

A flavor of Nanomagnetism and Spintronics

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<http://neel.cnrs.fr>



Local environment

Grenoble : 500 000 inhabitants with surroundings

Universities : Université Joseph Fourier (UJF) / Grenoble Institute of Technology (INP)

National Institutes : CNRS (broad topic), CEA (energy), INSERM (health) etc.

Large scale facilities : ILL (neutrons) and ESRF (synchrotron)

Fundamental research and technology (ex : Minatec, LETI, STMicroelectronics etc.)

Institut Néel

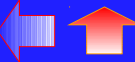
Staff : 170 scientists ; 125 technical staff ; 140 students & post-docs

3 departments : Nanosciences, low temperatures, materials & functions

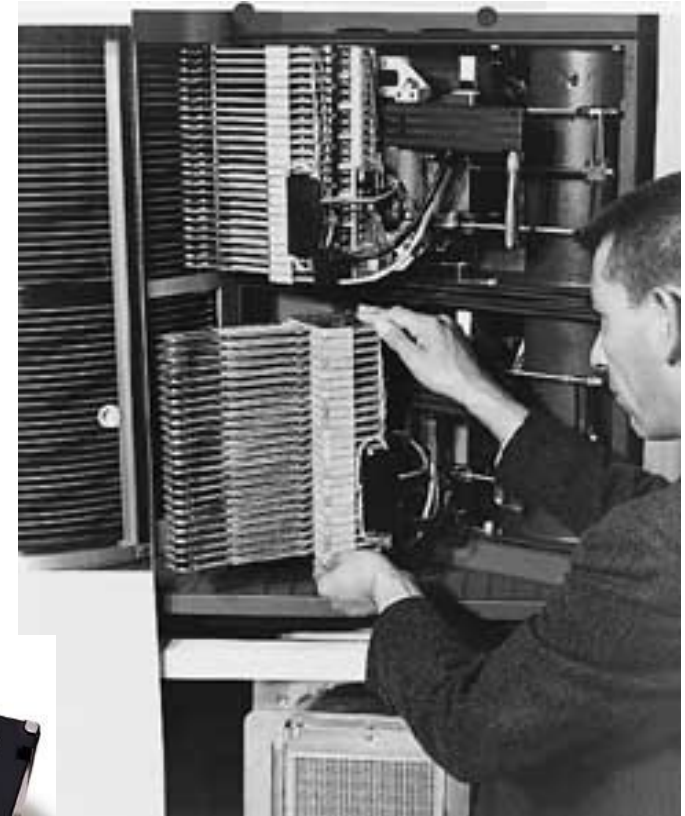
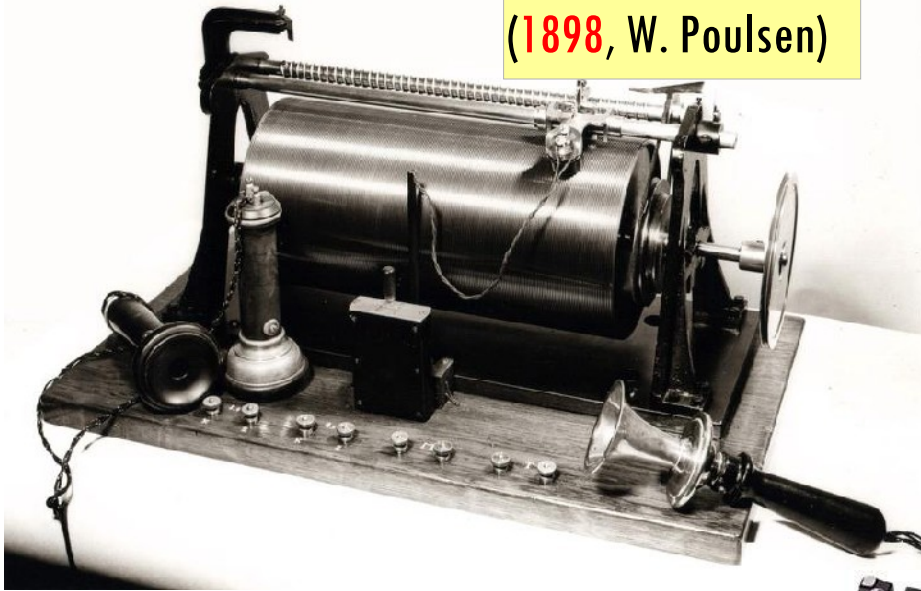
Nanosciences : 7 research teams

Micro- and NanoMagnetism team : 35 staff, including 15 full-staff scientists.

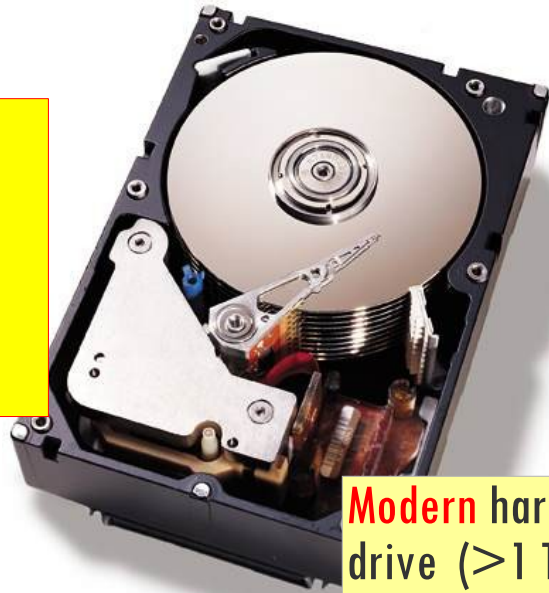




Telegraphone
(1898, W. Poulsen)



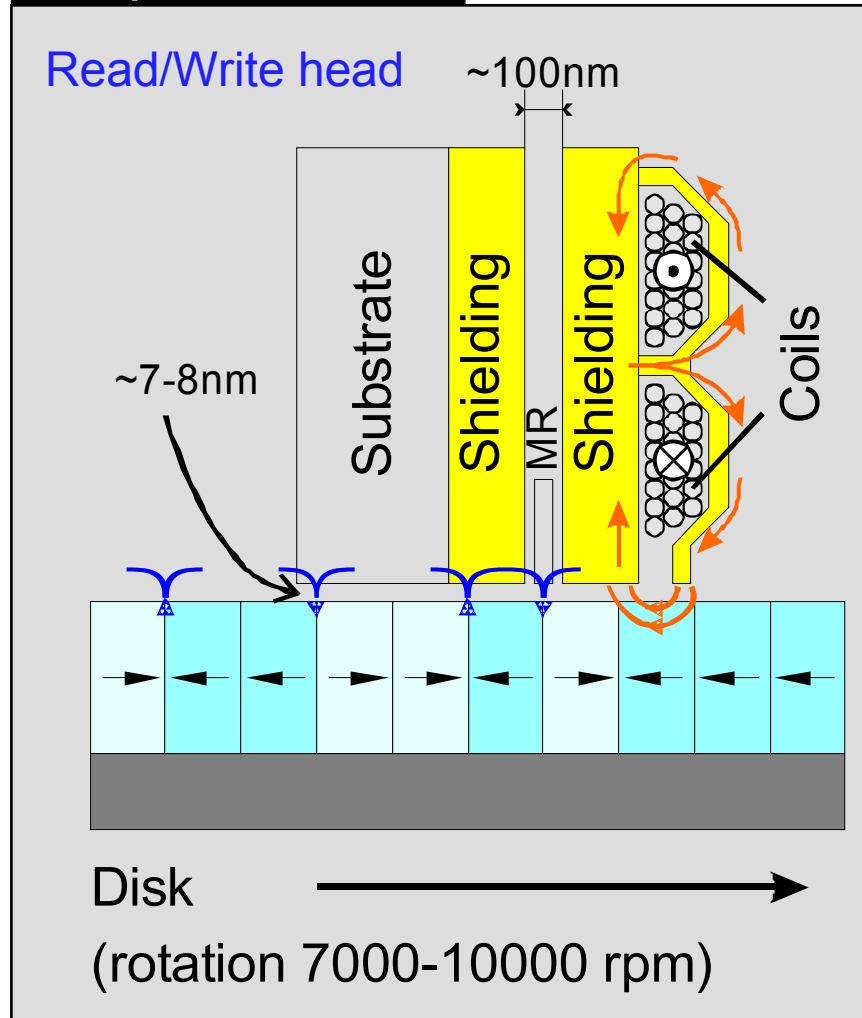
RAMAC (IBM, 1956)
2 kbit/in²
50 disks Ø 60 cm
Total 5Mbytes



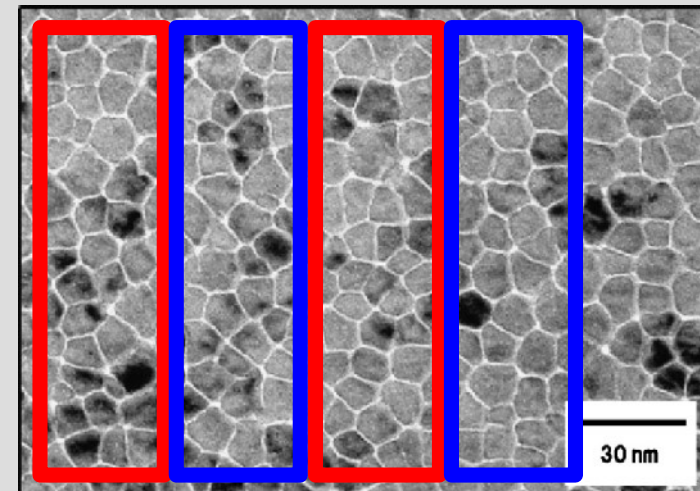
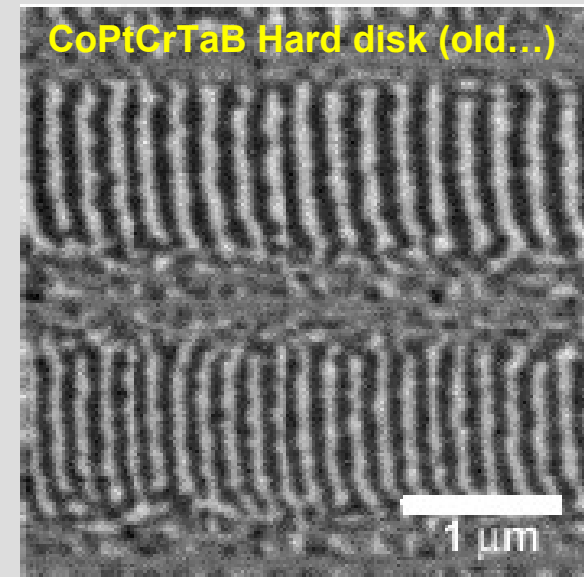
Modern hard disk
drive (>1 To)

↻ Same concept over 100 years
↻ Technological innovation?
↻ New science?

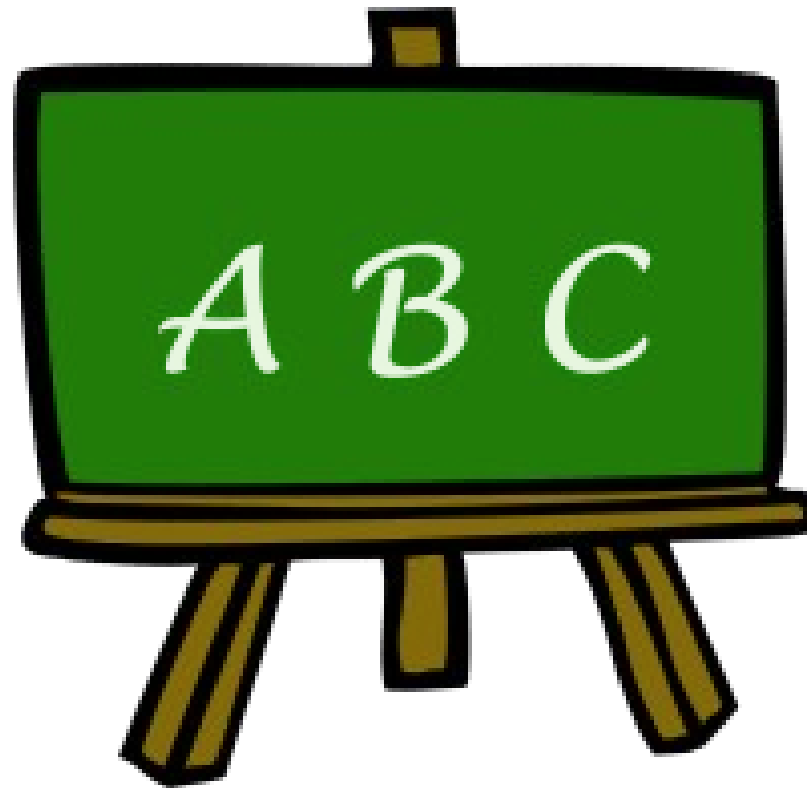
Principle of hard-disks



Magnetic bits



S. Takenoiri, J. Magn. Magn. Mater. 321, 562 (2009)





Fundamental issues for nanomagnetism

⇒ Is a small grain stable against thermal fluctuations?

$$k_B T(300 \text{ K}) \approx 4 \times 10^{-21} \text{ J} \approx 25 \text{ meV}$$

$$100 k_B T(300 \text{ K}) \approx 2.5 \text{ eV}$$



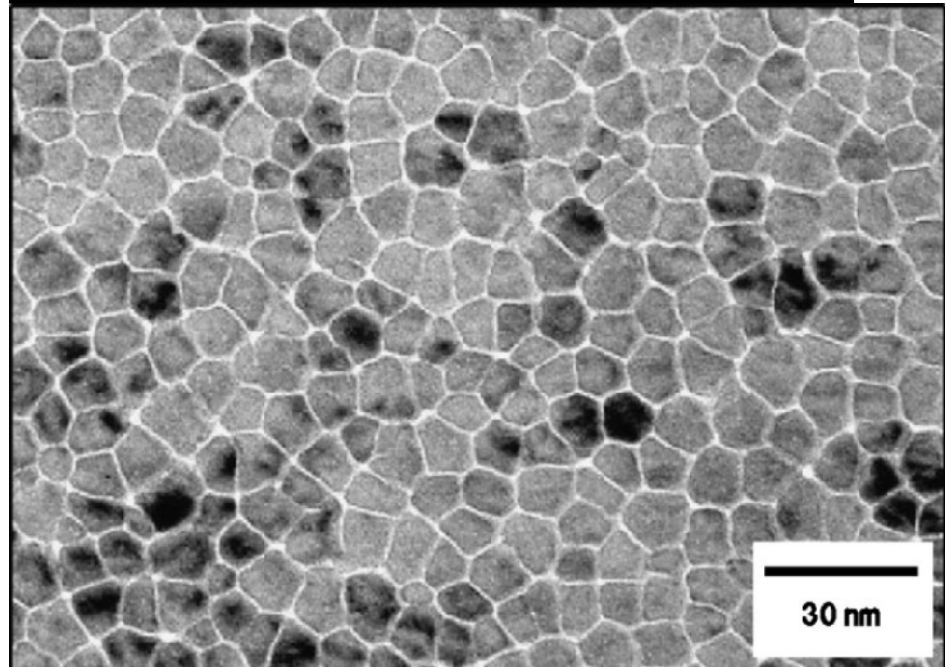
Derive from
macroscopic
arguments

⇒ Is a small grain (ferro)magnetic?



