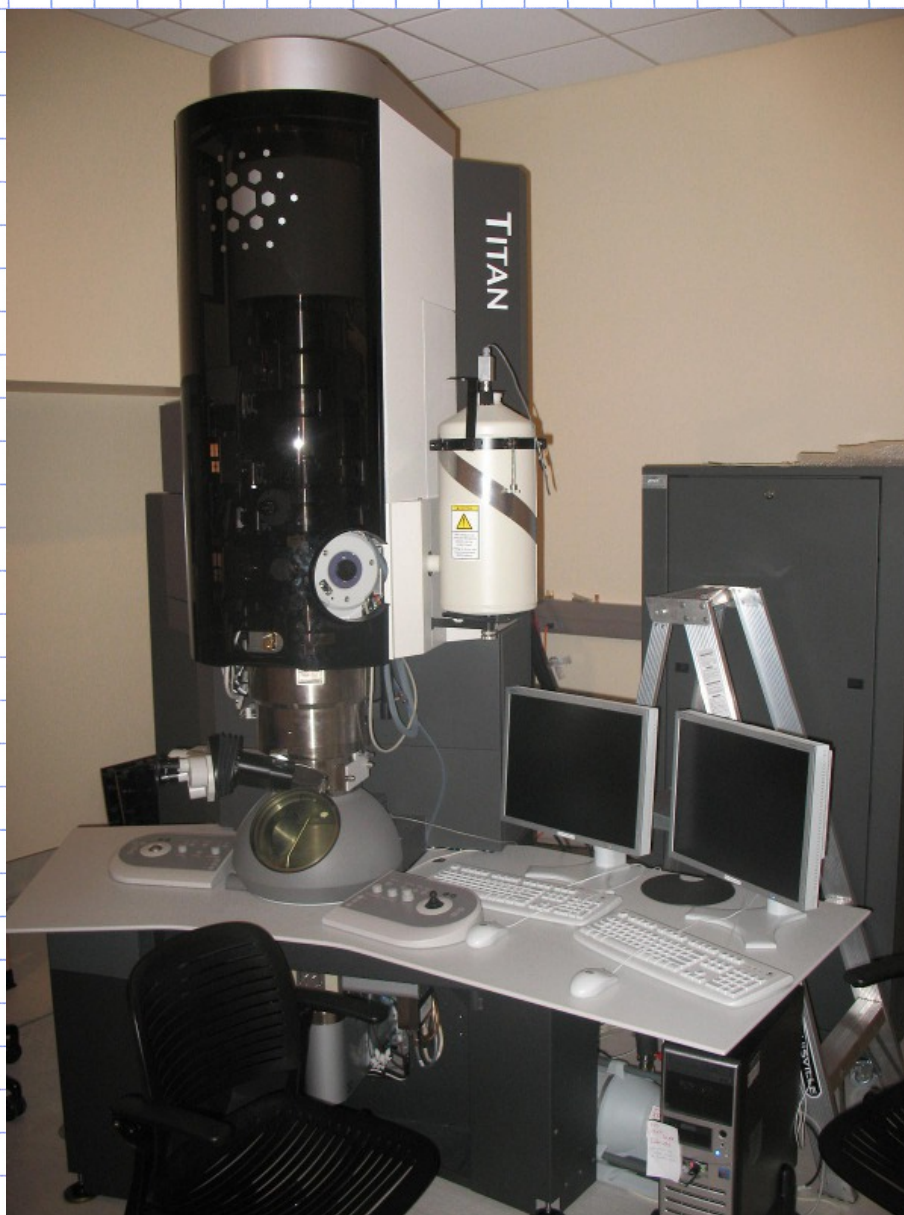
A. Masseboeuf et al., Phys. Rev. Lett. 104, 127204 (2010)

(a)



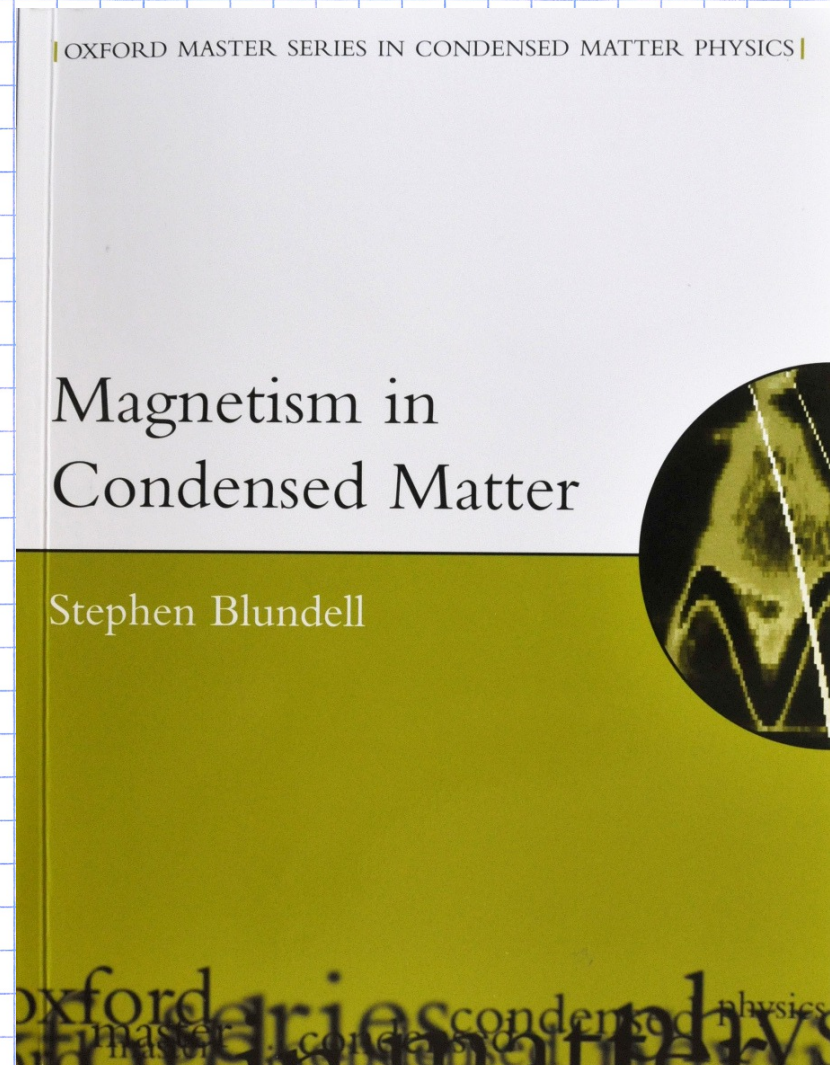
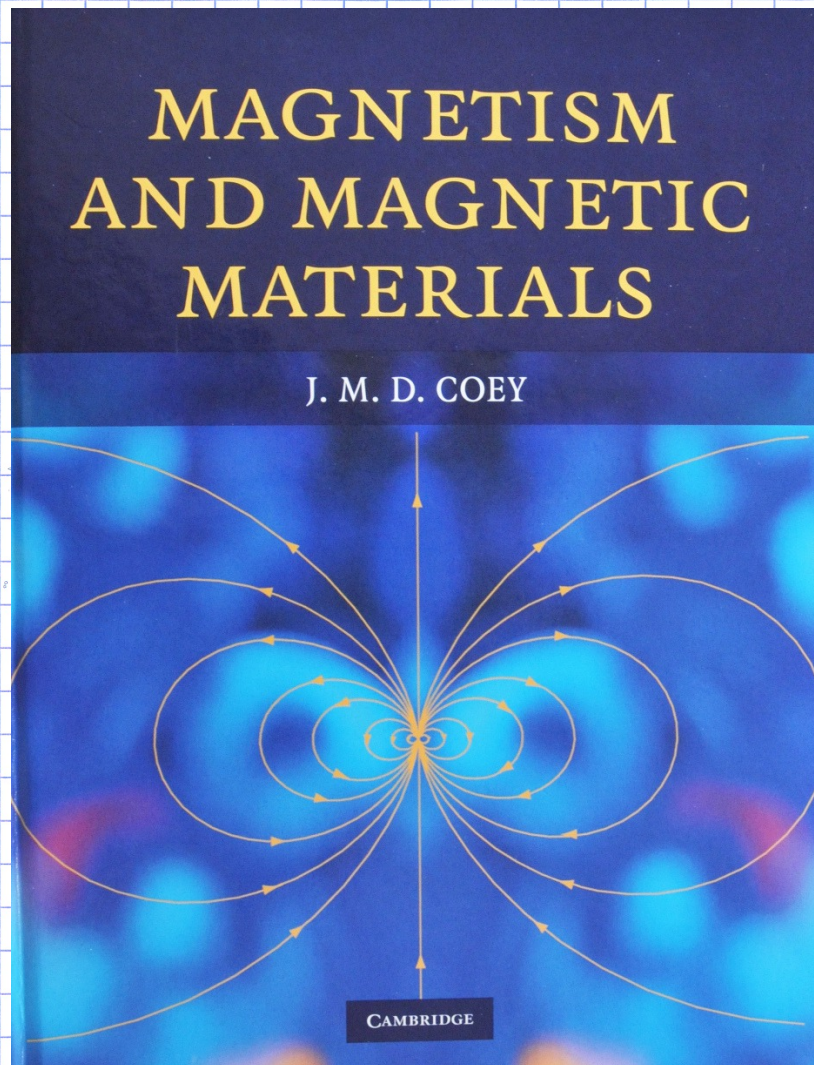
(b)





**mETSa**





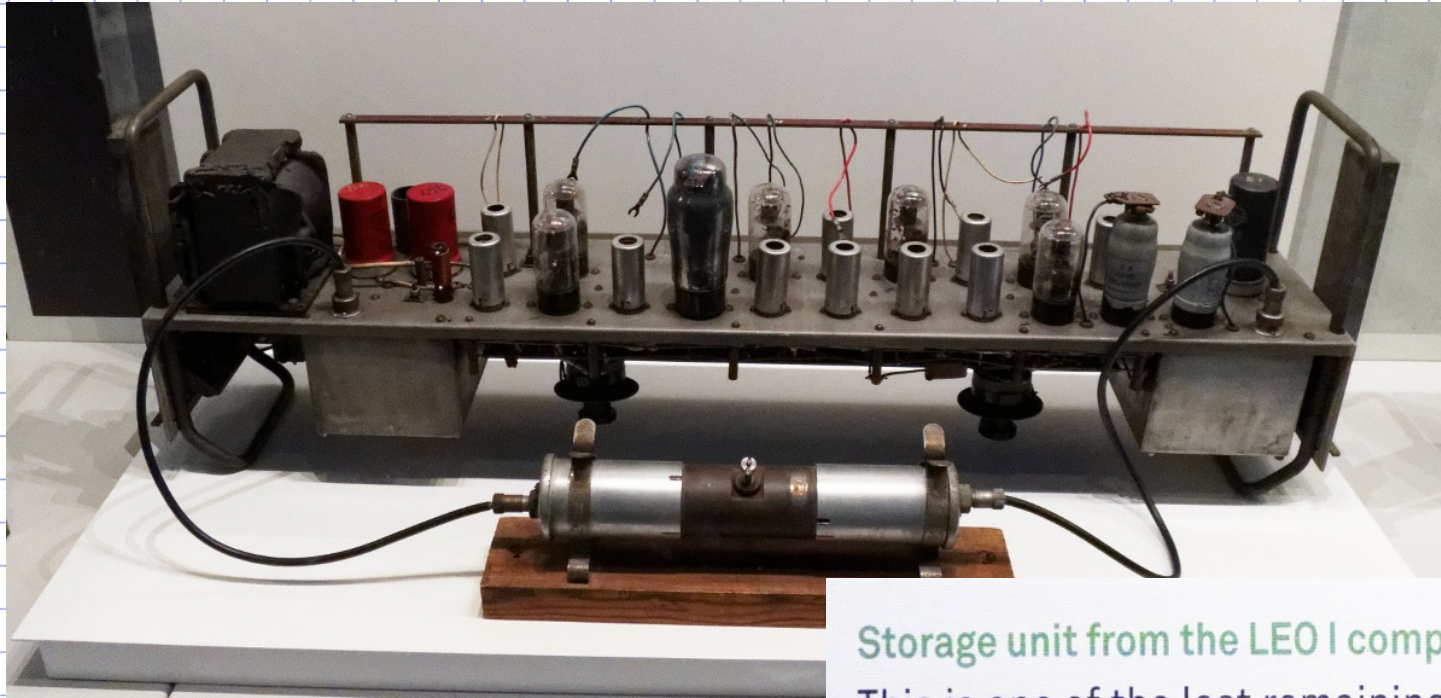
Repository of lectures of the European School on Magnetism: <http://magnetism.eu>





- ➡ 1. Low-dimensional structures in nanomagnetism
- ➡ 2. What could come next for magnetism in data storage ?
- ➡ 3. An example of academic study towards 'next'





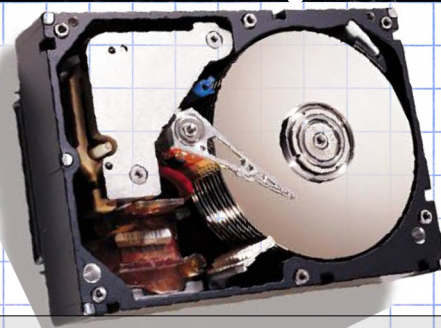
## Storage unit from the LEO I computer, 1951

This is one of the last remaining parts of the original Lyons Electronic Office – the first computer built for ordinary business tasks. This storage unit consists of a regeneration chassis and a short mercury delay line. The delay line slowed down, and therefore momentarily stored, electronic signals, and the chassis amplified and ‘clocked’ the signals.

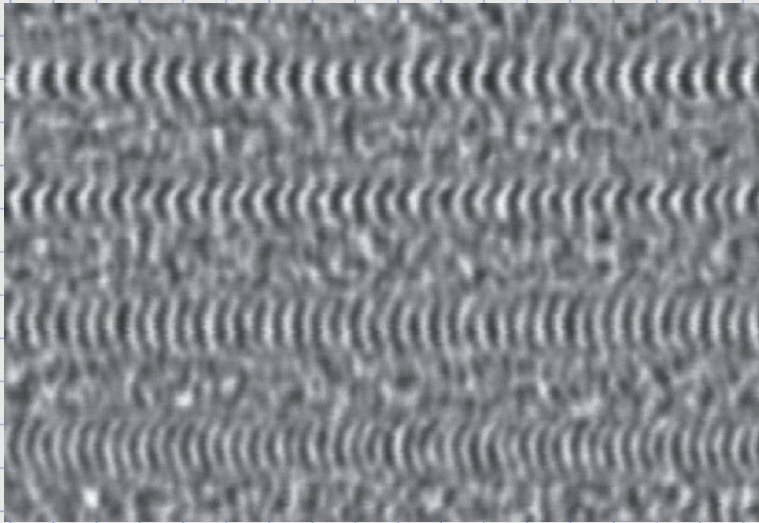
Donated by: J Lyons & Co. Ltd Object No: 1965-33  
Image: Science Museum/SSPL



## Magnetic bits on Hard Disk Drive

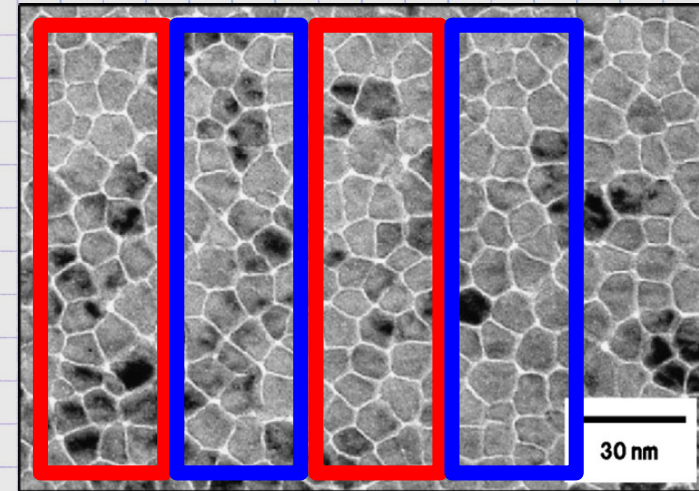


Co-based hard disk media : bits 50nm and below



B. C. Stipe, Nature Photon. 4, 484 (2010)

## Underlying microstructure



S. Takenori, J. Magn. Magn. Mater. 321, 562 (2009)

## Technological / Physical breakdown

- ↪ Compromise time stability, writability, readability
- ↪ Disruptive solutions sought