Count number of
surface atoms

Magnetic grain media of current hard disks



S. Takenori, J. Magn. Magn. Mater. 321, 562 (2009)

⇒ Decades-old (yet still modern) topic

The technological need for spin electronics

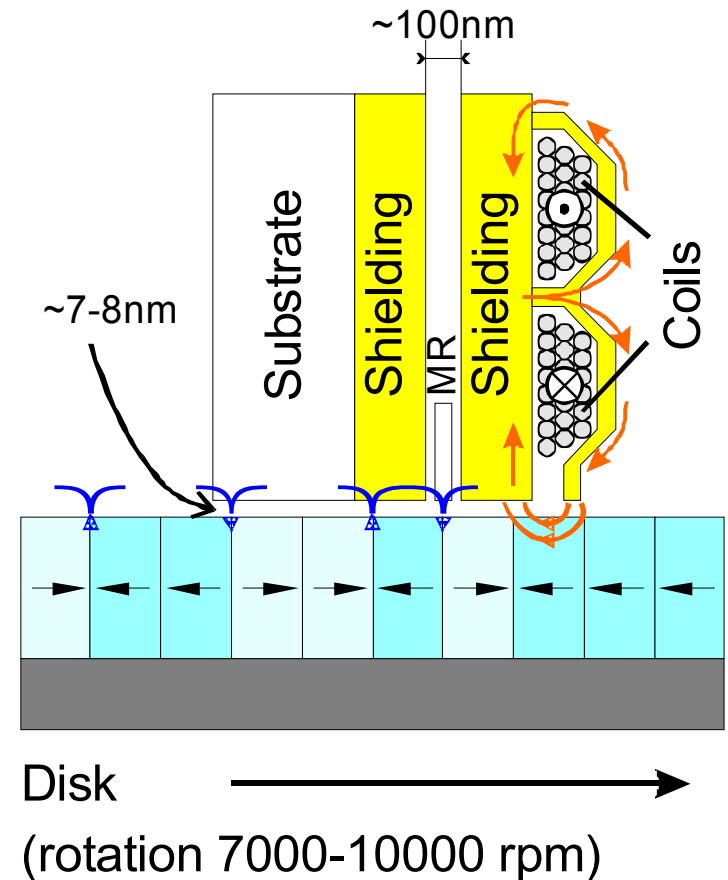
- ⇒ How to read information?
 - Convert magnetic information to electric signal
- ⇒ Field of spin electronics
 - Magneto-transport.
 - Requires nanometer length scales

⇒ Official birth: discovery of magneto-resistance

N. M. Baibich, Phys. Rev. Lett. 61, 2472 (1988)

G. Binach, Phys. Rev. B 39, 4828 (1989)

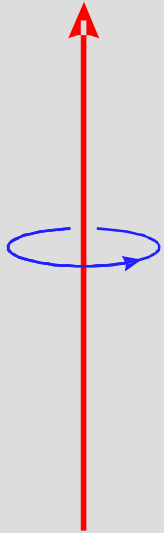
⇒ Nobel prize 2007: A. Fert & P. Grünberg



0. Motivation

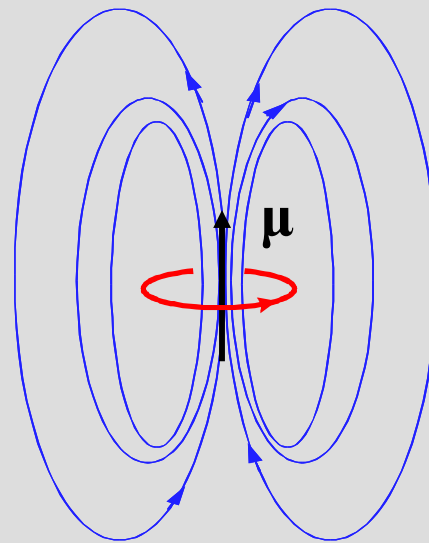
- ➔ **1. Introduction on magnetism**
- ➔ **2. Energies and length scales in magnetism**
- ➔ **3. Single-domain magnetization reversal**
- ➔ **4. Magnetostatics**
- ➔ **5. Surfaces and interfaces**

Oersted field



$$B = \frac{\mu_0 I}{2\pi r}$$

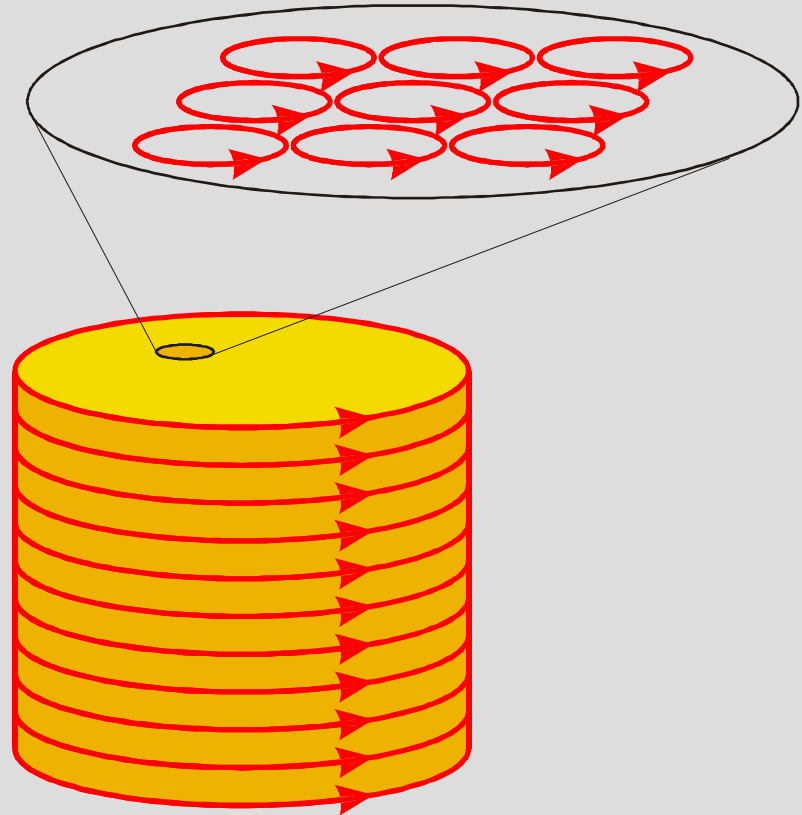
Magnetic dipole



$$B = \frac{\mu_0}{4\pi r^3} \times \left[\frac{3}{r^2} (\boldsymbol{\mu} \cdot \mathbf{r}) \mathbf{r} - \boldsymbol{\mu} \right]$$

Magnetic dipole: A.m²

Magnetic material



Magnetization: A.m⁻¹

Magnetic moment: A.m²

Manipulation of magnetic materials:

⇒ Application of a magnetic field

Zeeman energy: $E_Z = -\mu_0 \mathbf{H} \cdot \mathbf{M}_s$



Spontaneous $\neq$ **S**aturation

Spontaneous magnetization M_s

Another notation
 $J_s = \mu_0 M_s$

Remanent magnetization M_r

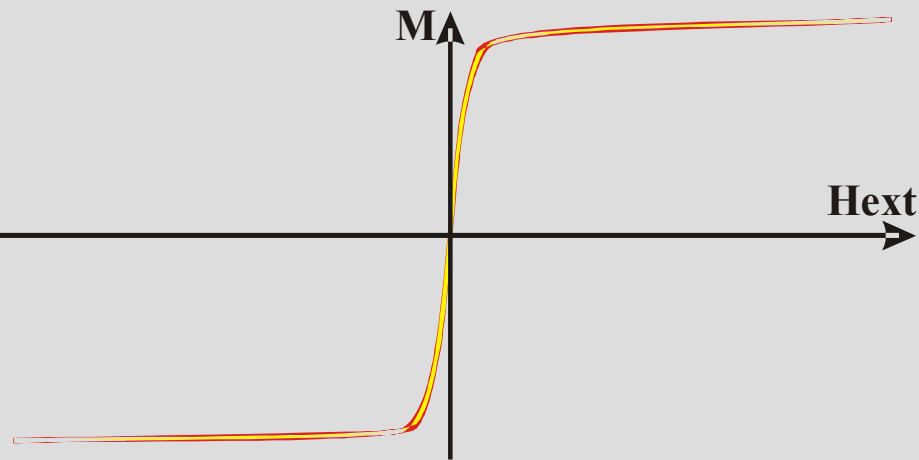
Coercive field H_c

H_{ext}

Losses

$$E = \oint \mu_0 H_{\text{ext}} dM$$

Soft materials

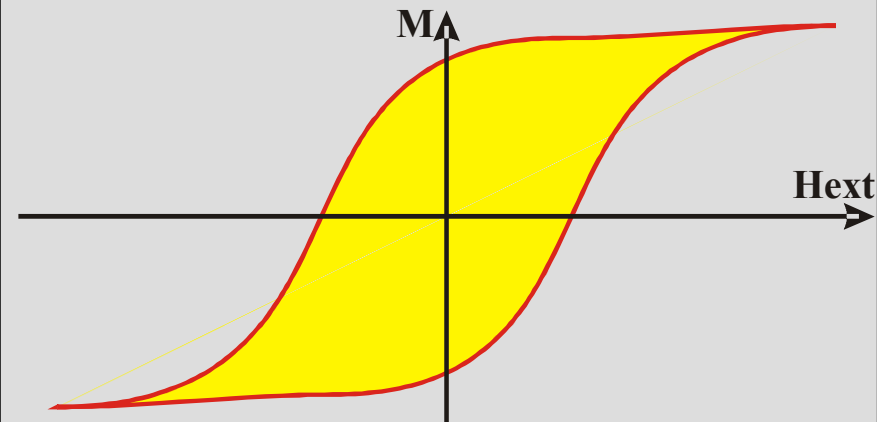


Transformers

Flux guides, sensors

Magnetic shielding

Hard materials



Permanent magnets, motors

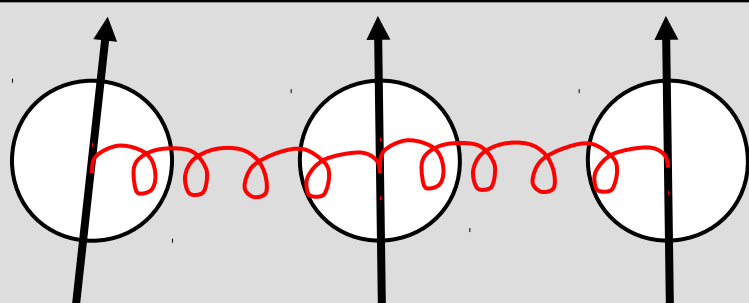
Magnetic recording



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- ➔ 1. Introduction on magnetism
- ➔ **2. Energies and length scales in magnetism**
- ➔ 3. Single-domain magnetization reversal
- ➔ 4. Magnetostatics
- ➔ 5. Surfaces and interfaces

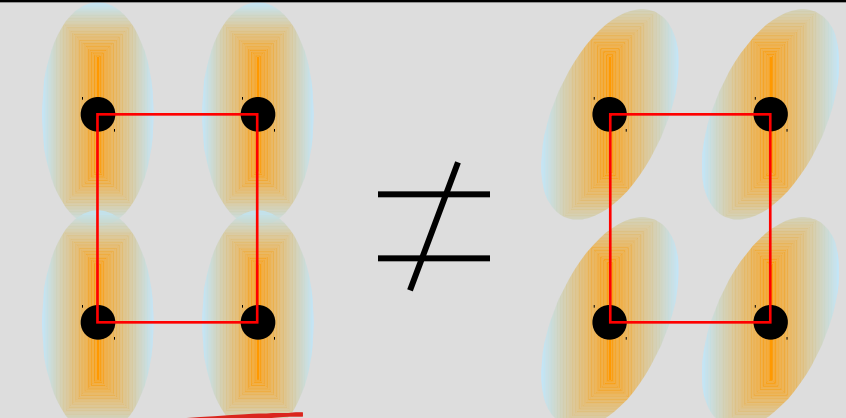
Exchange energy



$$E_{\text{Ech}} = -J_{1,2} \vec{S}_1 \cdot \vec{S}_2$$

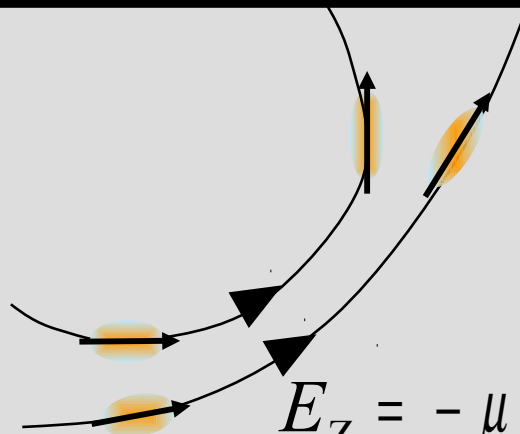
$$= A(\nabla \theta)^2$$

Magnetocrystalline anisotropy energy



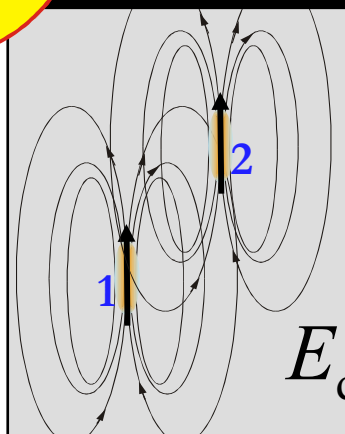
$$E_{\text{mc}} = K \sin^2(\theta)$$

Zeeman energy (enthalpy)



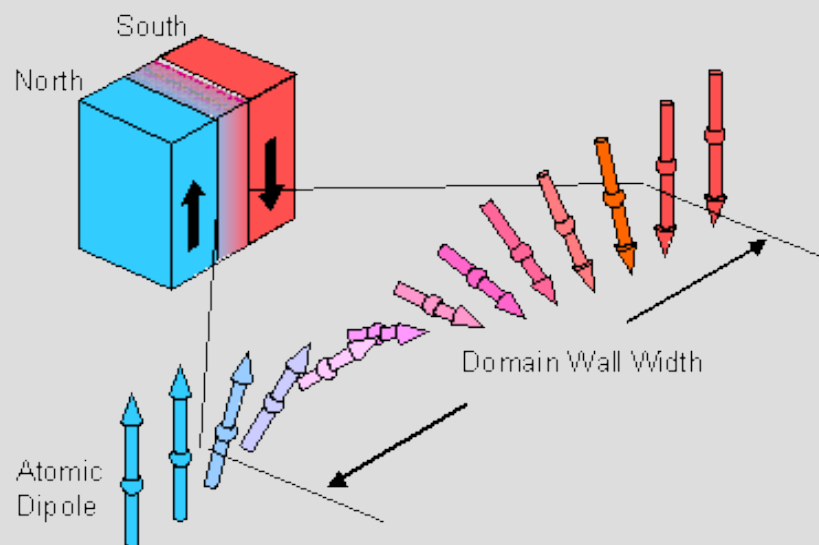
$$E_Z = -\mu_0 \vec{M}_s \cdot \vec{H}$$

Dipolar energy



$$E_d = -\frac{1}{2} \mu_0 \vec{M}_s \cdot \vec{H}_d$$

Bloch parameter



$$E = A \left(\partial_x \theta \right)^2 + K \sin^2 \theta$$

$\xrightarrow{\text{Exchange}} \text{J/m}$
 $\xrightarrow{\text{Anisotropy}} \text{J/m}^3$

Bloch parameter: $\Delta = \sqrt{A/K}$

$$\Delta \approx 1 \text{ nm} \rightarrow \Delta \geq 100 \text{ nm}$$

Hard

Soft

Exchange length

$$E = A \left(\partial_x \theta \right)^2 + K_d \sin^2 \theta$$

$\xrightarrow{\text{Exchange}} \text{J/m}$
 $\xrightarrow{\text{Dipolar energy}} \text{J/m}^3$

$$\Lambda = \sqrt{A/K_d}$$

$$= \sqrt{2A/\mu_0 M_s^2}$$

$$\Lambda \approx 3 - 10 \text{ nm}$$

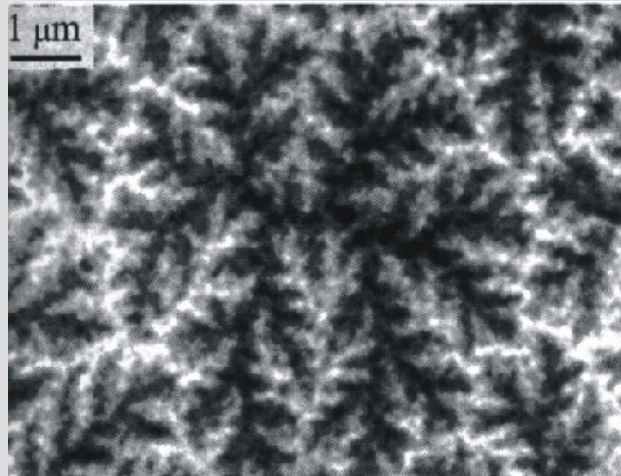
Single-domain critical size
relevant for nanoparticles
made of soft magnetic material

Notice:

Other length scales: with field etc.