1956



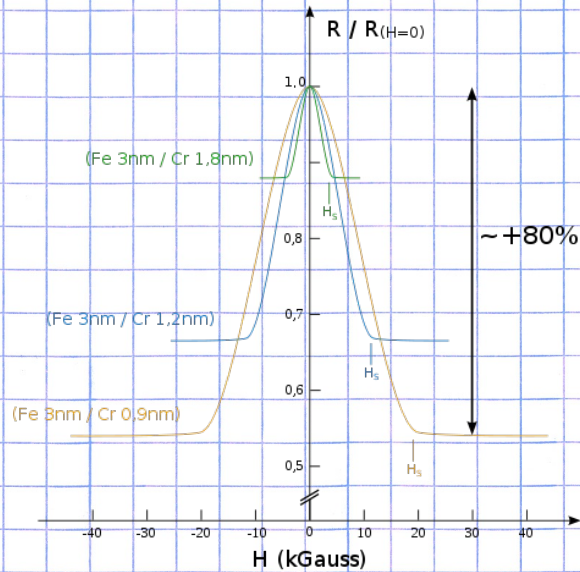
RAMAC, IBM, first hard disk drive



1986



RenaultFive.com



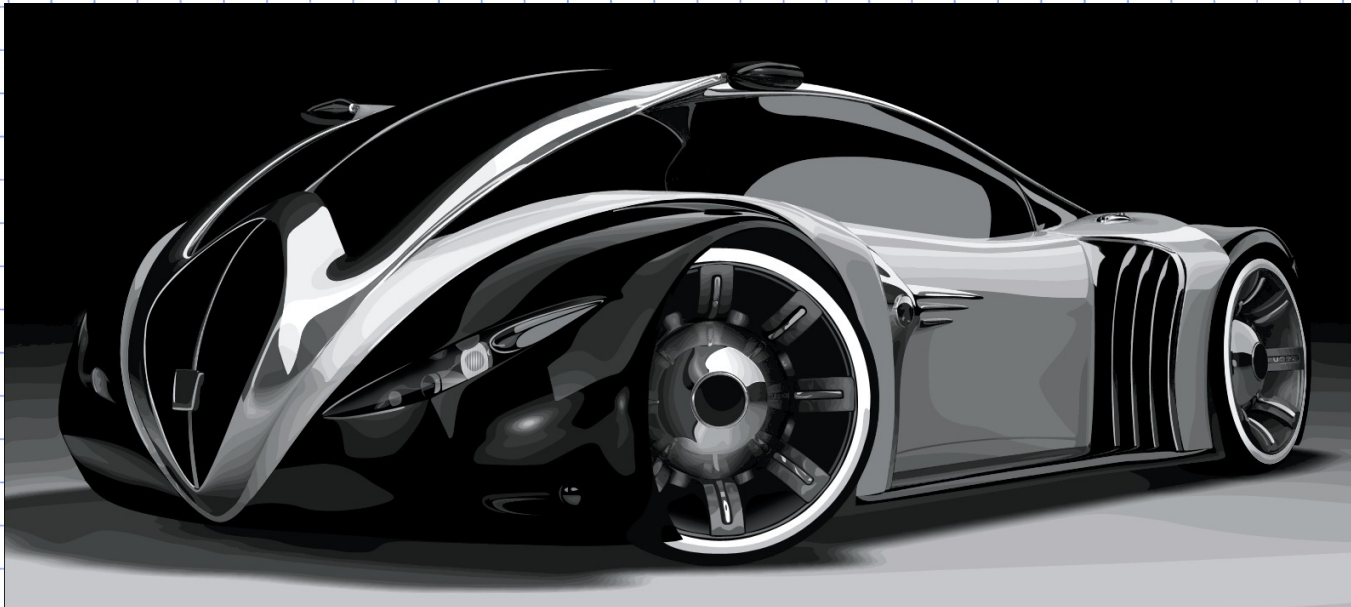
Discovery of Giant Magneto-Resistance  
→ Nobel prize in Physics 2007

1998



GMR implemented in HDD read heads  
 $\times 10^6$  increase of density from 1956





## Physics (recent)

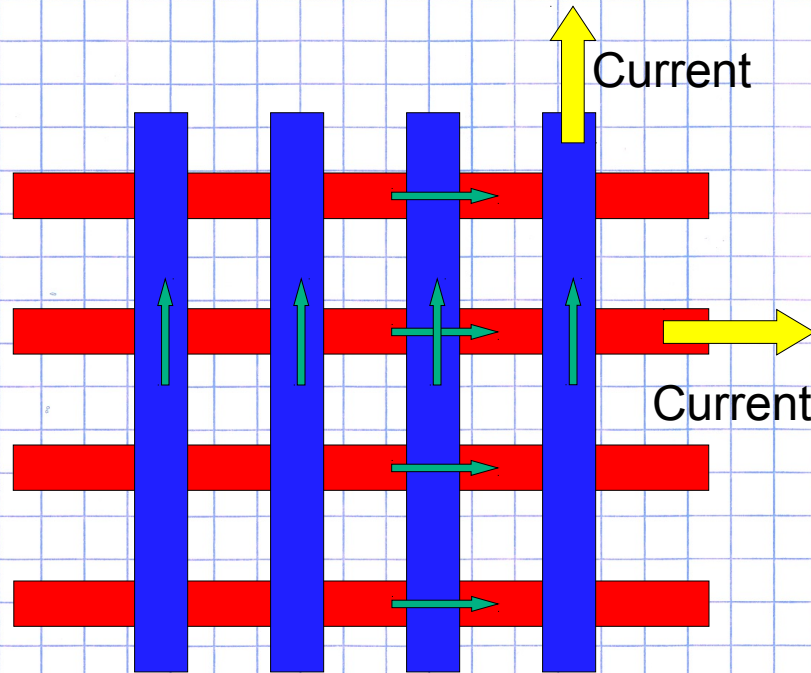
- ⇒ Spin-transfer torques. Induces magnetization switching, oscillations
- ⇒ Interfacial effects, chirality

## Technology (to come)

- ⇒ Magnetic Random Access Memories (dots)
- ⇒ Logic and memory devices based on domain walls. 3D memories ?

## MRAM = Magnetic Random Access Memory

### Overview



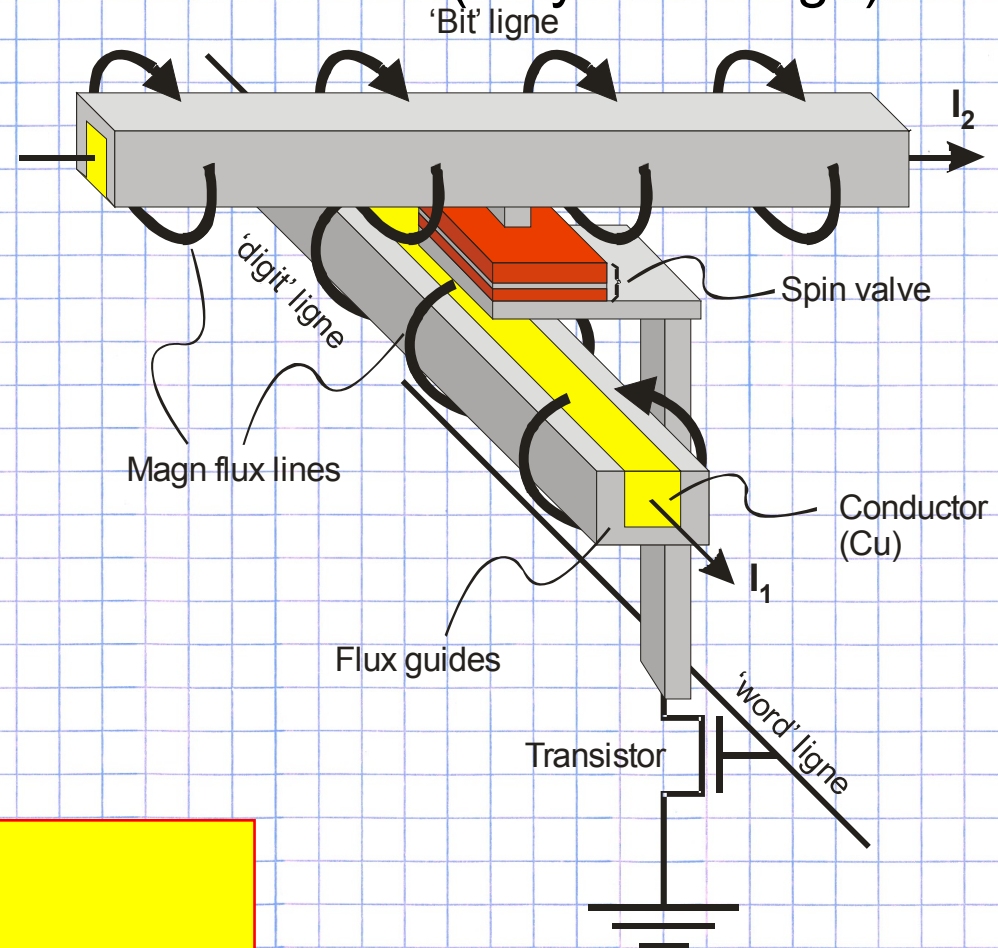
### Main features:

Solid state memory

Non-volatile and fast

Issues being fixed → entered semiconductor roadmap

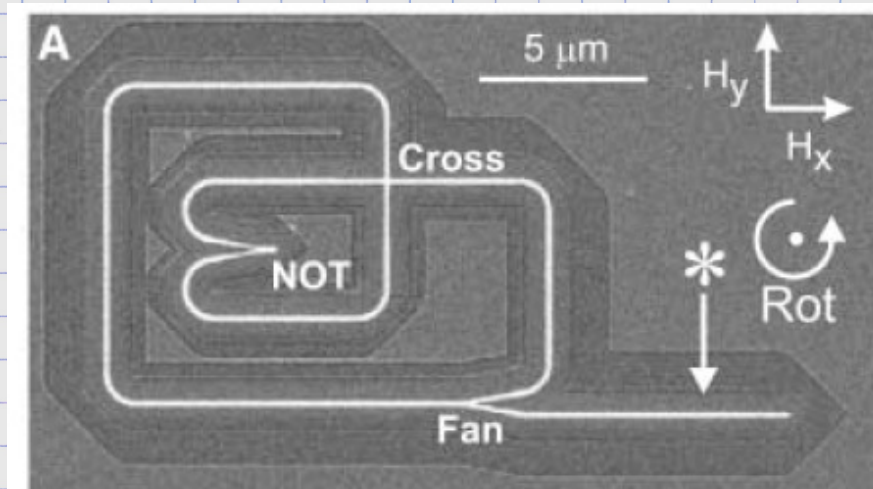
### Detail of a cell (very old design)