Bulk material

Numerous and complex magnetic domains

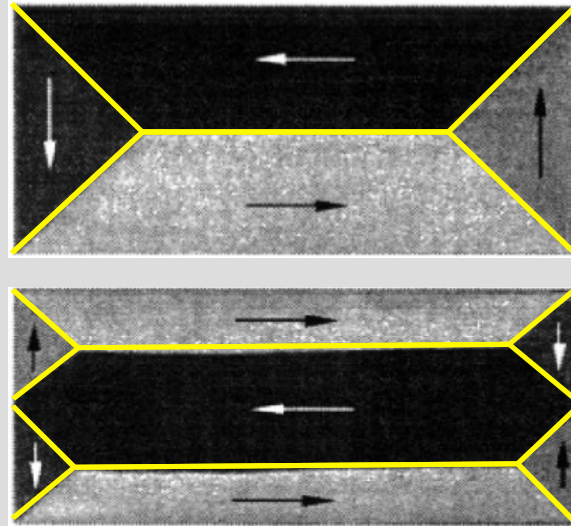


Co(1000) crystal – SEMPA

A. Hubert, *Magnetic domains*

Mesoscopic scale

Small number of domains, simple shape

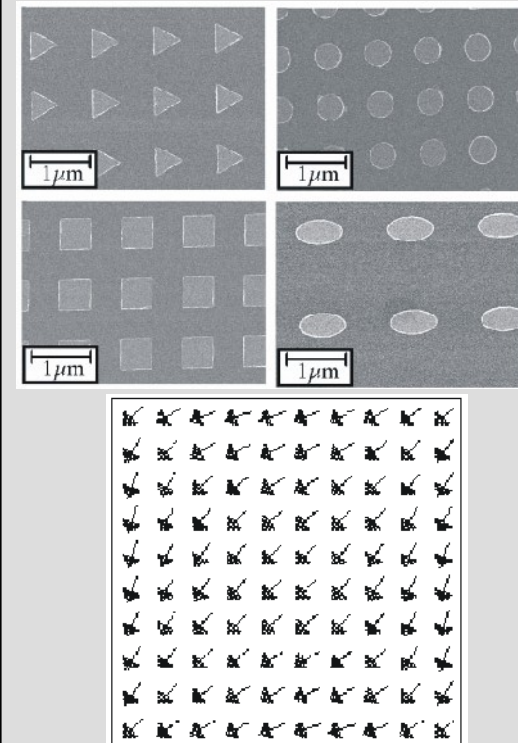


Microfabricated dots
Kerr magnetic imaging

A. Hubert, *Magnetic domains*

Nanometric scale

Magnetic single-domain



R.P. Cowburn,
J.Phys.D:Appl.Phys.33,
R1 (2000)

Nanomagnetism ~ mesoscopic magnetism

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- ➔ 4. Magnetostatics
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Framework

Approximation: $\partial_r \mathbf{m} = \mathbf{0}$ (uniform magnetization)
(strong!)

$$\mathcal{E} = EV = V [K_{\text{eff}} \sin^2 \theta - \mu_0 M_s H \cos(\theta - \theta_H)]$$

$$K_{\text{eff}} = K_{\text{mc}} + K_d$$

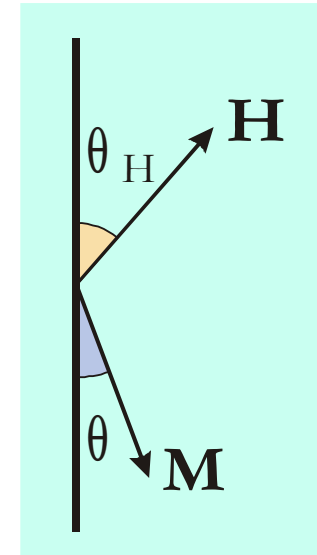
Dimensionless units:

$$e = \mathcal{E} / KV$$

$$h = H / H_a$$

$$e = \sin^2 \theta - 2h \cos(\theta - \theta_H)$$

$$H_a = 2K / \mu_0 M_s$$



L. Néel, *Compte rendu Acad. Sciences* 224, 1550 (1947)

E. C. Stoner and E. P. Wohlfarth, *Phil. Trans. Royal. Soc. London* A240, 599 (1948)

***IEEE Trans. Magn.* 27(4), 3469 (1991) : reprint**

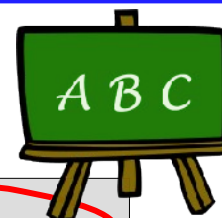
Names used

➡ Uniform rotation / magnetization reversal

➡ Coherent rotation / magnetization reversal

➡ Macrospin etc.

Example for $\theta_H = 180^\circ \longrightarrow e = \sin^2 \theta + 2h \cos \theta$



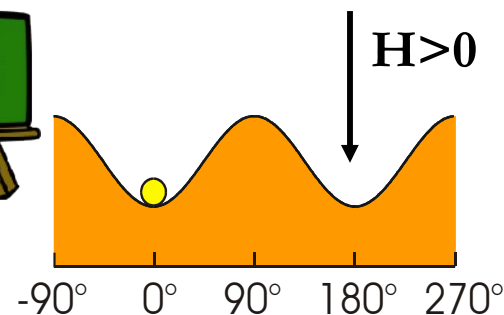
Equilibrium states

$$\partial_\theta e = 2 \sin \theta (\cos \theta - h)$$

$$\partial_\theta e = 0 \implies$$

$$\cos \theta_m = h$$

$$\theta \equiv 0 [\pi]$$



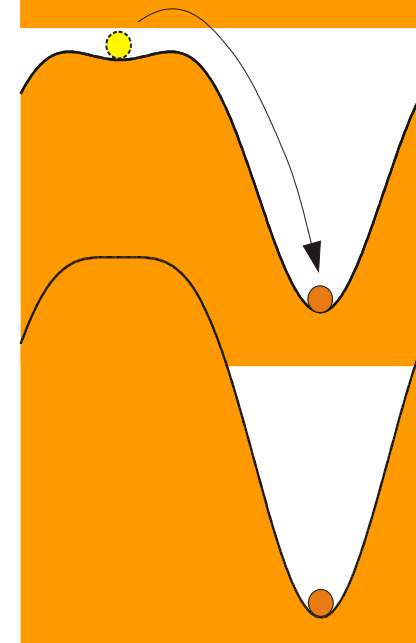
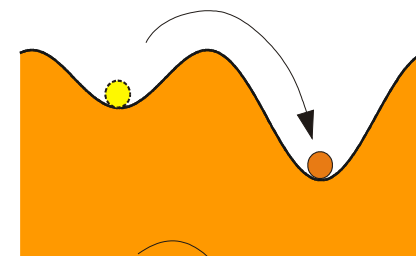
Stability

$$\begin{aligned} \partial_{\theta\theta} e &= 2 \cos 2\theta - 2h \cos \theta \\ &= 4 \cos^2 \theta - 2 - 2h \cos \theta \end{aligned}$$

$$\partial_{\theta\theta} e(0) = 2(1-h)$$

$$\partial_{\theta\theta} e(\theta_m) = 2(h^2 - 1)$$

$$\partial_{\theta\theta} e(\pi) = 2(1+h)$$



Energy barrier

$$\begin{aligned} \Delta e &= e(\theta_{\max}) - e(0) \\ &= 1 - h^2 + 2h^2 - 2h \\ &= (1-h)^2 \end{aligned}$$

Switching

$$h = 1$$

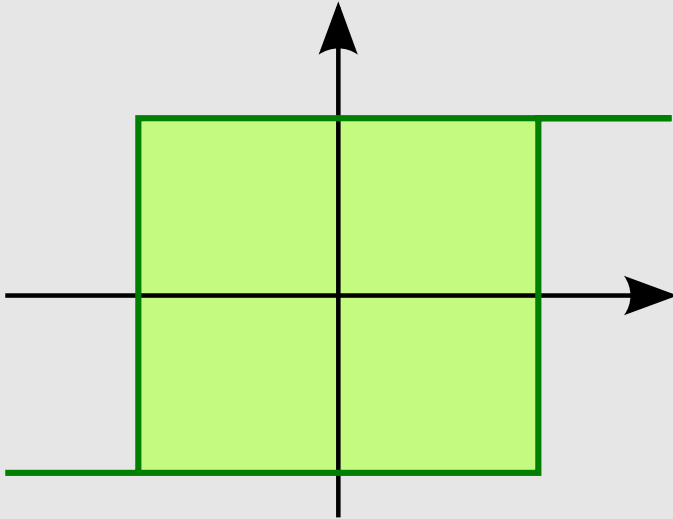
$$H = H_a = 2K / \mu_0 M_s$$



$(1-h)^\alpha$ with exponent 1.5 in general



Easy axis

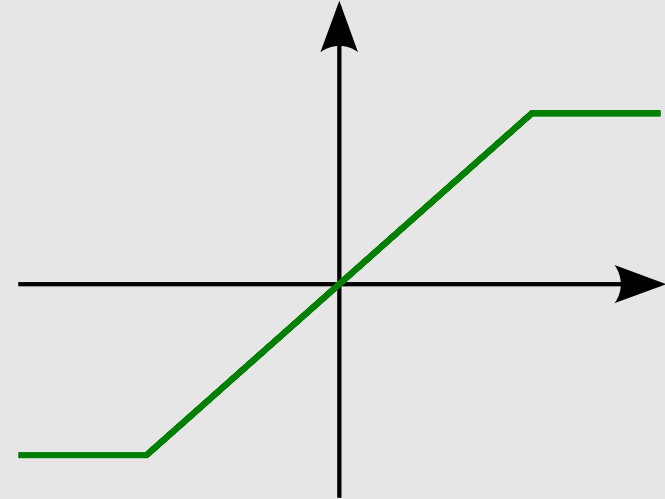


⇒ High +/- remanence

⇒ Coercivity

Memory, permanent magnet etc.

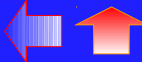
Hard axis



⇒ Reversibility

⇒ Linearity

Sensor, shielding etc.



Hitachi to Buy IBM's Hard Drive Business

By: Ken Popovich

06.05.2002 0 comments

IBM has agreed to sell its more than 45-year-old hard-drive business to Tokyo-based electronics giant Hitachi Ltd. for \$2.05 billion, the two companies announced Tuesday.

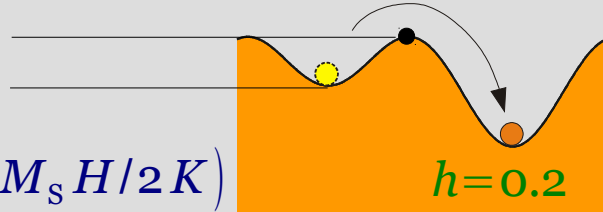
<http://www.pcmag.com/article2/0,2817,5915,00.asp>

*You see things and say « Why ? »,
but I dream things that never were and I say « Why not »*

G. B. Shaw

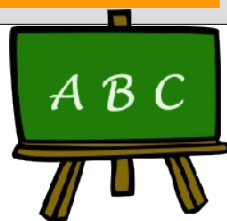
Barrier height

$$\Delta e = e(\theta_{\max}) - e(0) = (1-h)^2$$

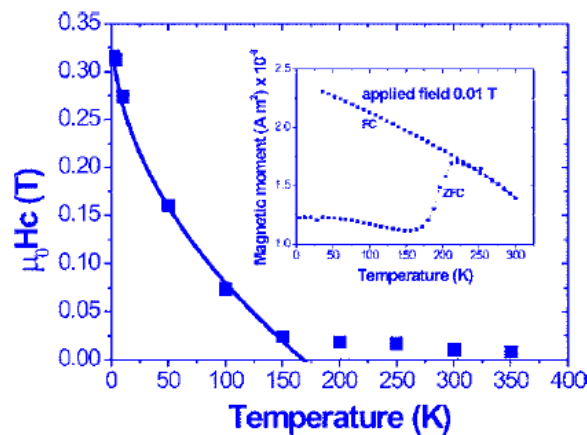


$$(h = \mu_0 M_s H / 2K)$$

$$h = 0.2$$



J. Appl. Phys. **99**, 08Q514 (2006)



Thermal activation

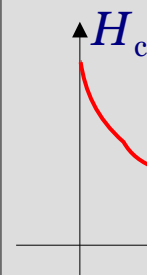
Brown, Phys.Rev.130, 1677 (1963)

$$\tau = \tau_0 \exp\left(\frac{\Delta \mathcal{E}}{k_B T}\right) \quad \Rightarrow \quad \Delta \mathcal{E} = k_B T \ln(\tau/\tau_0)$$

$$\tau_0 \approx 10^{-10} \text{ s}$$

Lab measurement : $\tau \approx 1 \text{ s} \Rightarrow \Delta \mathcal{E} \approx 25 k_B T$

$$\Rightarrow H_c = \frac{2K}{\mu_0 M_s} \left(1 - \sqrt{\frac{25 k_B T}{KV}}\right)$$



Blocking temperature

$$T_b \approx KV / 25 k_B$$

**E. F. Kneller, J. Wijn (ed.),
Handbuch der Physik XIII/2: Ferromagnetismus,
Springer, 438 (1966)**

M. P. Sharrock, J. Appl. Phys. **76,
6413-6418 (1994)**

Notice, for magnetic recording : $\tau \approx 10^9 \text{ s}$

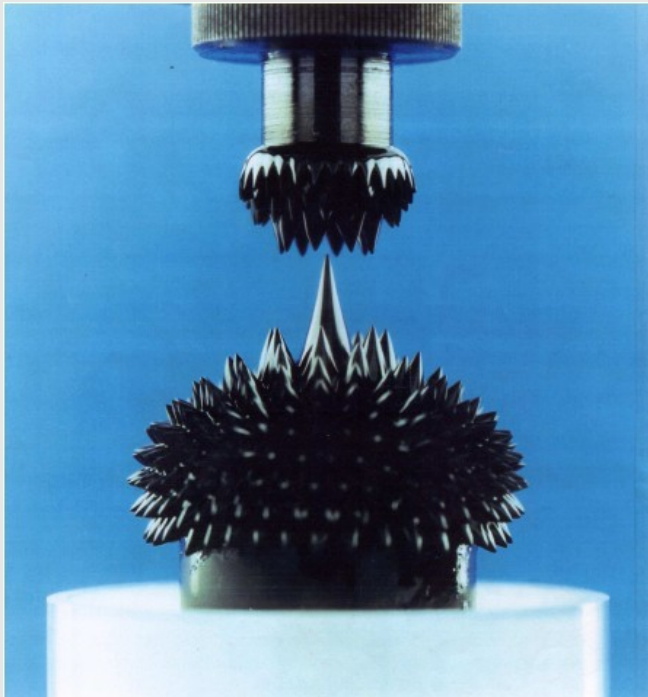
$$KV_b \approx 40 - 60 k_B T$$



Ferrofluids

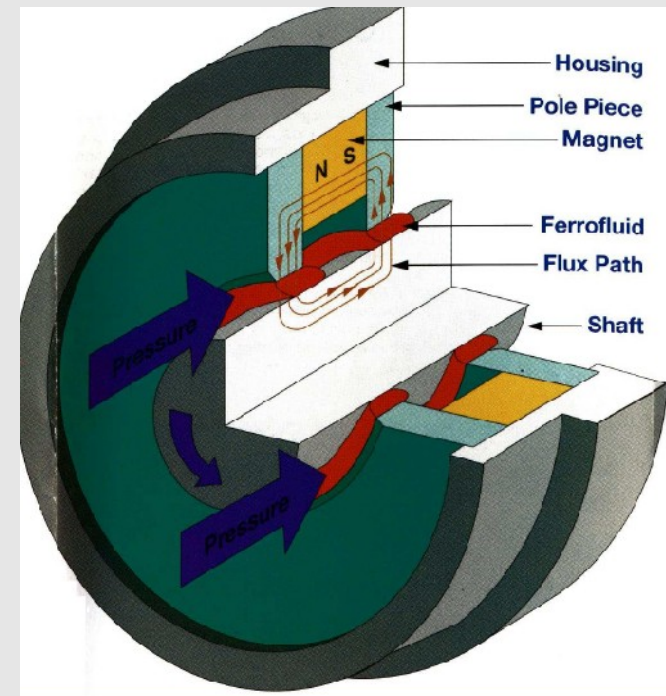
⇒ Principle

Surfactant-coated nanoparticles,
preferably superparamagnetic
→ Avoid agglomeration of the particles
→ Fluid and polarizable



⇒ Example of use

Seals for rotating parts



**R. E. Rosensweig, Magnetic fluid seals,
US patent 3,260,584 (1971)**

<http://esm.neel.cnrs.fr/2007-cluj/slides/vekas-slides.pdf>

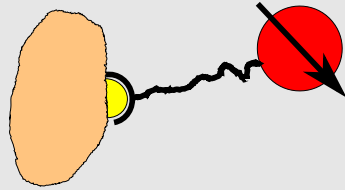


Health and biology

Beads = coated nanoparticles,
preferably superparamagnetic
→ Avoid agglomeration of the particles

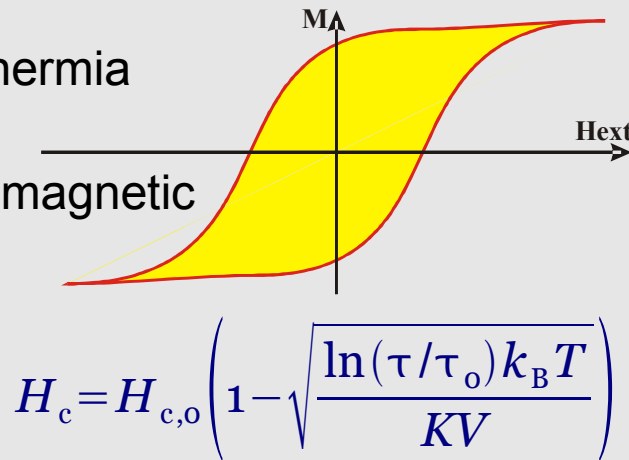
⇒ Cell sorting

$$\mathbf{F} = \nabla \mu \cdot \mathbf{B}$$

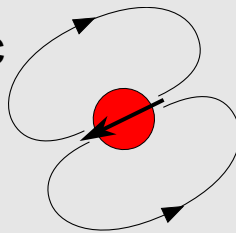


⇒ Hyperthermia

Use ac magnetic
field



⇒ Contrast agent in Magnetic
Resonance Imaging (MRI)



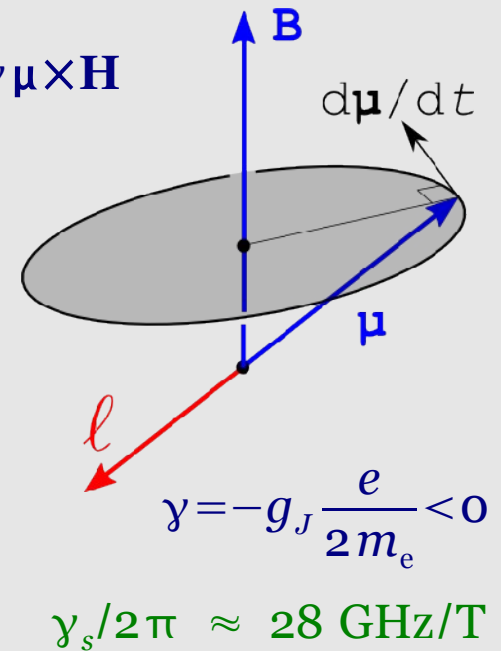
RAM (radar absorbing materials)

⇒ Principle

Absorbs energy at a well-defined
frequency (ferromagnetic
resonance)

$$\Rightarrow \frac{d\ell}{dt} = \Gamma = \mu_0 \mu \times \mathbf{H} = \mu_0 \gamma \ell \times \mathbf{H}$$

$$\Rightarrow \frac{d\mu}{dt} = \mu_0 \gamma \mu \times \mathbf{H}$$





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- ➔ 3. Single-domain magnetization reversal
- ➔ 4. **Magnetostatics**
- ➔ 5. Surfaces and interfaces



Density of dipolar energy

$$E_d(\mathbf{r}) = -\frac{1}{2} \mu_0 \mathbf{M}(\mathbf{r}) \cdot \mathbf{H}_d(\mathbf{r})$$

By definition $\text{div}(\mathbf{H}_d) = -\text{div}(\mathbf{M})$. As $\text{curl}(\mathbf{H}_d) = \mathbf{0}$ we have (analogy with electrostatics):

$$\mathbf{H}_d(\mathbf{r}) = -M_s \iiint_{\text{space}} \frac{\text{div}[\mathbf{m}(\mathbf{r}')] \cdot (\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^3 r'$$

Notation

$$\mathbf{M}(\mathbf{r}) = M_s m_i(\mathbf{r}) \mathbf{u}_i$$

$$\rho(\mathbf{r}) = -M_s \text{div}[\mathbf{m}(\mathbf{r})] \quad \text{volume density of magnetic charges}$$

To lift the divergence arising at sample boundaries:

$$\mathbf{H}_d(\mathbf{r}) = M_s \left(- \iiint_{\text{space}} \frac{\text{div}[\mathbf{m}(\mathbf{r}')] \cdot (\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^3 r' + \iint_{\text{sample}} \frac{[\mathbf{m}(\mathbf{r}') \cdot \mathbf{n}(\mathbf{r}')] \cdot (\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 r' \right)$$

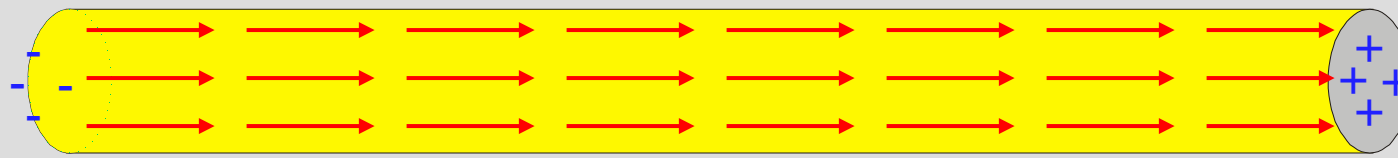
$$\sigma(\mathbf{r}) = M_s \mathbf{m}(\mathbf{r}) \cdot \mathbf{n}(\mathbf{r}) \quad \text{surface density of magnetic charges,}$$

where $\mathbf{n}(\mathbf{r})$ is the outgoing unit vector at boundaries

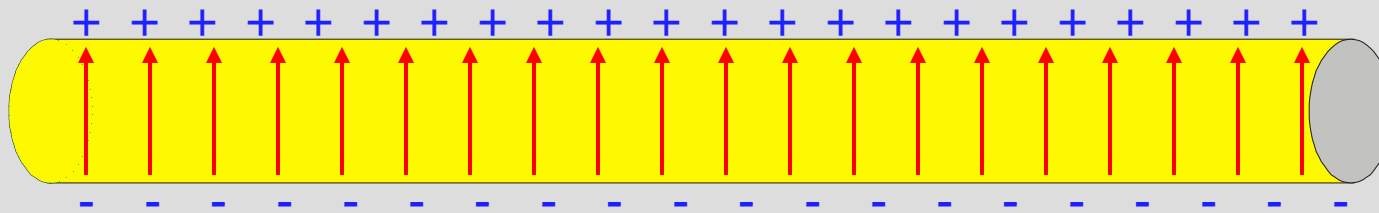
$$\mathcal{E} = -\frac{1}{2}\mu_0 \iiint_{\text{sample}} \mathbf{M} \cdot \mathbf{H}_d \cdot dV = \frac{1}{2}\mu_0 \iiint_{\text{space}} \mathbf{H}_d^2 \cdot dV$$

⇒ $\mathcal{E}$ is always positive

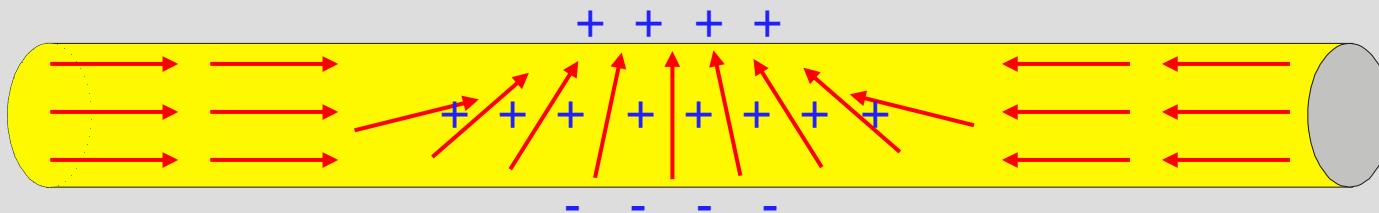
Examples of magnetic charges



Notice: no charges and $\mathcal{E}=0$ for infinite cylinder



Charges on surfaces



Surface and volume charges



⇒ Magnetization will tend to align parallel to long axis of samples

Hypothesis

Uniform magnetization $\mathbf{M}(\mathbf{r}) = M_s m_i \mathbf{u}_i$ (strong assumption!)

Demagnetizing coefficients

$$\langle \mathbf{H}_d(\mathbf{r}) \rangle = -M_s \overline{\mathbf{N}} \cdot \mathbf{m}$$

$$\mathcal{E}_d = K_d N_{ij} m_i m_j = K_d {}^t \mathbf{m} \cdot \overline{\mathbf{N}} \cdot \mathbf{m}$$

$\mathbf{N}$ is a positive second-order tensor

...and can be defined and diagonalized for any sample shape



$$\mathbf{N} = \begin{pmatrix} N_x & 0 & 0 \\ 0 & N_y & 0 \\ 0 & 0 & N_z \end{pmatrix}$$

$$\mathcal{E}_d = K_d (N_x m_x^2 + N_y m_y^2 + N_z m_z^2)$$

$$\langle H_{d,i}(\mathbf{r}) \rangle = -M_s N_i \quad \leftarrow \text{Valid along main axes only!}$$

$$N_x + N_y + N_z = 1$$

What with ellipsoids???

➡ Requires $\mathbf{H}_d(\mathbf{r})$ is uniform. Satisfied only in volumes limited by polynomial surfaces of order 2 or less: slabs, cylinders, ellipsoids etc.

J. C. Maxwell, Clarendon 2, 66-73 (1872)

Ellipsoids

$$N_x = \frac{1}{2} abc \int_0^\infty \left[(a^2 + \eta) \sqrt{(a^2 + \eta)(b^2 + \eta)(c^2 + \eta)} \right]^{-1} d\eta$$

General ellipsoid:
main axes (a,c,c)

$$N_x = \frac{\alpha^2}{1 - \alpha^2} \left[\frac{1}{\sqrt{1 - \alpha^2}} \operatorname{Asinh} \left(\frac{\sqrt{1 - \alpha^2}}{\alpha} \right) - 1 \right]$$

For prolate revolution ellipsoid:
(a,c,c) with $\alpha = c/a < 1$

$$N_x = \frac{\alpha^2}{\alpha^2 - 1} \left[1 - \frac{1}{\sqrt{\alpha^2 - 1}} \operatorname{Asin} \left(\frac{\sqrt{\alpha^2 - 1}}{\alpha} \right) \right]$$

For oblate revolution ellipsoid:
(a,c,c) with $\alpha = c/a > 1$

$$N_y = N_z = \frac{1}{2} (1 - N_x)$$

Cylinders

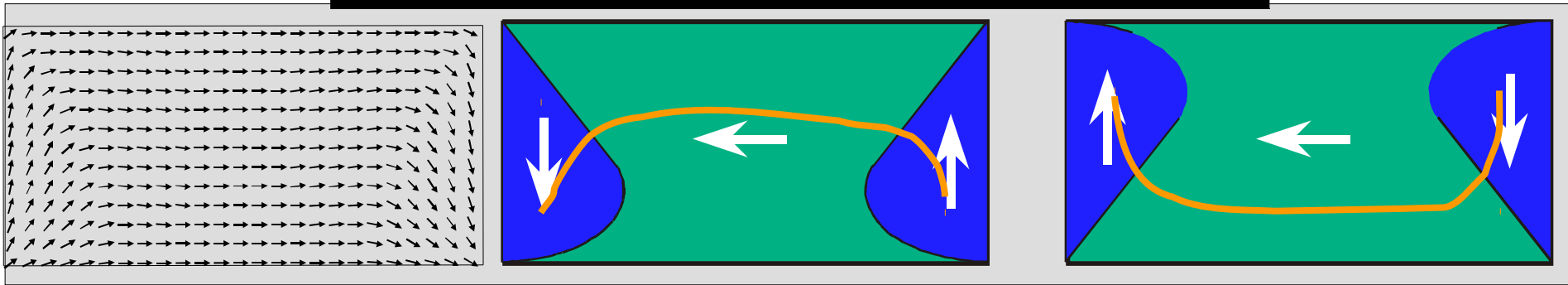
$$N_x = 0; \quad N_y = c/(b + c); \quad N_z = b/(b + c) \quad \text{For a cylinder along } x$$