## Magnetic logic with domain walls (Field driven)

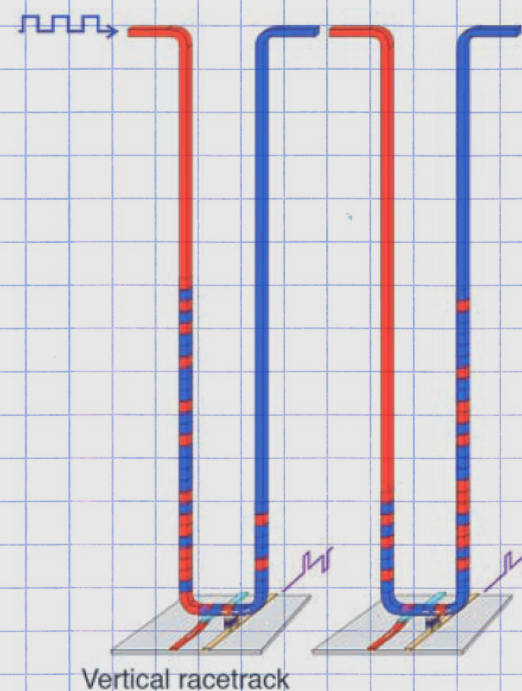


D. A. Allwood et al., Science 309, 1688 (2005)

### Limitation:

Requires homogeneous rotating field

## Proposal for a race-track memory in 3D



S. S. P. Parkin, Science 320, 190 (2008)  
+ patents (IBM)

↪ Potentially 3D storage, however  
technologically challenging  
↪ Cylinders are the 'natural'  
geometry



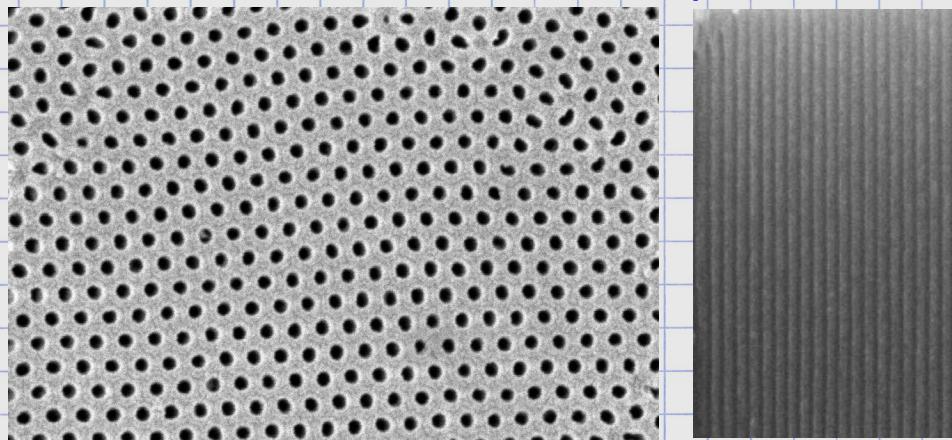
- ➡ **1. Low-dimensional structures in nanomagnetism**
- ➡ **2. What could come next for magnetism in data storage ?**
- ➡ **3. An example of academic study towards 'next'**





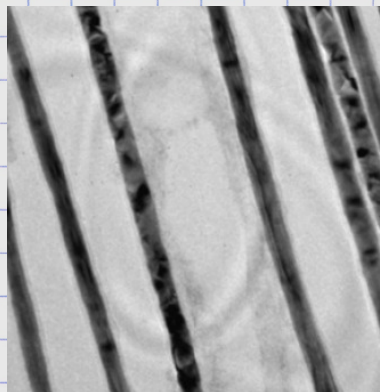
## The basics

Anodization of aluminum → template



H. Masuda, *Science* **268**, 1466-1468 (1995)

Electroplating → magnetic nanowires

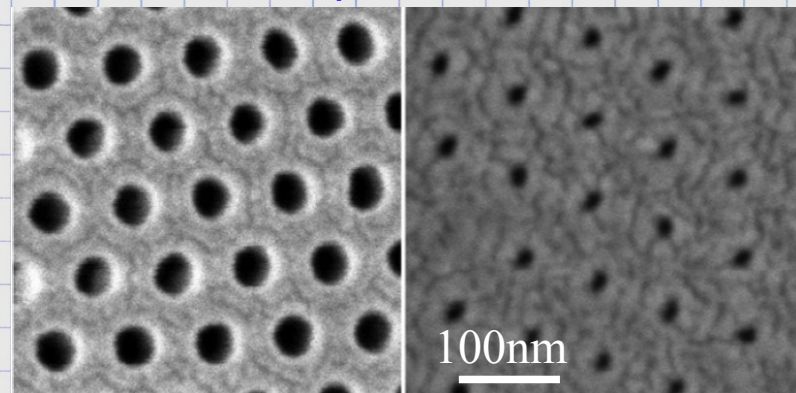


100nm

⇒ Simple metals and alloys :  
Co, Ni,  $\text{Fe}_{20}\text{Ni}_{80}$

## Specific aspects

ALD to reduce pore diameter

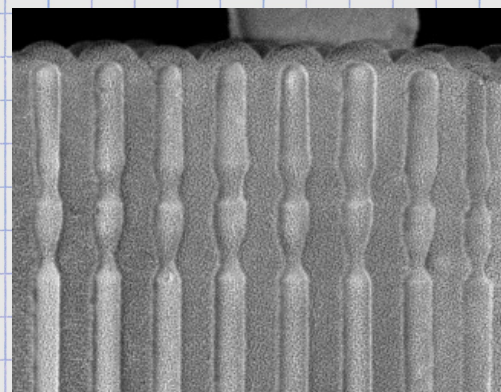


S. Da Col et al., *Appl. Phys. Lett.* **98**, 112501 (2011)

⇒ Decrease dipolar interactions

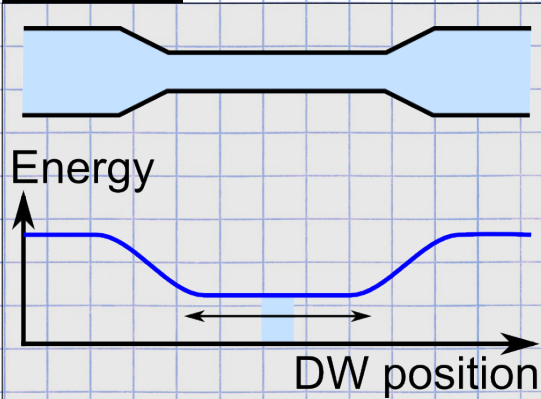
Modulation of pore diameter

S. Allende et al., *Phys. Rev. B* **80**, 174402 (2009)



⇒ Landscape for domain walls

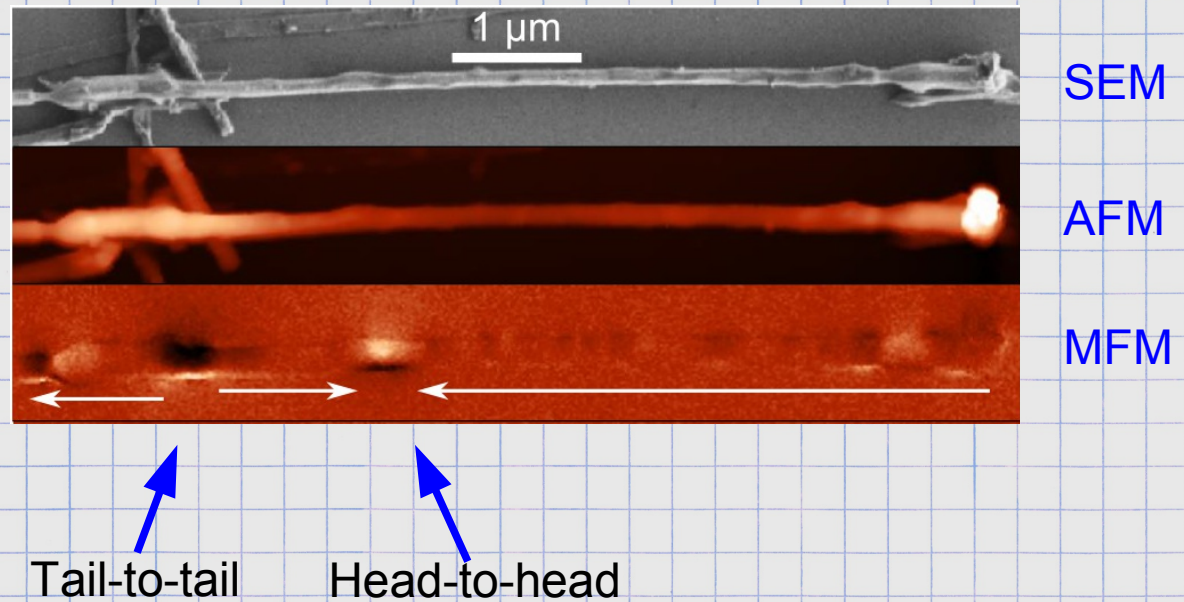
## Principle



- ⇒ Provides energy landscape for domain walls
- ⇒ NB : reports with modulations however no domain walls