J. A. Osborn, Phys. Rev. 67, 351 (1945).

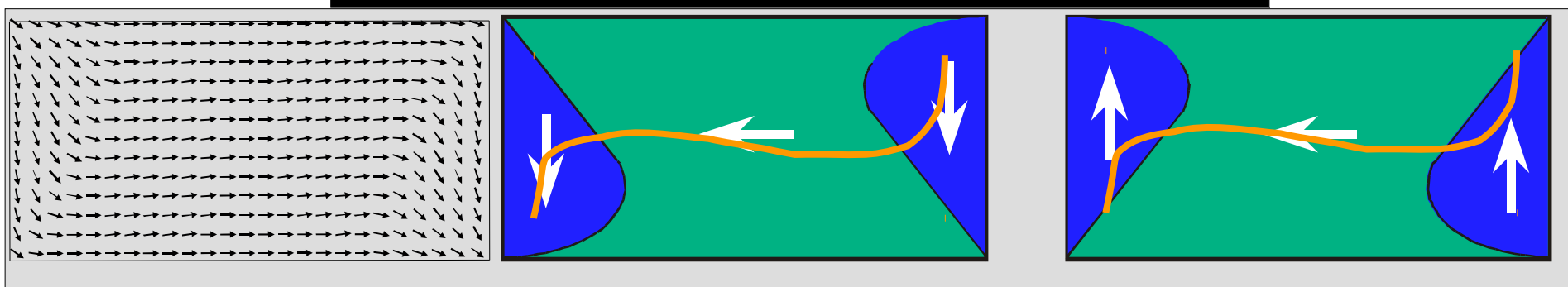
For prisms, see: **A. Aharoni, J. Appl. Phys. 83, 3432 (1998)**

More general forms, FFT approach: **M. Beleggia et al., J. Magn. Magn. Mater. 263, L1-9 (2003)**

'C' state

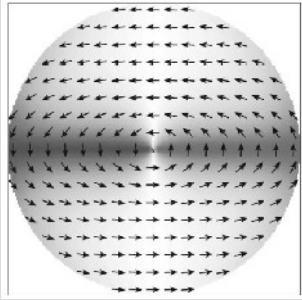


'S' state



↪ At least 8 nearly-equivalent ground-states for a rectangular dot
↪ Numerical simulation becomes important

Magnetic vortex



P.-O. Jubert & R. Allenspach,
PRB 70, 144402/1-5 (2004)

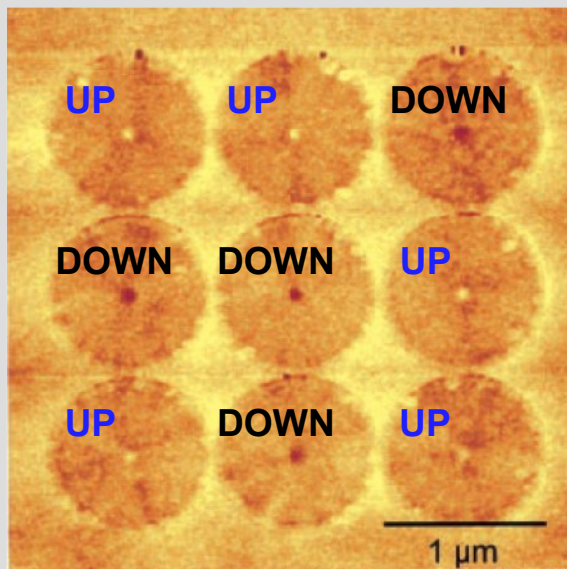


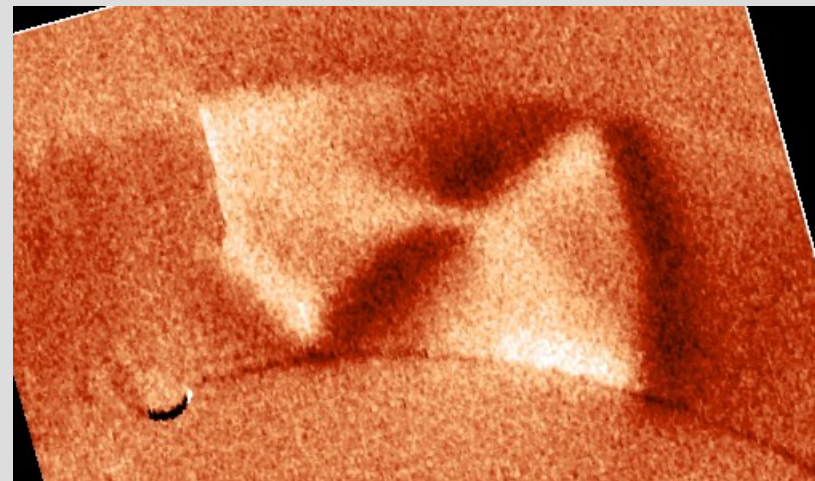
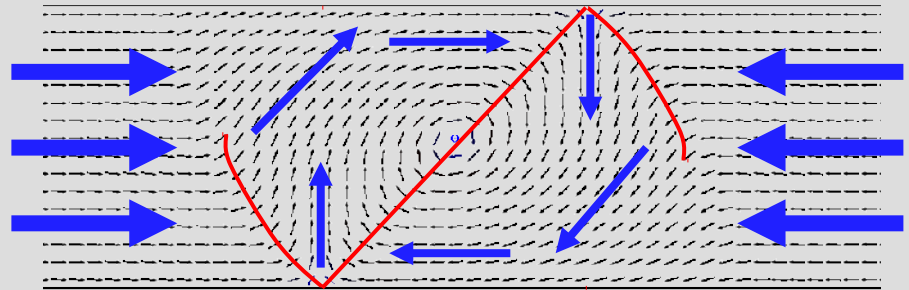
Fig. 2. MFM image of an array of permalloy dots 1 μm in diameter and 50 nm thick.

T. Shinjo et al., *Science* 289, 930 (2000)

T. Okuno et al., *JMMM*240, 1 (2002)

Magnetic domain wall

Thick and large stripes



500-nm wide, 15nm FeNi thick stripes

Basics of precessional switching

Magnetization dynamics:

Landau-Lifshitz-Gilbert equation:

$$\frac{d\mathbf{M}}{dt} = -\gamma_0 [\mathbf{M} \times \mathbf{H}_{eff}] + \frac{\alpha}{M_s} \left[\mathbf{M} \times \frac{d\mathbf{M}}{dt} \right]$$

γ_0 Gyromagnetic factor

$$\gamma_0 = \mu_0 \gamma \quad \gamma = \frac{gq}{2m}$$

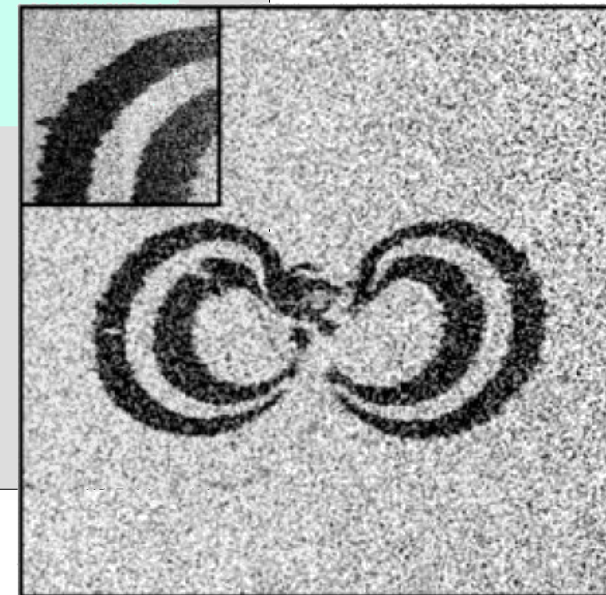
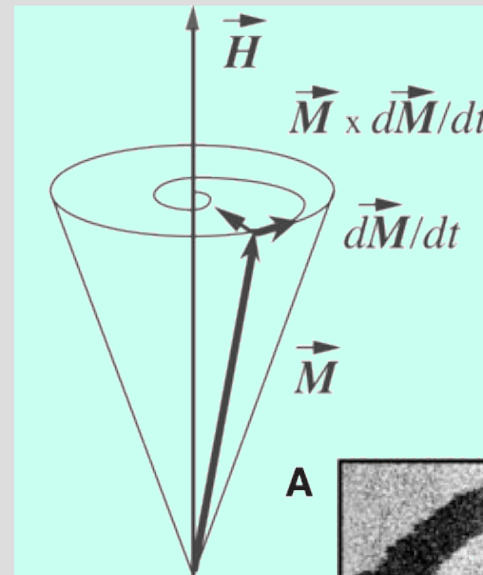
$$\gamma / 2\pi = 28 \text{ GHz/T}$$

$\mathbf{H}_{eff}$ Effective field
(including applied)

$$\mu_0 \mathbf{H}_{eff} = - \frac{\partial \mathbf{E}_{mag}}{\partial \mathbf{M}}$$

α Damping coefficient ($10^{-3} > 10^{-1}$)

Démonstration: 1999



150 μm

C. Back et al., Science 285, 864 (1999)

Precessional trajectories using energy conservation

(1) $E = \frac{1}{2} \mu_0 M_s^2 N_z m_z^2 - K m_x^2 - \mu_0 M_s H m_y$ In-plane uniaxial anisotropy

(2) $m_x^2 + m_y^2 + m_z^2 = 1$

Starting condition: $m_x = 1$

(1) $\Rightarrow e = \frac{1}{2} N_z m_z^2 - h_K m_x^2 - h m_y$

Using (2) $\Rightarrow$

$$m_x^2 = 1 - \frac{2h}{N_z + h_K} m_y - \frac{N_z}{N_z + h_K} m_y^2$$

Can be rewritten:

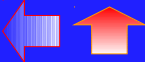
$$m_x^2 + \frac{(m_y + h/N_z)^2}{1 + h_K/N_z} = 1 + \frac{h^2}{N_z(N_z + h_K)}$$

Using (2) $\Rightarrow$

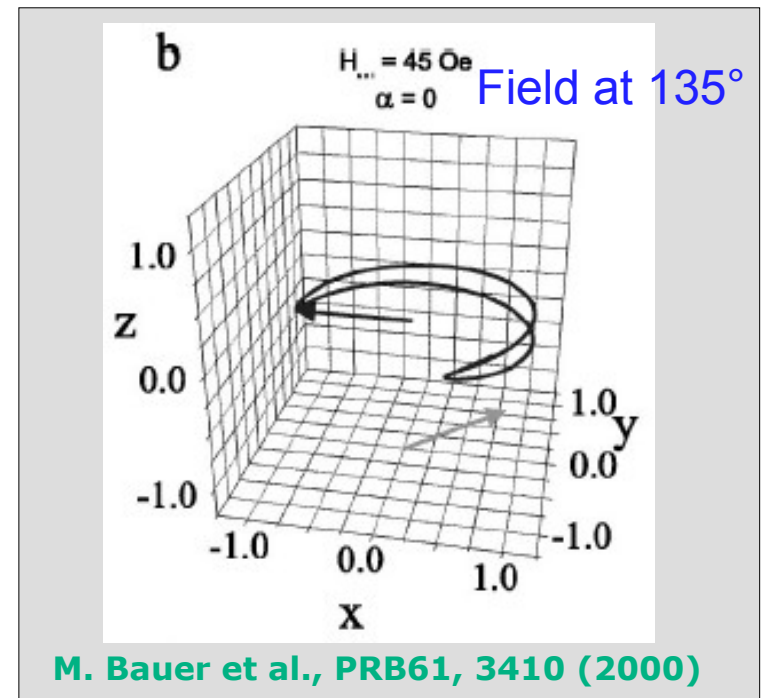
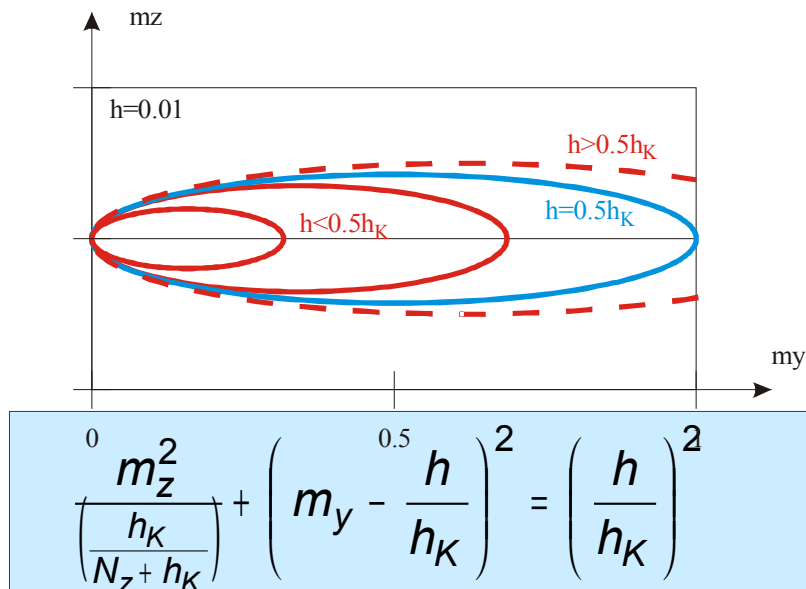
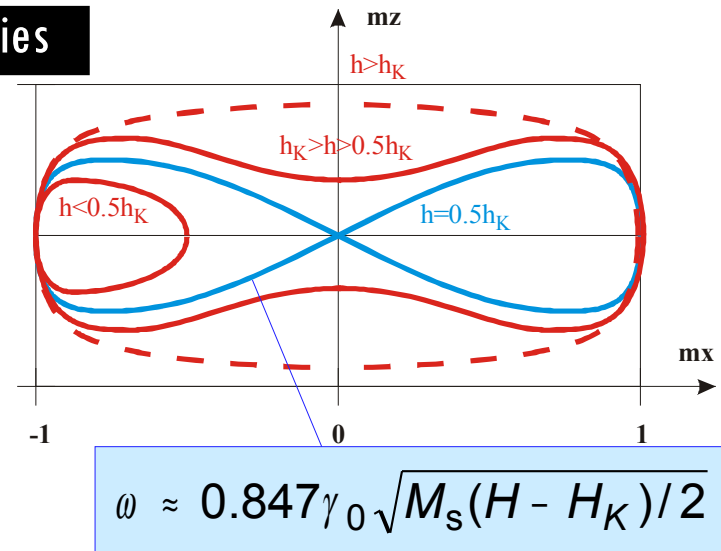
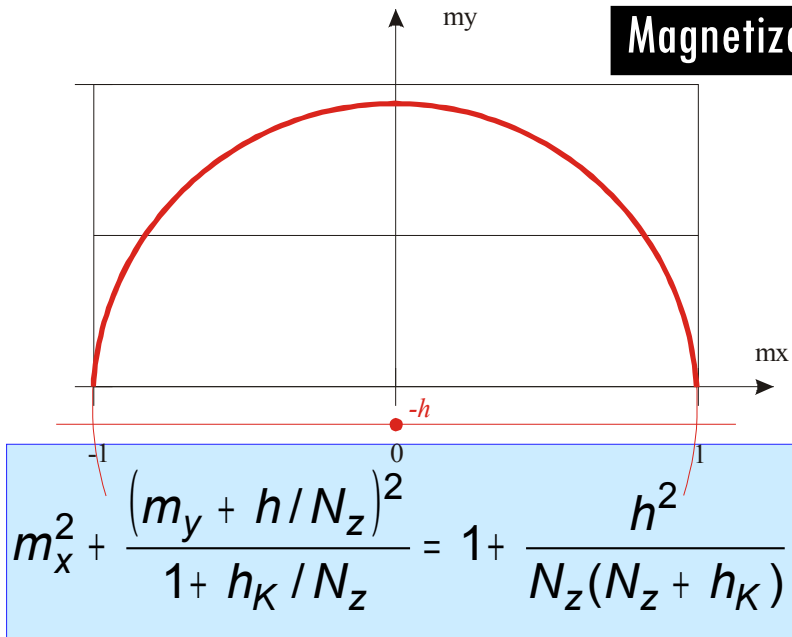
$$m_z^2 = \frac{2h}{N_z + h_K} m_y - \frac{h_K}{N_z + h_K} m_y^2$$

Can be rewritten:

$$\left(\frac{m_z^2}{\frac{h_K}{N_z + h_K}} \right) + \left(m_y - \frac{h}{h_K} \right)^2 = \left(\frac{h}{h_K} \right)^2$$



Magnetization trajectories



0. Motivation

- ➔ 1. Introduction on magnetism
- ➔ 2. Energies and length scales in magnetism
- ➔ 3. Single-domain magnetization reversal
- ➔ 4. Magnetostatics
- ➔ 5. Surfaces and interfaces

Probing surface magnetization

Surface techniques at 0K

- Mossbauer with probe layers

Plot $m(t)$ at 0K:

- Magnetometry
- XMCD

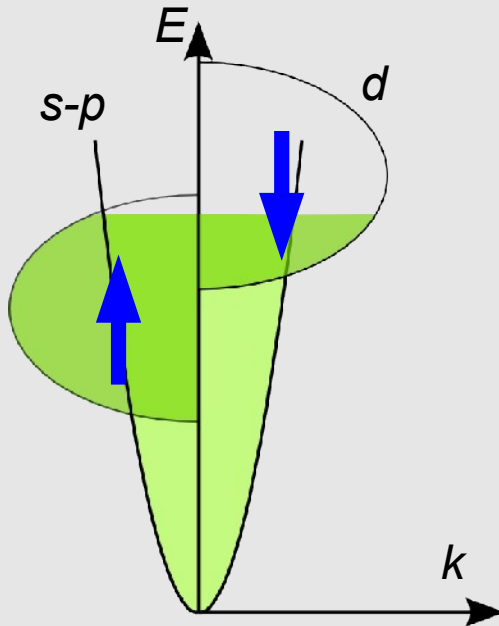
Some results

- Fe/W(110) : 0.14ML(+0.35 μ_B)
- UHV/Fe(110); Ag/Fe(110): 0.26ML(+0.65 μ_B)
- Cu/Ni(111): -0.5ML
- Overlayers: Pd/Ni(111)/Re(0001)

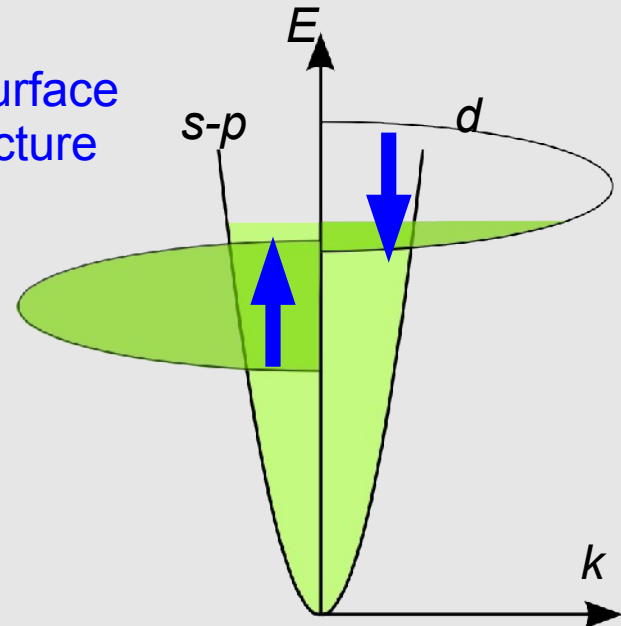
(Too) simple picture: band narrowing at surfaces

Enhanced moment at surfaces

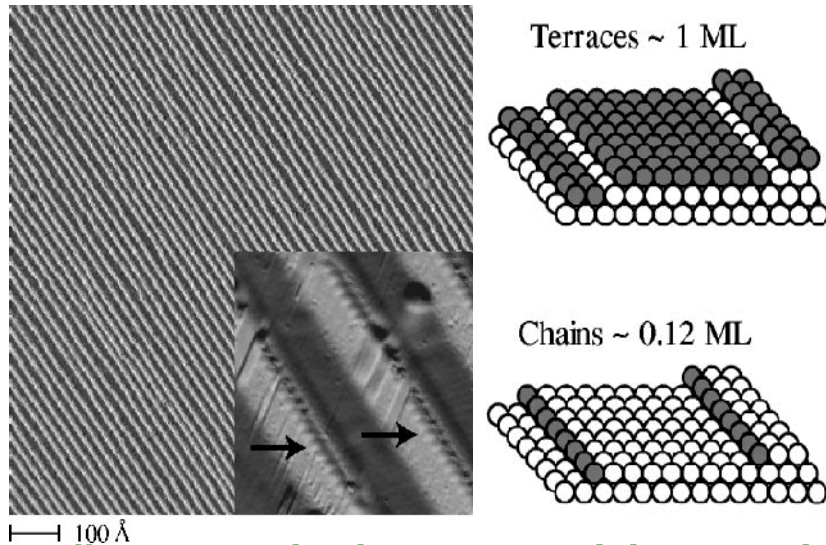
Bulk picture



Surface picture



Co/Pt(997)



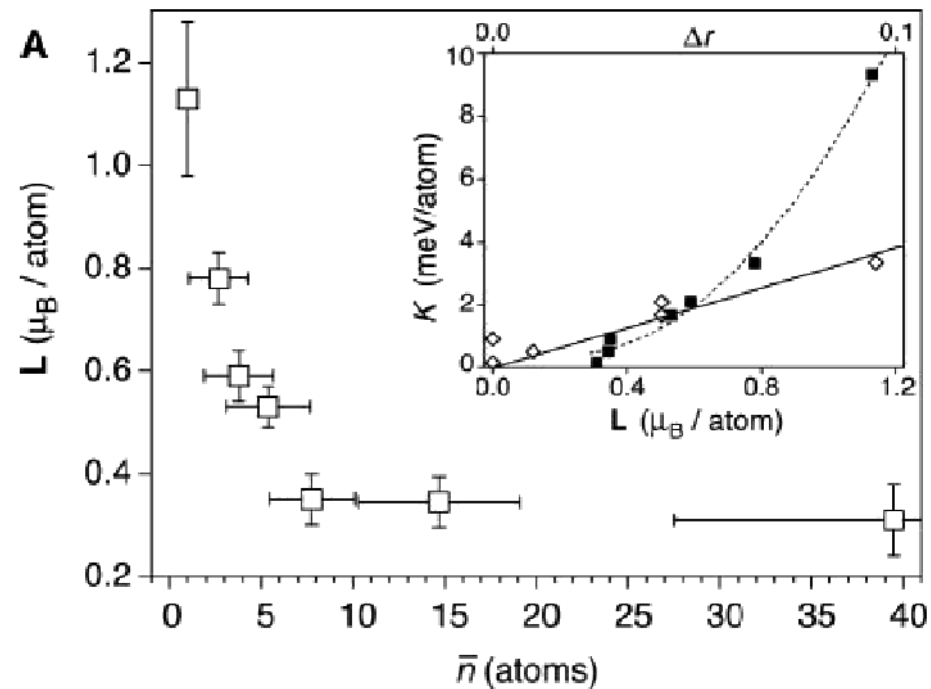
A. Dallmeyer *et al.*, *Phys.Rev.B* 61(8), R5153 (2000)

Conclusions

- Bulk: $m_L = 0.14\mu_B/\text{at.}$
- Surface: $m_L = 0.31\mu_B/\text{at.}$
- Bi-atomic wire: $m_L = 0.37\mu_B/\text{at.}$
- Mono-atomic wire: $m_L = 0.68\mu_B/\text{at.}$
- bi-atom: $m_L = 0.78\mu_B/\text{at.}$
- atom: $m_L = 1.13\mu_B/\text{at.}$

P. Gambardella *et al.*, *Nature* 416, 301 (2002)

Co/Pt(111)



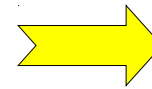
P. Gambardella *et al.*, *Science* 300, 1130 (2003)

Conclusions

- From bulk to atoms: considerable **increase of orbital moment**
- **2 atoms closer to wire than 1 atom**
- **bi-atomic wire closer to surface than wire**

Elements of theory

- Ising (1925). No magnetic order at $T > 0K$ in 1D Ising chain.
- Bloch (1930). No magnetic order at $T > 0K$ in 2D Heisenberg. (spin-waves; isotropic Heisenberg)
- → N. D. Mermin, H. Wagner, PRL17, 1133 (1966)
- Onsager (1944) + Yang (1951).
2D Ising model: $T_c > 0K$

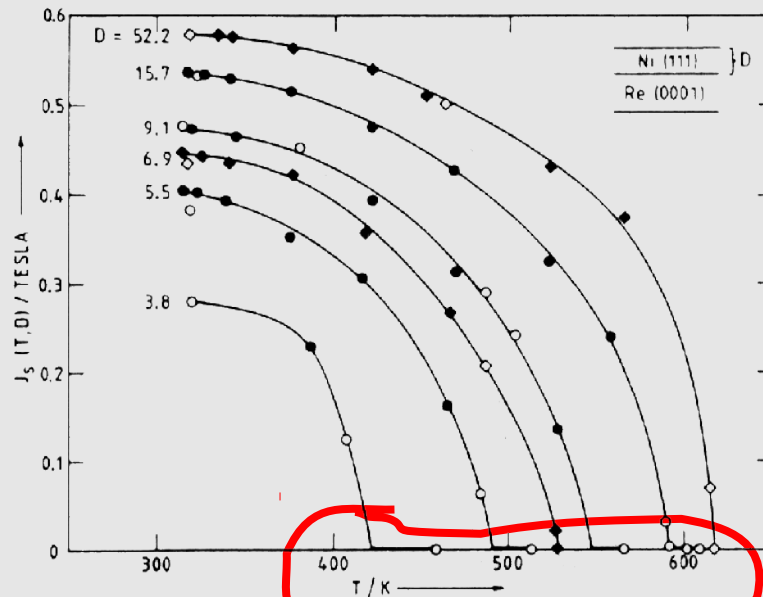


Magnetic anisotropy stabilizes ordering

Experiments

Ni(111)/Re(0001)

R. Bergholz and
U. Gradmann,
JMMM45, 389 (1984)



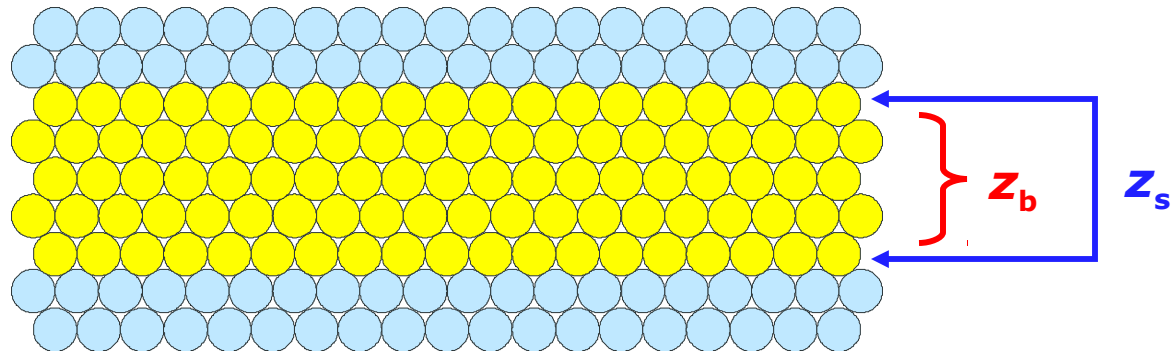
T_c interpreted with
molecular field

Naïve model

Molecular field

$$T_c = \frac{\mu_0 \langle z \rangle n_{W,1} n g_J^2 \mu_B^2 J(J+1)}{3k_B}$$

z neighbors



N atomic layers

$$\langle z \rangle = z_b - \frac{2(z_b - z_s)}{N} \quad \Rightarrow \quad \Delta T_c(t) \sim t^{-1}$$

Less naïve...

Thickness-dependent molecular field

$$\Delta T_c(t) \sim t^{-\lambda}$$

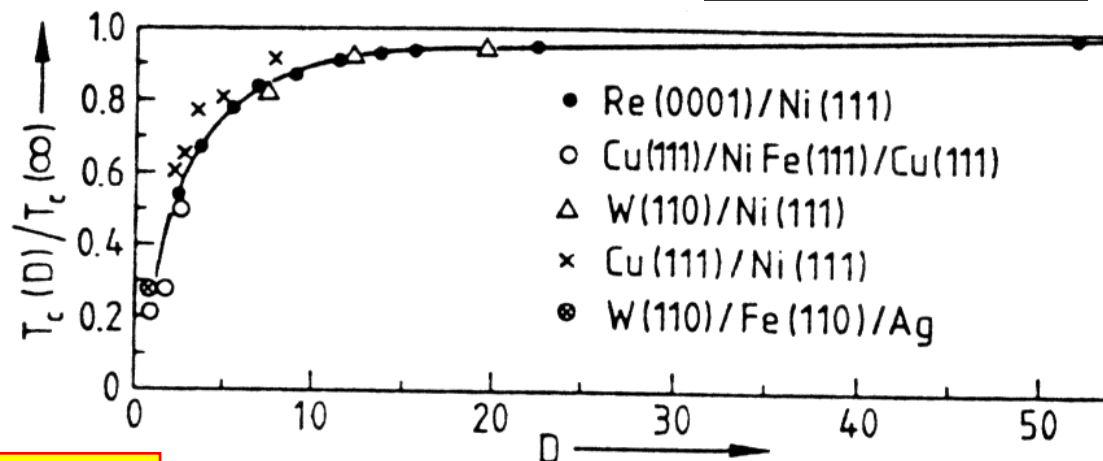
$$\lambda = 1$$

G.A.T. Allan, PRB1, 352 (1970)

Conclusion:

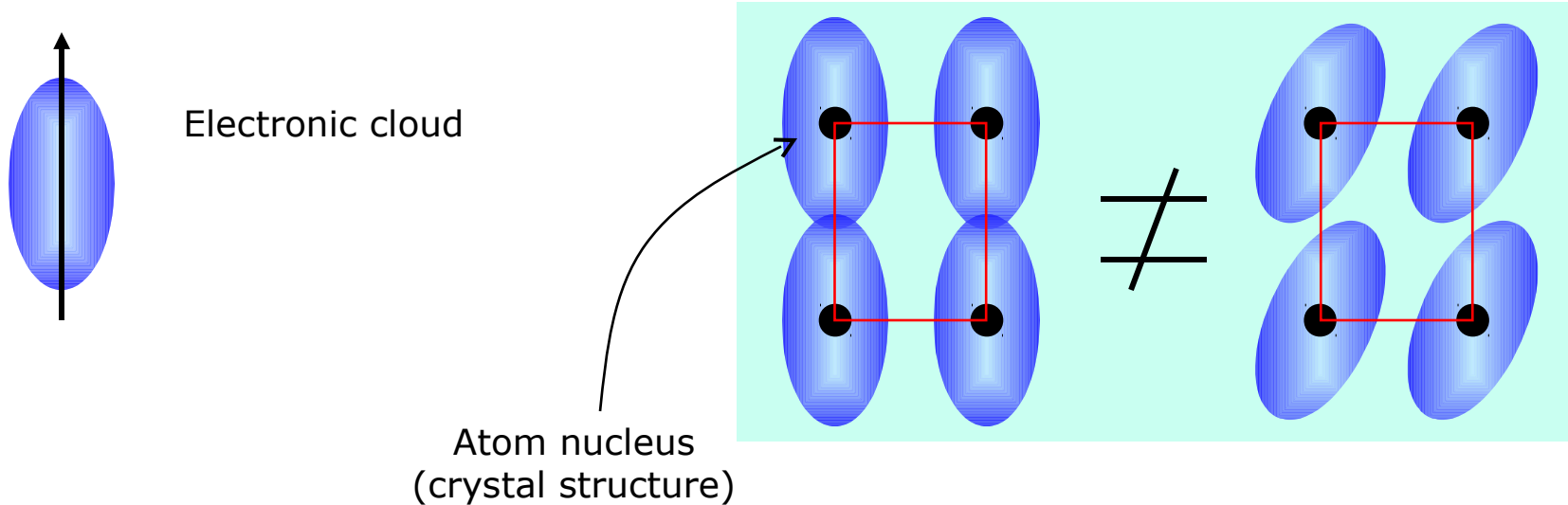
Naïve views are roughly correct

Experiments



U. Gradmann,
Handbook of Magn. Mater. Vol.7, ch.1 (1993)

Magnetocrystalline anisotropy energy



Spin-orbit coupling $\Rightarrow$ the energy of both spin and orbital moment depends on orientation

Series development on an angular basis:

Anisotropy energy

Normalized magnetization components

$$E_{mc} = K_1 m_z^2 + K_2 m_z^4 + \dots \quad \text{Uniaxial}$$

$$E_{mc} = K_4 (m_x^2 m_y^2 + m_y^2 m_z^2 + m_z^2 m_x^2) + \dots \quad \text{Cubic}$$

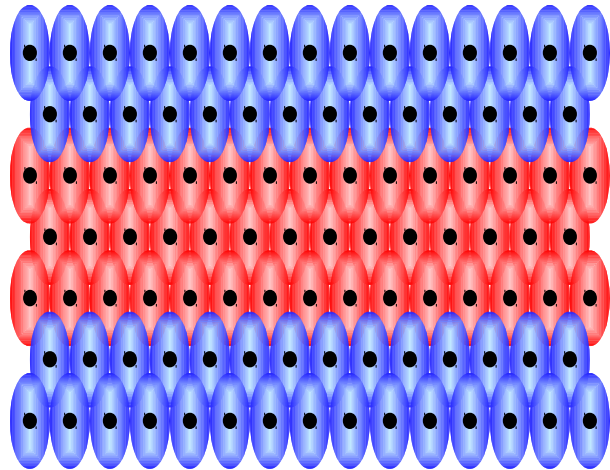
...

**Alignment of magnetization
is favored along
given axes of the crystal**

Surface anisotropy

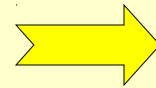
L. Néel,
J. Phys. Radium 15,
15 (1954)

« Superficial magnetic anisotropy and orientational superstructures »



Overview

Breaking of symmetry for
surface/interface atoms



Correction to the
magneto-crystalline energy

$$E_s = K_{S,1} \cos^2(\theta) + K_{S,2} \cos^4(\theta) + \dots$$

« This surface energy, of the order of 0.1 to 1 erg/cm², is liable to play a significant role in the properties of ferromagnetic materials spread in elements of dimensions smaller than 100Å »

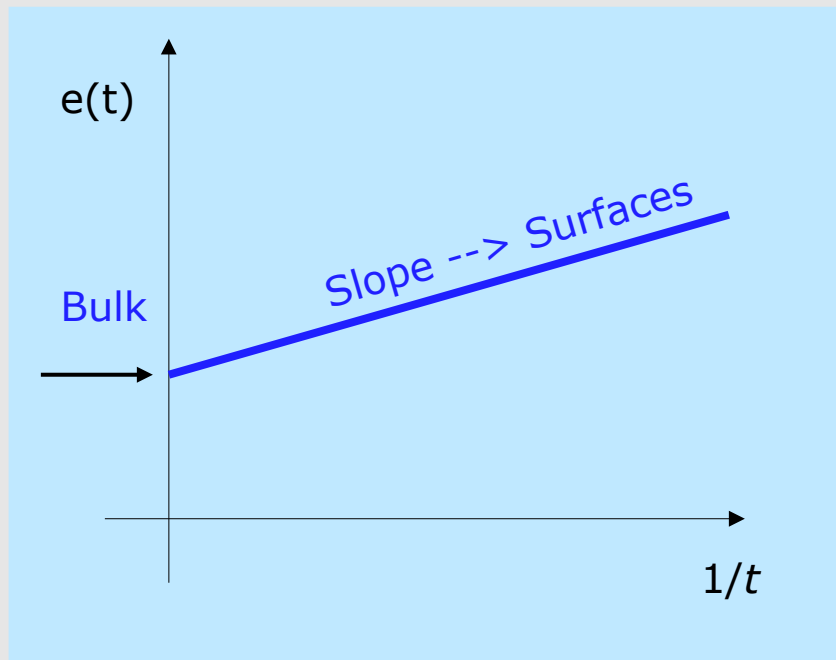
Pair model of Néel:

- Ks estimated from magneto-elastic constants
- Does not depend on interface material
- Yields order of magnitude only: correct value from experiments or calculations (precision !)

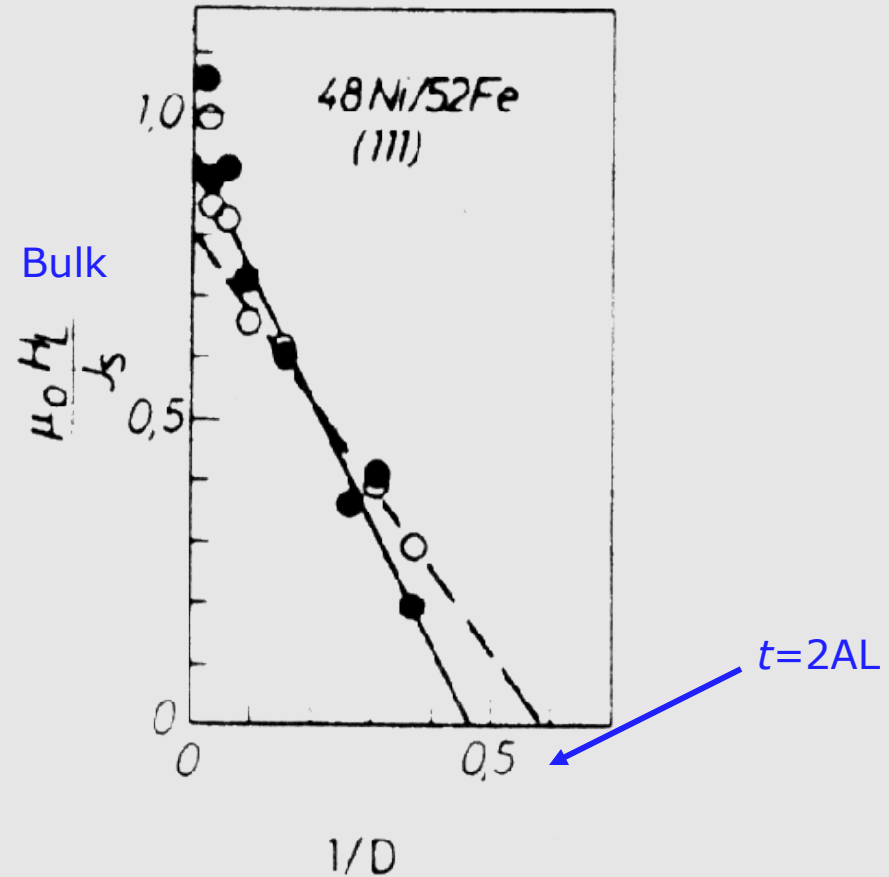
History of surface anisotropy : STEP 1 (1/t plot)

$$E_{\text{tot}}(t) = k_V t + 2k_S$$

$$\Rightarrow e(t) = k_V + \frac{2k_S}{t}$$



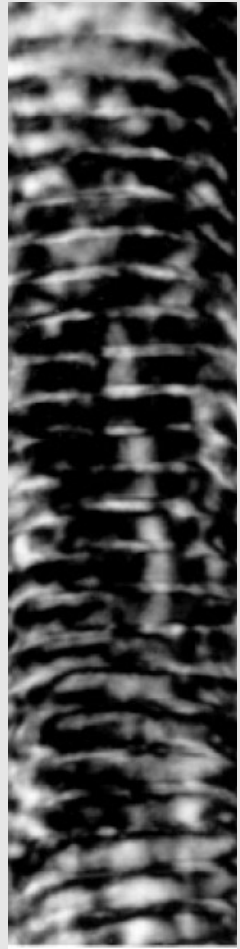
First example of perpendicular anisotropy



U. Gradmann and J. Müller,
Phys. Status Solidi 27, 313 (1968)

Main use in applications : perpendicular magnetic anisotropy in thin films

Materials and geometry



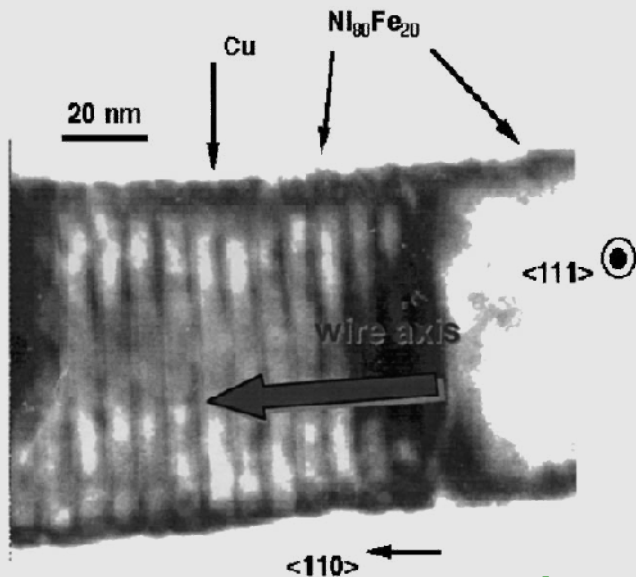
Interfacial elements with large spin-orbit: Pt, Au, Pd

Often: multilayers

Co/Au film



M. T. Johnson et al.,
Rep. Prog. Phys. 59,
1409 (1996)

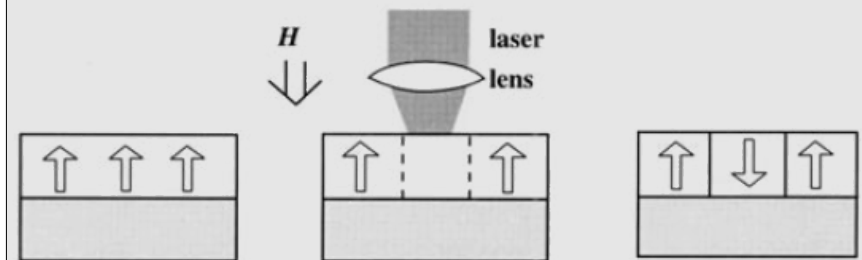
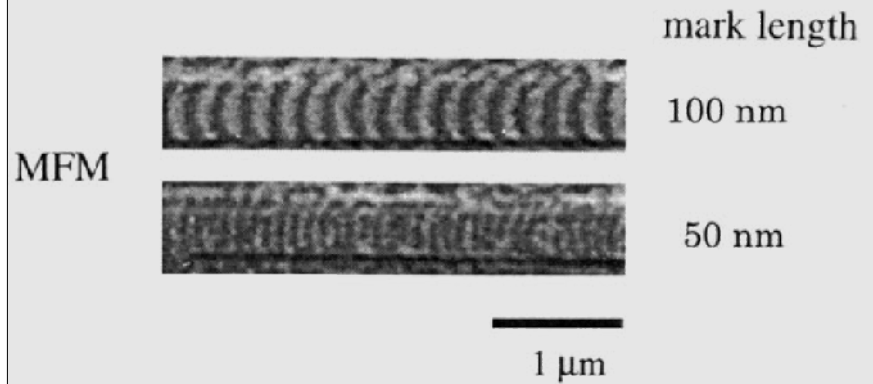


A. Fert et al., J. Magn. Magn. Mater. 200, 338 (1999)

Magneto-optical recording

Why: large magneto-optical response

Material: 3D-Rare-Earth based

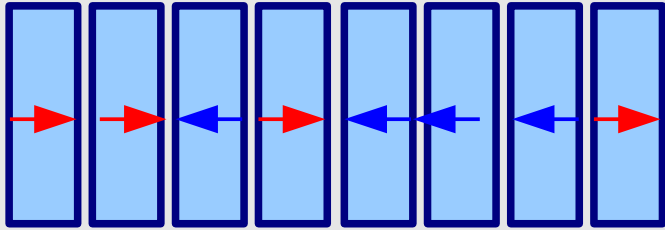


S. Tsunashima, J. Phys. D 34, R87 (2001)

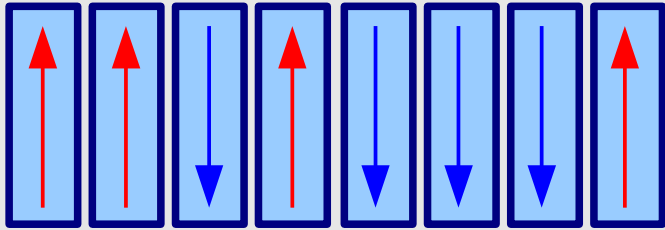
Main use in applications : perpendicular magnetic anisotropy

Decreased dipolar coupling in HDD media

Longitudinal recording (1956 -)



Perpendicular recording (2005 -)



S. N. Piramanayagam, *J. Appl. Phys.* **102**, 011301 (2007)

- ⇒ High anisotropy with low spread angle
- ⇒ Reduced intra- and inter-grain dipolar coupling

Enhanced anisotropy for solid-state memories

Concerns MRAM: Magnetic Random Access Memories

C. Chappert et al., *The emergence of spin electronics in data storage*, *Nat. Mater.* **6**, 813 (2007)

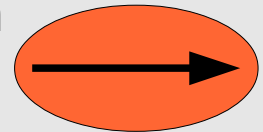
Reminder for the thermal stability for small flat elements:

$$H_c = \frac{2K}{\mu_0 M_s} \left(1 - \sqrt{\frac{25k_B T}{KV}} \right)$$

⇒ In-plane magnetization

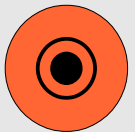
$$K = N \times \frac{1}{2} \mu_0 M_s^2$$