K. Pitzschel et al., J. Appl. Phys. 109, 033907 (2011)

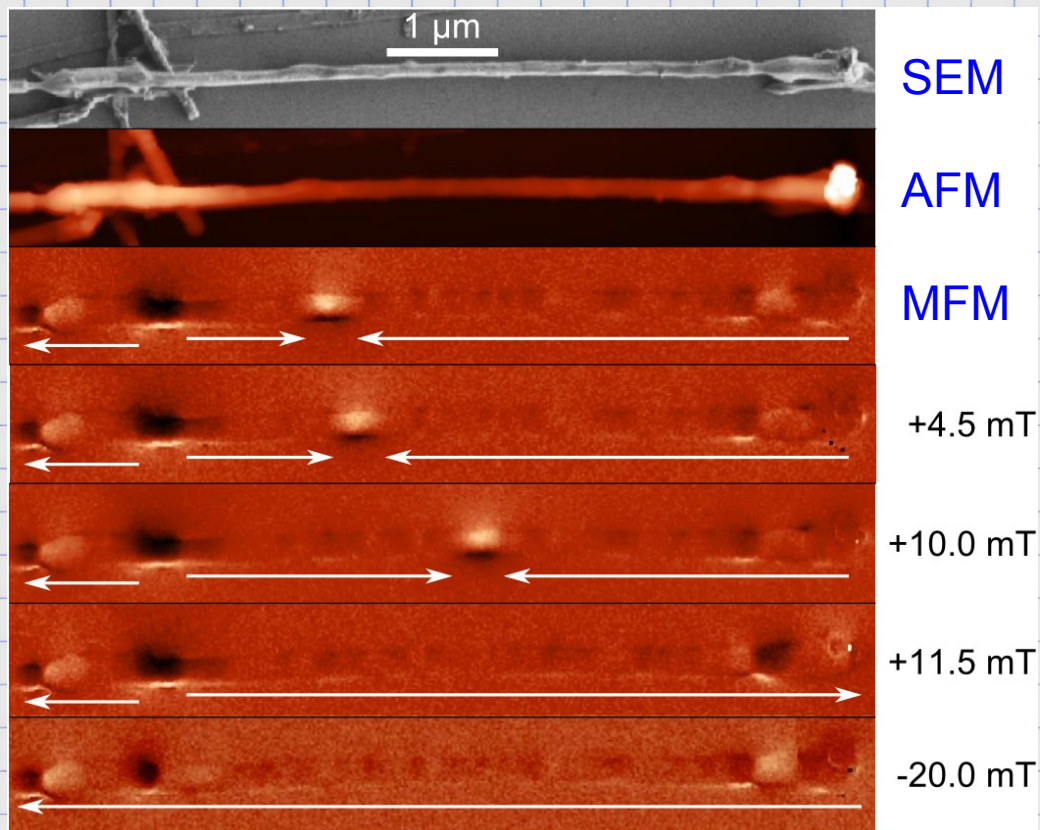
## Nucleation of domain walls



⇒ Protrusions create a 'box' for domain walls

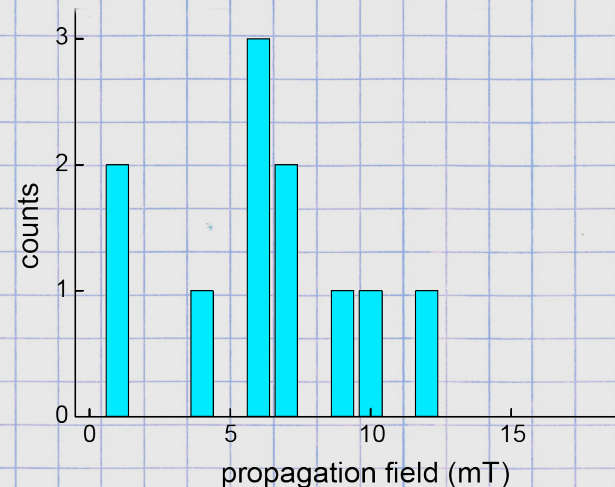


## Experiments



↪ Domain-wall motion demonstrated (range 1-10mT)  
↪ Pinning at modulations of diameter

## Straight sections

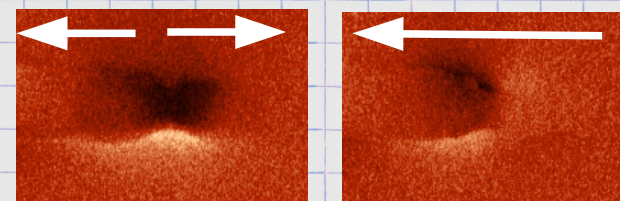


⇒ Distribution of propagation fields, range 1-10mT

⇒ Similar to the case of strips

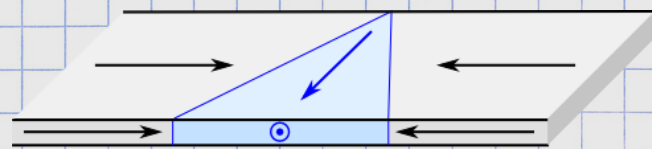
**J. Sampaio et al., J. Appl. Phys. (2013)**

## Protrusions and constrictions

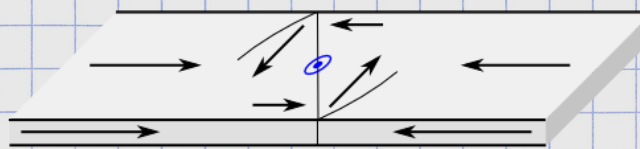


⇒ Pinning field ~30mT

## Domain walls in one-dimensional systems



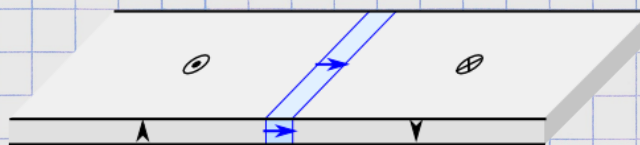
Transverse



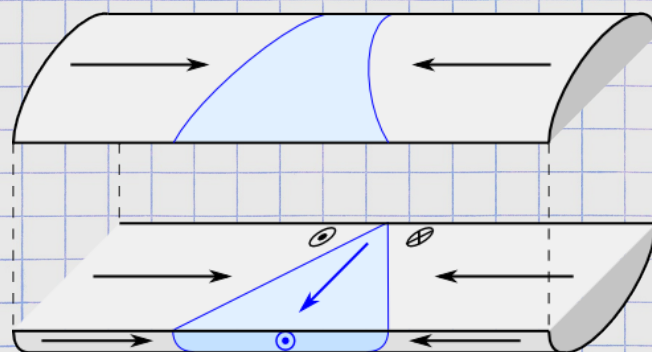
Vortex



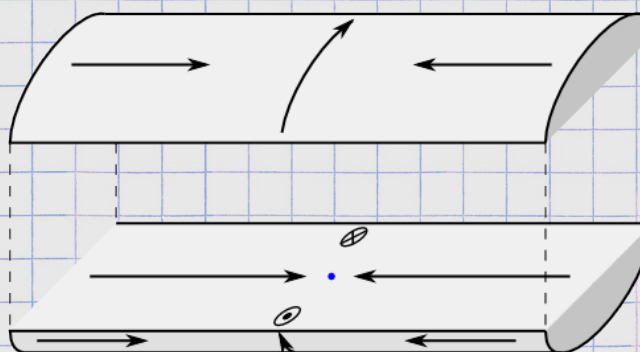
Bloch



Néel



Transverse (TW)



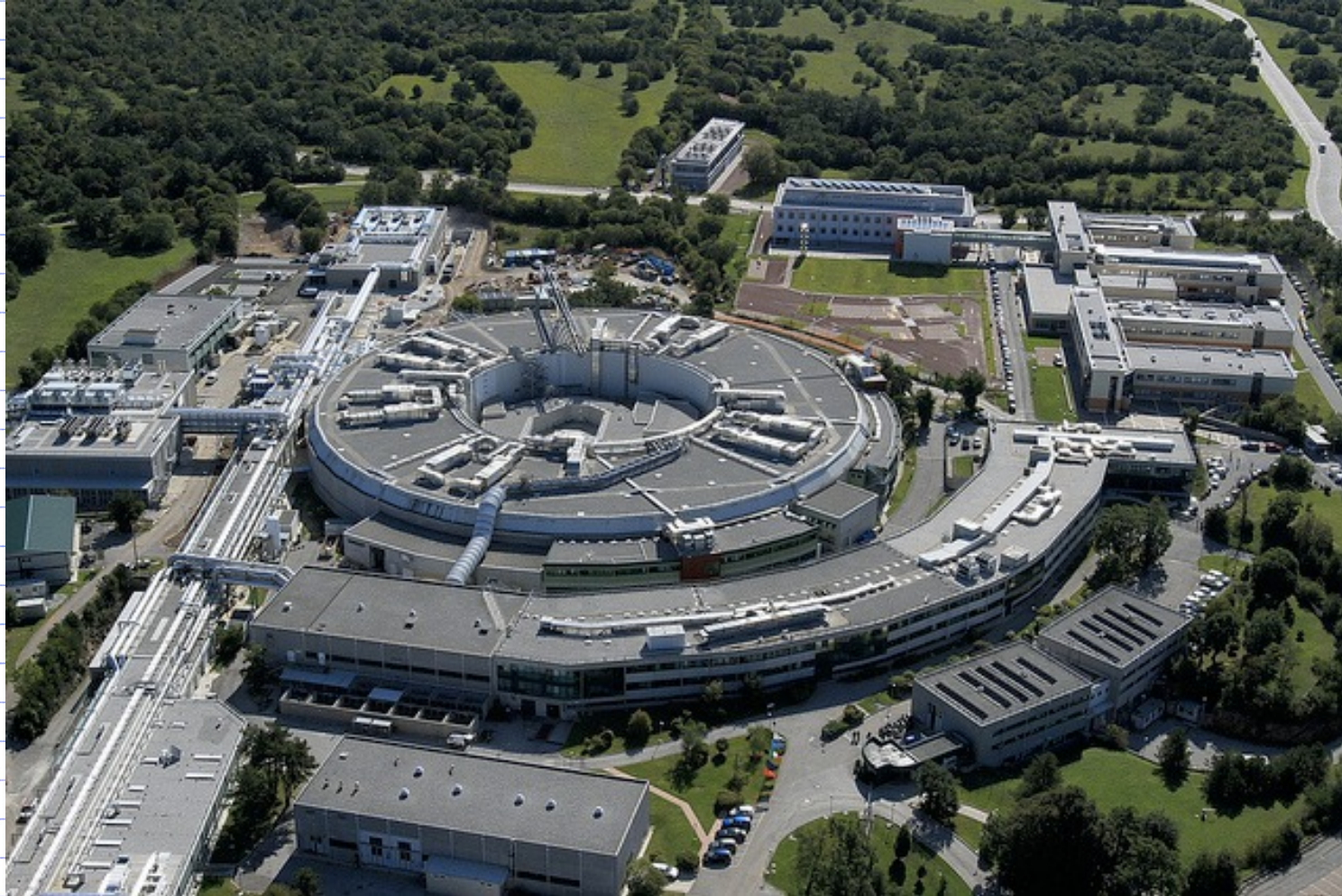
Bloch-point (BPW)

➡ Need for advanced magnetic microscopies to identify domain walls





⇒ Elettra synchrotron, Trieste, Italy







⇒ Swiss Light Source (SLS), close to Zürich

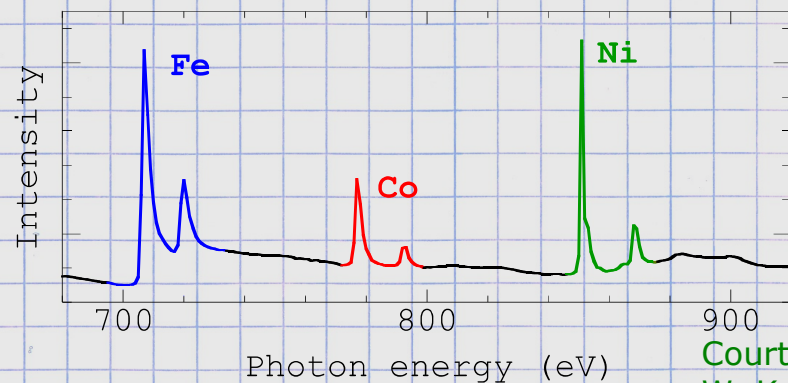




## XMCD

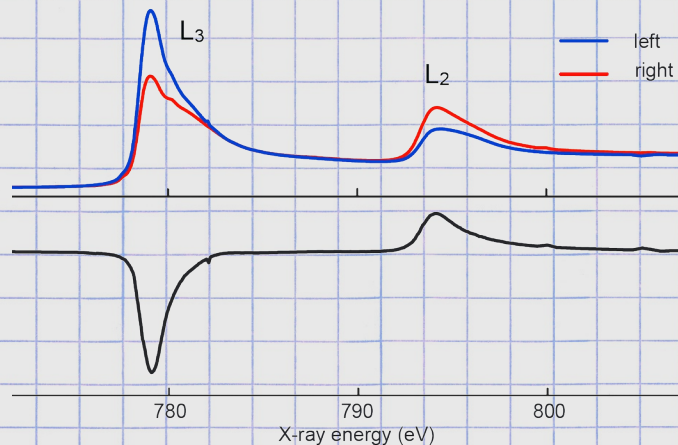
### X-ray Magnetic Circular Dichroism

⇒ Element selectivity



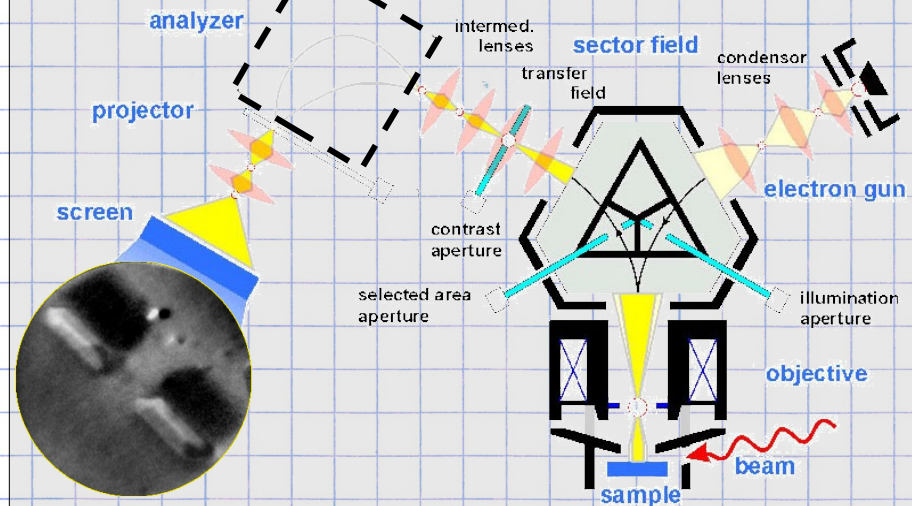
Courtesy:  
W. Kuch

⇒ Magnetic sensitivity



## PEEM

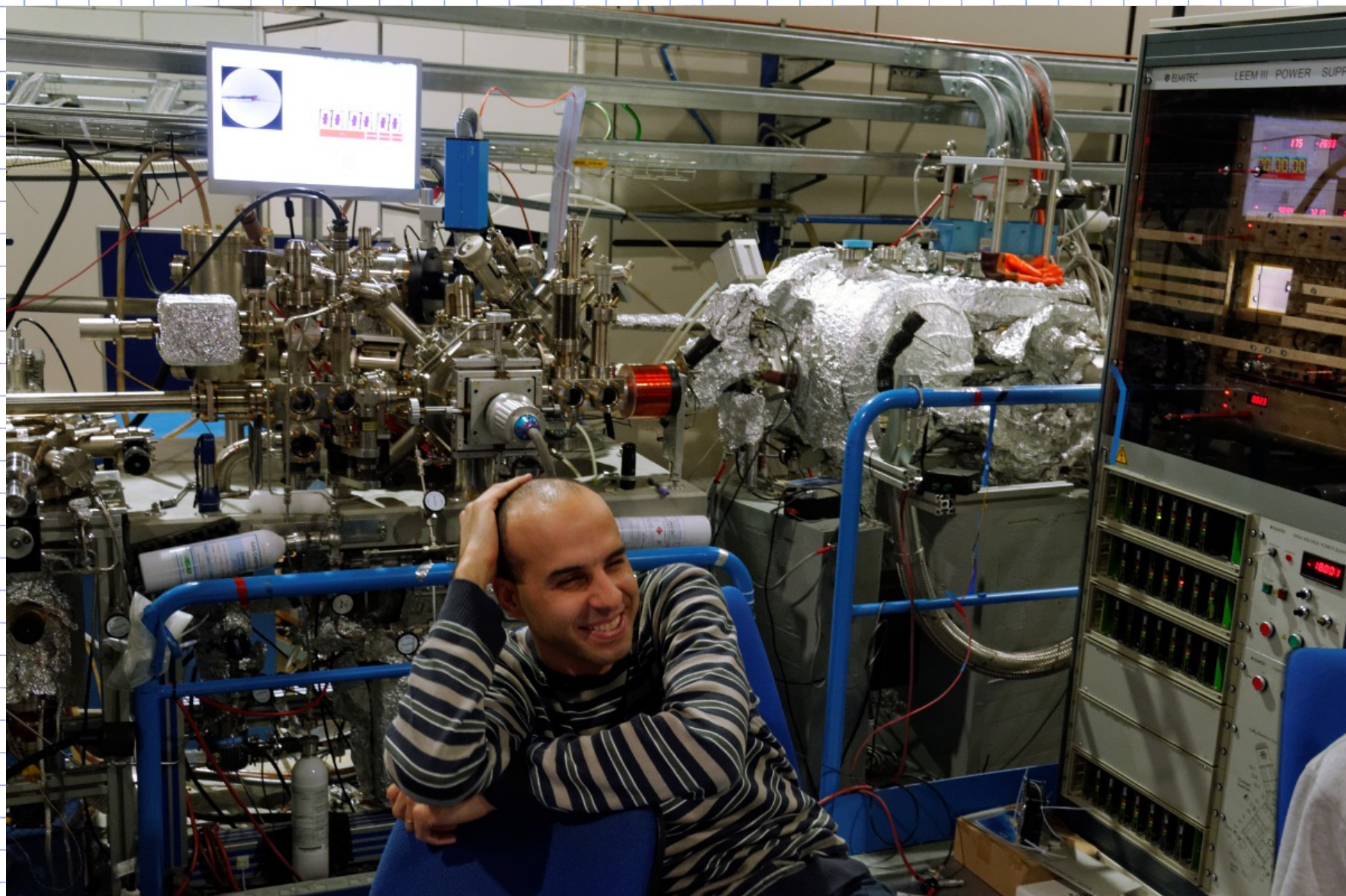
### Photo-Emission Electron Microscopy



## Features

- ⇒ Secondary electrons → surface sensitive