Issue: N is small with flat elements



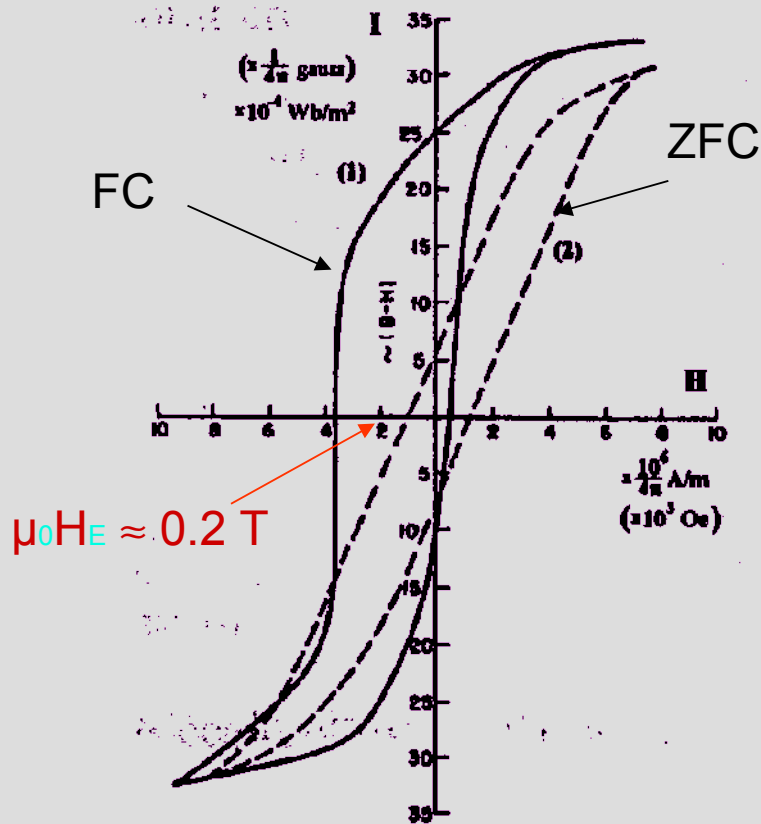
⇒ Perpendicular magnetization

$$K \approx \frac{1}{2} \mu_0 M_s^2$$

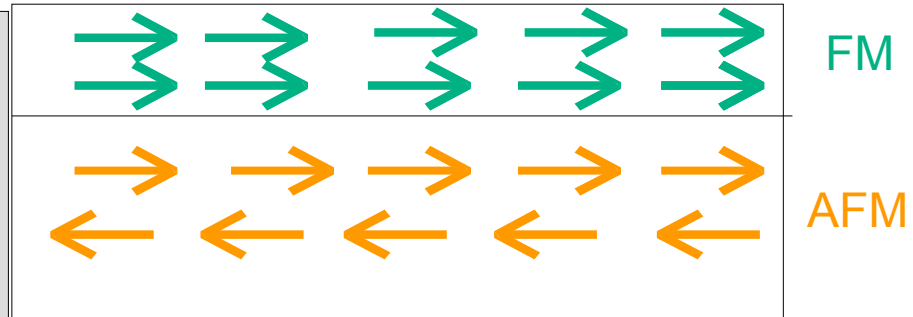


Seminal studies

Oxidized Co nanoparticles



Meiklejohn and Bean,
 Phys. Rev. 102, 1413 (1956),
 Phys. Rev. 105, 904, (1957)



Field-cooled hysteresis loops:

- Increased coercivity
- Shifted in field

Exchange bias

J. Nogués and Ivan K. Schuller
 J. Magn. Magn. Mater. 192 (1999) 203

Exchange anisotropy—a review

A E Berkowitz and K Takano
 J. Magn. Magn. Mater. 200 (1999)

Increase coercivity of layers

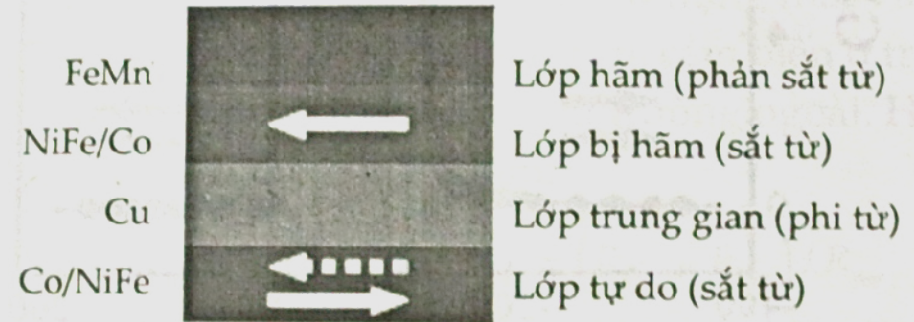


Crude approximation for thin layers:

$$H_{F-AF} \approx H_F \left(1 + \frac{K_{AF} t_{AF}}{K_F t_F} \right)$$

Application

Concept of spin-valve in magneto-resistive elements

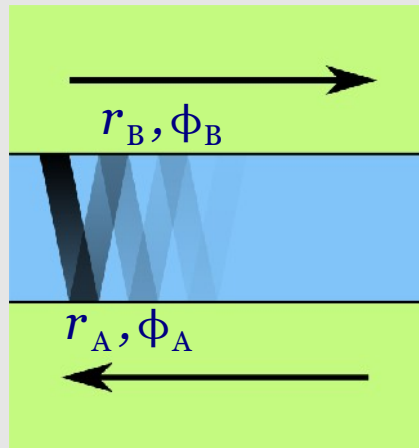


B. Diény et al., Phys. Rev. B 43, 1297 (1991)

- ⇒ Sensors
- ⇒ Memory cells
- ⇒ Etc.

The physics

Spin-dependent quantum confinement in the spacer layer



Forth & back
phase shift
 $\Delta \phi = q t + \phi_A + \phi_B$

Spin-independent

$$q = k^+ - k^-$$

Spin-dependent

$$r_A, \phi_A, r_B, \phi_B$$

Figures

Constructive and destructive interferences

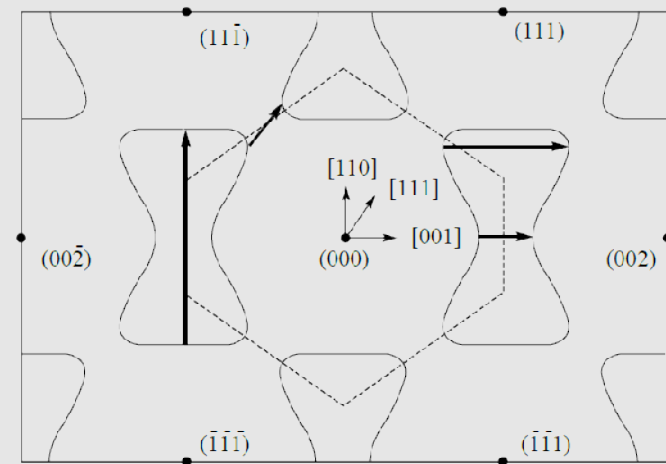
⇒ Maxima and minima of $n(\epsilon)$

Coupling strength:

$$E_s = J(t) \cos \theta \quad \text{in } J/\text{m}^2$$

$$\theta = \langle m_1, m_2 \rangle$$

$$\text{with: } J(t) = \frac{A}{t^2} \sin(q_\alpha t + \Psi)$$



P. Bruno, J. Phys. Condens. Matter 11, 9403 (1999)



Ti 	V 	Cr 	Mn 	Fe 	Co 	Ni 	Cu 			
No Coupling	9	3	7	7	Ferro-Magnet	Ferro-Magnet	Ferro-Magnet	8	3	
	0.1	9	.24	18				0.3	10	
2.89	2.62	2.50	2.24	2.48	2.50	2.49	2.56			
Zr 	Nb 	Mo 	Tc 	Ru 	Rh 	Pd 	Ag 			
No Coupling	9.5	2.5	5.2	3	3	3	7.9	3	No Coupling	No Coupling
	.02	*	.12	11	5	11	1.6	9		
3.17	2.86	2.72	2.71	2.65	2.69	2.75	2.89			
Hf 	Ta 	W 	Re 	Os 	Ir 	Pt 	Au 			
No Coupling	7	2	5.5	3	4.2	3.5	No Coupling	No Coupling		
	.01	*	.03	*	.41	10			4	3
3.13	2.86	2.74	2.74	2.68	2.71	2.77	2.88			

fcc bcc
 hcp complex cubic

Element	
A_1 (Å)	ΔA_1 (Å)
J_1 (erg/cm ²)	P (Å)
r_{we} (Å)	

$$J(t) = \frac{A}{t^2} \sin\left(\frac{2\pi t}{P} + \Psi\right)$$

Illustration of coupling strength

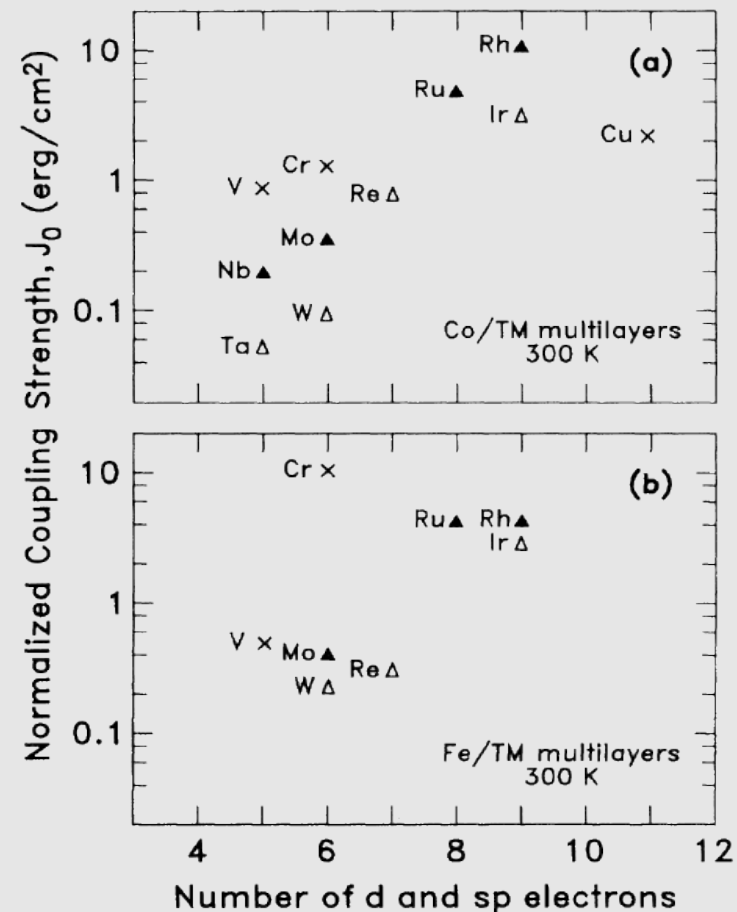
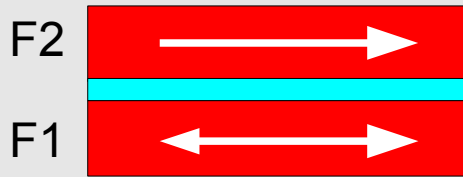


FIG. 3. Dependence of the normalized exchange coupling constant on the 3d, 4d and 5d transition metals in (a) Co/TM and (b) Fe/TM multilayers.

Note: $J(t)$ extrapolated for $t=3\text{\AA}$

S. S. P. Parkin, Phys. Rev. Lett. 67, 3598 (1991)

Synthetic Ferrimagnets (SyF) — Crude description



Hypothesis:

- ⇒ Two layers rigidly coupled
- ⇒ Reversal modes unchanged
- ⇒ Neglect dipolar coupling

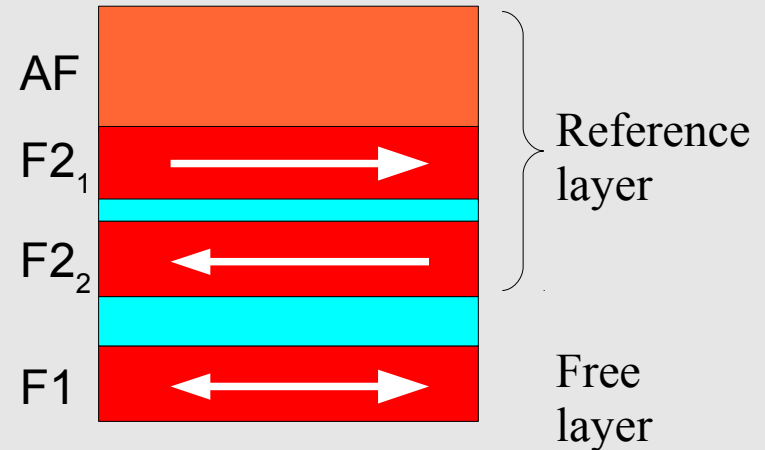


$$M = \frac{|e_1 M_1 - e_2 M_2|}{e_1 + e_2} \quad K = \frac{e_1 K_1 + e_2 K_2}{e_1 + e_2}$$

$$H_c = \frac{e_1 M_1 H_{c,1} + e_2 M_2 H_{c,2}}{|e_1 M_1 - e_2 M_2|}$$

What use?

- ⇒ Increase coercivity of pinned layers
- ⇒ Decrease intra- and inter- dot dipolar coupling



Practical aspects

- ⇒ Ru spacer layer (largest effect)
- ⇒ Control thickness within a few Angströms !



- [1] Magnetic domains, A. Hubert, R. Schäfer, Springer (1999, reed. 2001)
- [2] R. Skomski, Simple models of Magnetism, Oxford (2008).
- [3] R. Skomski, *Nanomagnetics*, J. Phys.: Cond. Mat. **15**, R841–896 (2003).
- [4] O. Fruchart, A. Thiaville, *Magnetism in reduced dimensions*, C. R. Physique **6**, 921 (2005) [Topical issue, Spintronics].
- [5] O. Fruchart, *Couches minces et nanostructures magnétiques*, Techniques de l'Ingénieur, E2-150-151 (2007) [FRENCH]
- [6] Lecture notes from undergraduate lectures, plus various slides:
<http://perso.neel.cnrs.fr/olivier.fruchart/slides/>
- [7] G. Chaboussant, Nanostructures magnétiques, Techniques de l'Ingénieur, revue 10-9 (RE51) (2005)
- [8] D. Givord, Q. Lu, M. F. Rossignol, P. Tenaud, T. Viadieu, Experimental approach to coercivity analysis in hard magnetic materials, J. Magn. Magn. Mater. **83**, 183-188 (1990).
- [9] D. Givord, M. Rossignol, V. M. T. S. Barthem, The physics of coercivity, J. Magn. Magn. Mater. **258**, 1 (2003).
- [10] J.I. Martin et coll., *Ordered magnetic nanostructures: fabrication and properties*, J. Magn. Magn. Mater. **256**, 449-501 (2003)
- [11] Lecture notes in magnetism: <http://esm.neel.cnrs.fr/repository.html>



Moment and anisotropy of ultrathin films

U. Gradmann, Handbook of magnetic materials vol. 7, K. H.K. Buschow Ed., Elsevier, Magnetism of transition metal films, 1 (1993)

M. Farle, Ferromagnetic resonance of ultrathin metallic layers, Rep. Prog. Phys. 61, 755 (1998)

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