- ⇒ Spatial resolution : 25nm

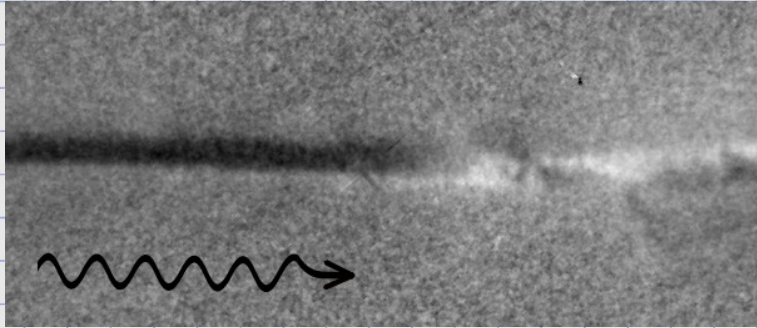




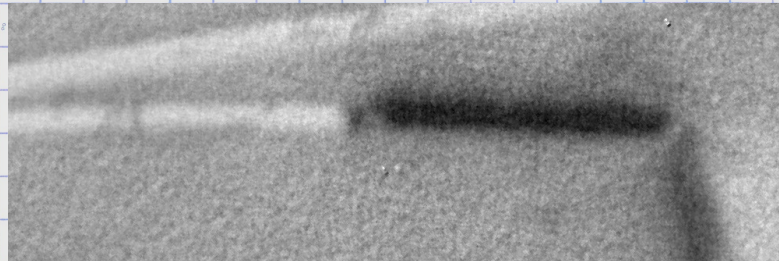
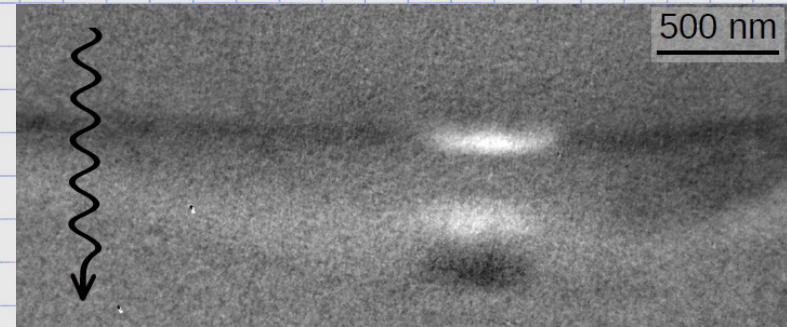


## Two examples

Beam along wire  
⇒ Locate domain walls

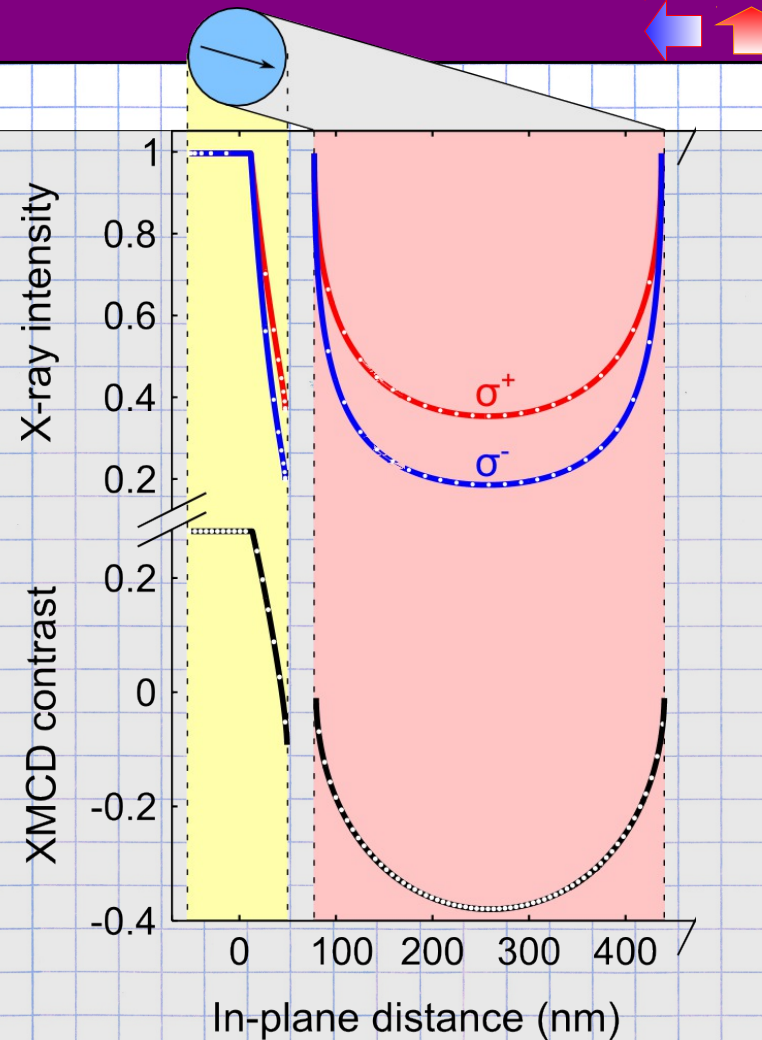
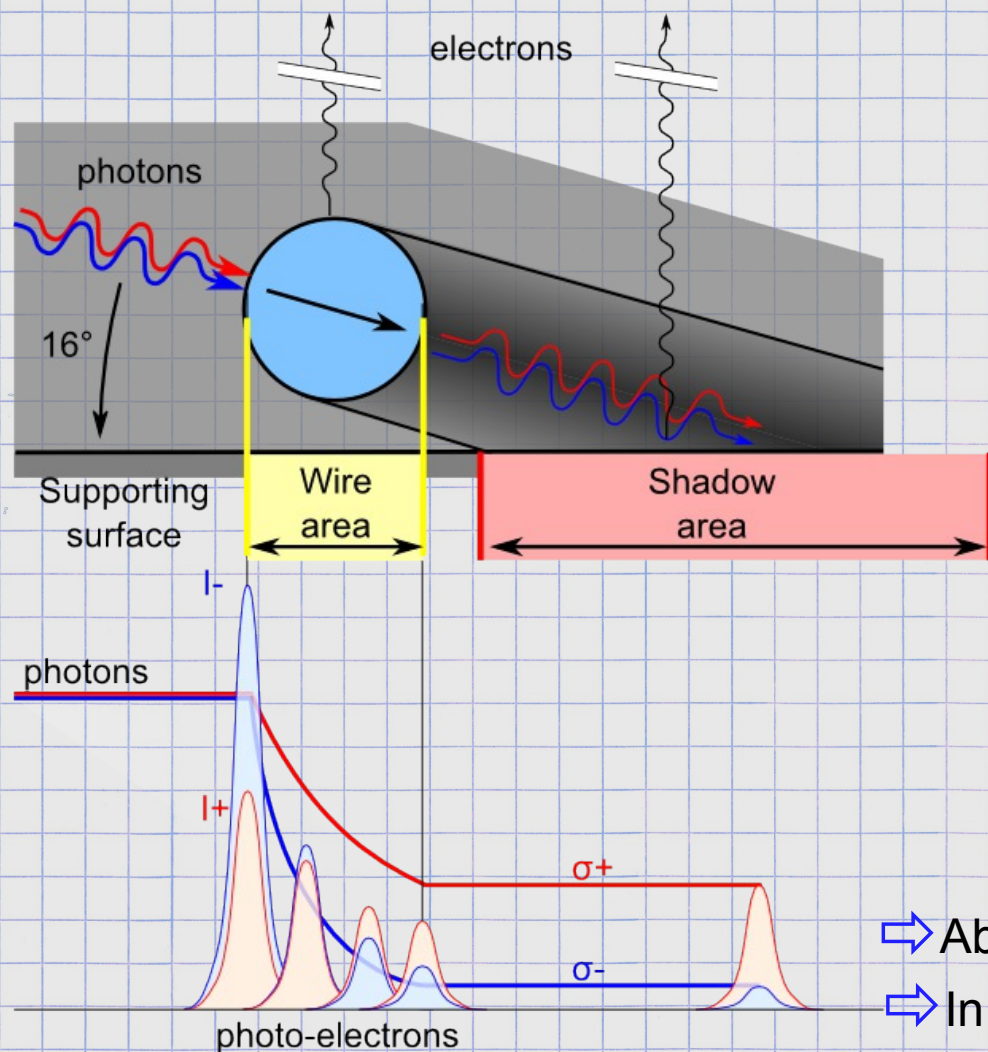


Beam across wire  
⇒ Inspect domain wall



⇒ Several non-trivial patterns  
⇒ Need for modelling

## Schematics



- ⇒ Above wire : **surface magnetization**
- ⇒ In the shadow : **volume magnetization**
- ⇒ Non-linear, even change of sign

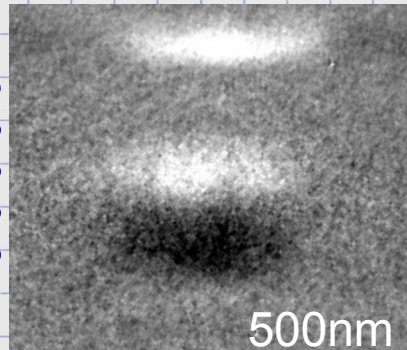


## Bloch-Point Wall (BPW)

Wire diameter : 95nm

Experiment

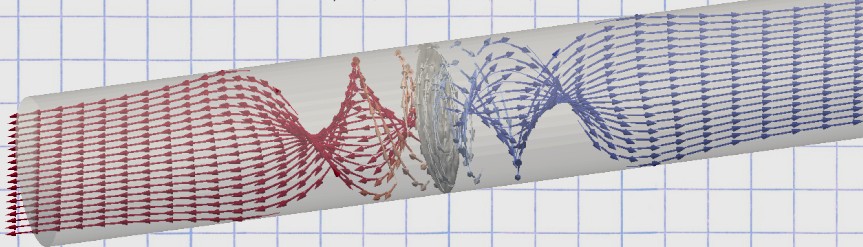
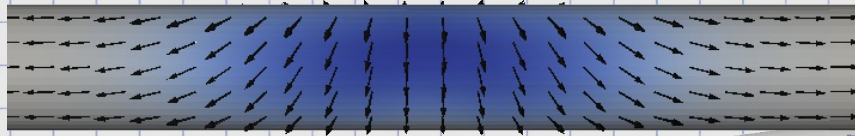
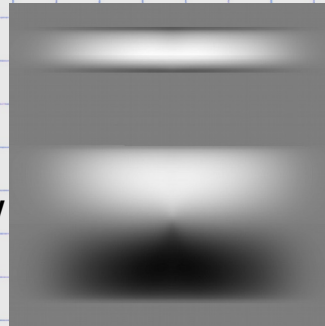
Simulation



Wire

Shadow

500nm



⇒ Orthoradial curling

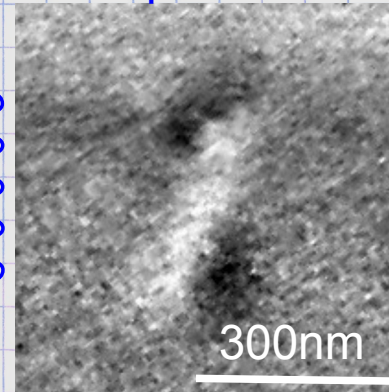
⇒ Symmetry with respect to plane perpendicular to axis

## Transverse Wall (TW)

Wire diameter : 70nm

Experiment

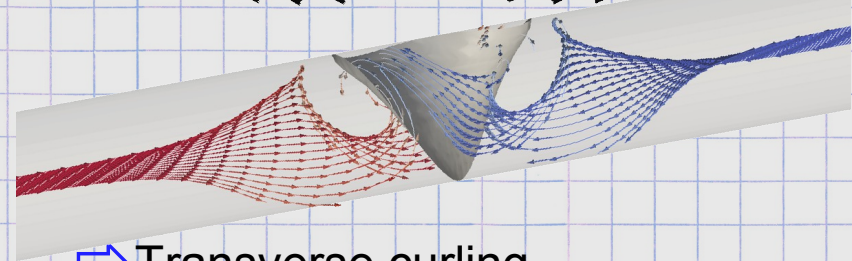
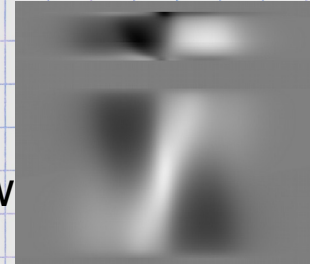
Simulation



Wire

Shadow

300nm

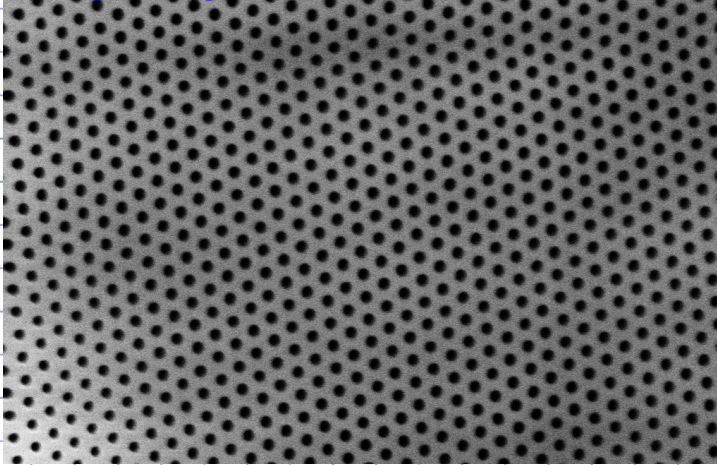


⇒ Transverse curling

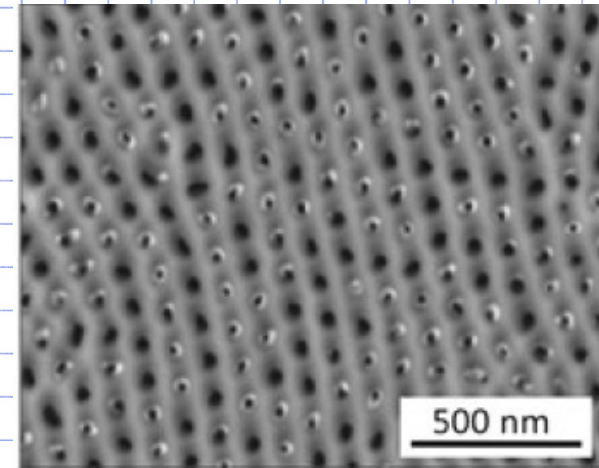
⇒ Loss of symmetry with respect to plane perpendicular to axis



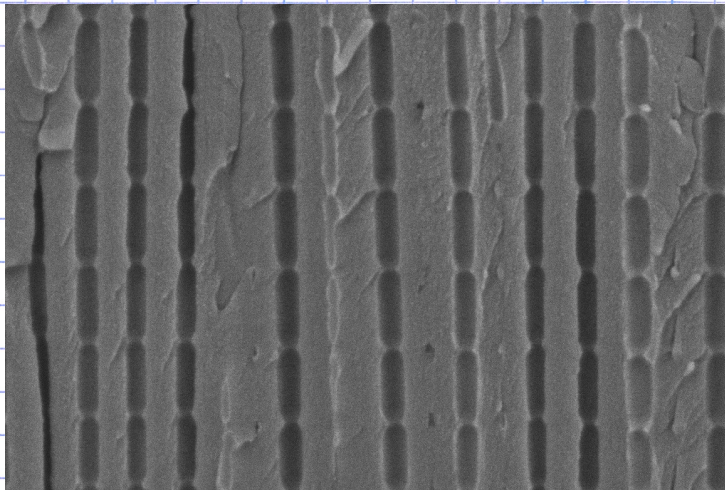
## Long-range ordered templates



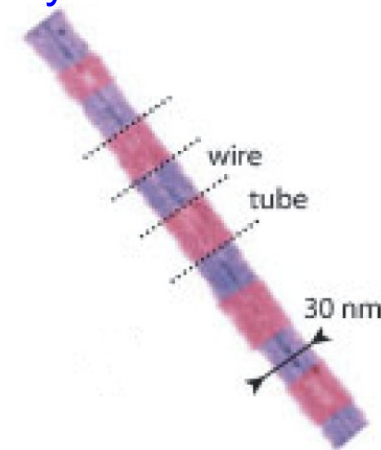
## Nanotubes



## Pre-defined bits



## Multilayered structures







## Areal density

- ⇒ Prospects for HDD :  $1 \text{ Tbit/in}^2$   
 $\approx 1.5 \times 10^{11} \text{ bit/cm}^2$
- ⇒ Pitch 100nm  $\rightarrow 10^{10} \text{ wire/cm}^2$
- ⇒ Need 100 bits/wire to overcome HDD
- ⇒ Goal 1bit/200nm  $\rightarrow 20 \mu\text{m}$

## Speed

- ⇒ Shift wire registers in parallel  
 $\rightarrow$  not a limiting factor
- ⇒ Determined by R/W (planar) device
- ⇒ Similar to 2D competitors

## Power

- ⇒ Current for spin-torque  $10^{12} \text{ A/m}^2$
- ⇒ Resistivity  $10^{-7} \Omega \cdot \text{m}$
- ⇒ Power consumption  $10 \text{ mW}$
- ⇒ Energy per bit  $10 - 100 \text{ pJ}$

## Cost per bit

- ⇒ 2D patterning  $\rightarrow$  similar to flash

## Scalability

- ⇒ 2D cost + 3D scalability  
 $\rightarrow$  cost/bit decreases
- ⇒ No limitation for 3D fabrication
- ⇒ Practical limitation for energy consumption









- ⇒ Perform experiments (or simulations, theory)
- ⇒ Develop instrumentation, codes etc.
- ⇒ Reading recent and less recent publications, books etc.
- ⇒ Go to conferences : learn and disseminate
- ⇒ Seeking funding → Grants, equipment, travel etc.
- ⇒ Do some teaching
- ⇒ Organize the lab : scientific life, technical versus scientific activity etc.

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**JEMS**  
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The European School on Magnetism (ESM) is an event organized by the European magnetism community. ESM is closely linked with its conference counterpart, the Joint European Magnetic Symposia , organized every two years as the largest European conference on Magnetism. **JEMS2013** was held in the island of Rhodes, Greece, Aug.25-30 2013. The joint JEMS and ESM actions aim at supporting European activity in magnetism, through the dissemination of knowledge and the education of young scientists.

**Latest news**

- [2013-07-02] Next ESM to be held in Cluj, Romania, Aug-Sep 2015.
- [2013-03-08] ESM 2013 held successfully in [Cargese](#) , Corsica, France (25 Feb - 8 Mar 2013) with topic: *Magnetism for Energy*.