

Magnetic Force Microscopy



Olivier Fruchart

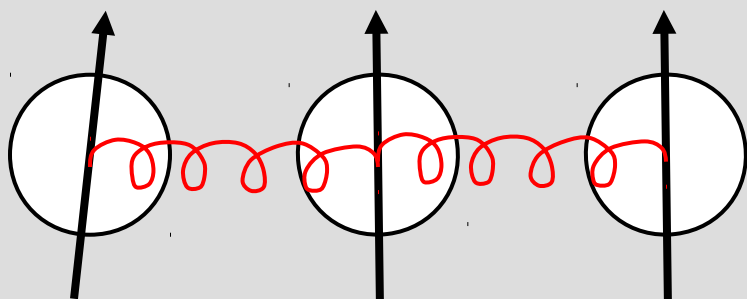
Institut Néel (CNRS-UJF-INPG)

Grenoble - France

<http://neel.cnrs.fr>



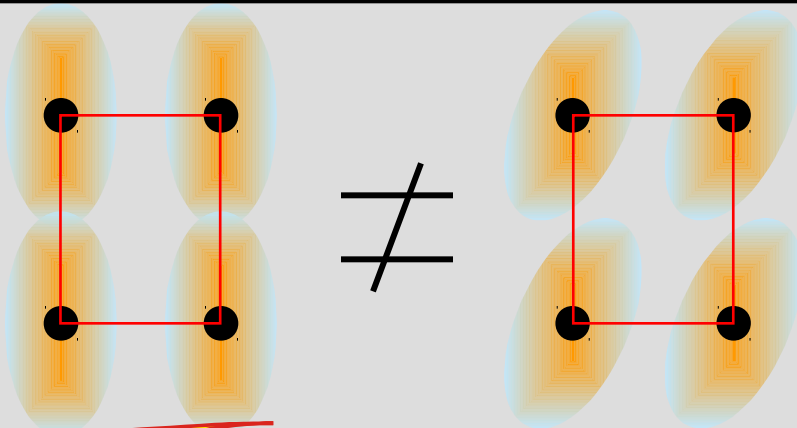
Exchange energy



$$E_{\text{Ech}} = -J_{1,2} \vec{S}_1 \cdot \vec{S}_2$$

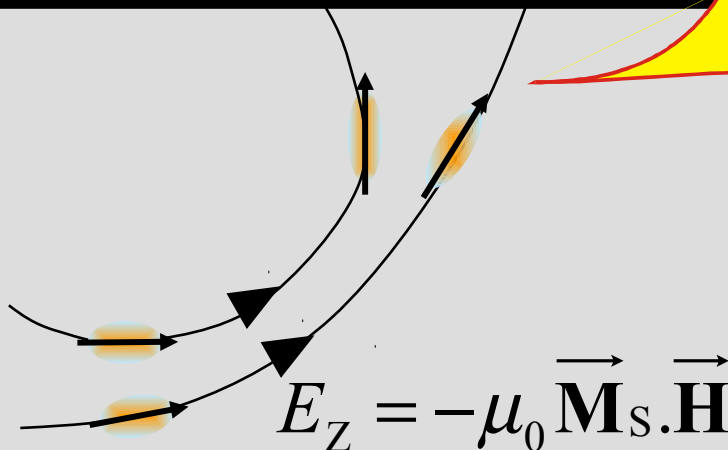
$$= A(\nabla \theta)^2$$

Magnetocrystalline anisotropy energy



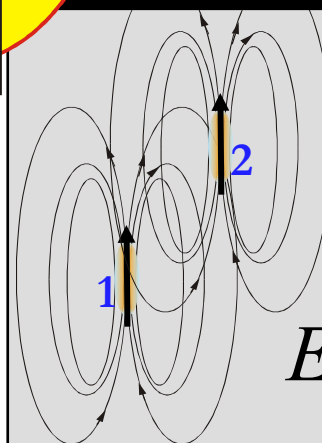
$$E_{\text{mc}} = K \sin^2(\theta)$$

Zeeman energy (enthalpy)



$$E_Z = -\mu_0 \vec{M}_s \cdot \vec{H}$$

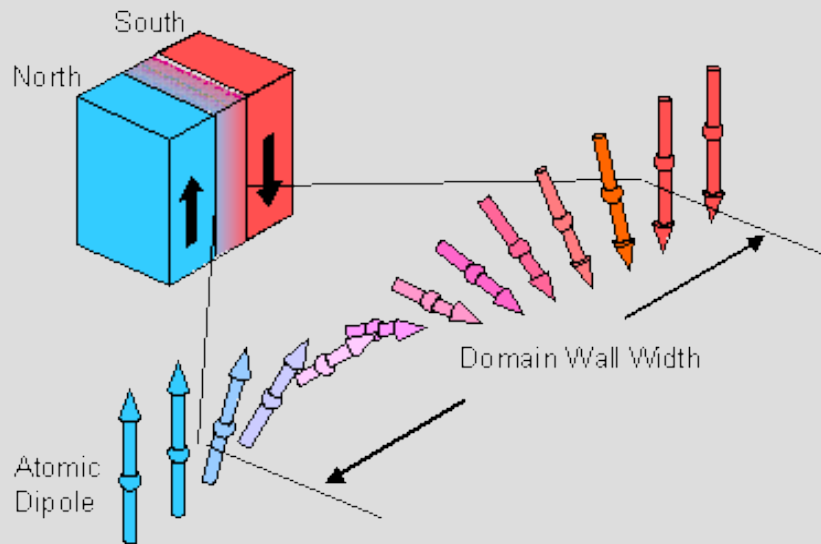
Dipolar energy



$$E_d = -\frac{1}{2} \mu_0 \vec{M}_s \cdot \vec{H}_d$$



Typical length scale:
Bloch wall width λ_B



$$e = A \left(\frac{d\theta}{dx} \right)^2 + K \sin^2 \theta$$

Exchange
J/m
Anisotropy
J/m³

Numerical values

$$\lambda_B = \pi \sqrt{A / K}$$

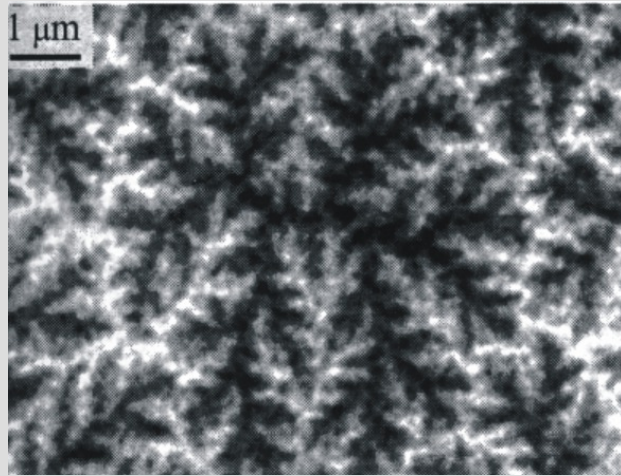
$$\lambda_B = 2 - 3 \text{ nm} \longrightarrow \lambda_B \geq 100 \text{ nm}$$

Hard
Soft



Bulk material

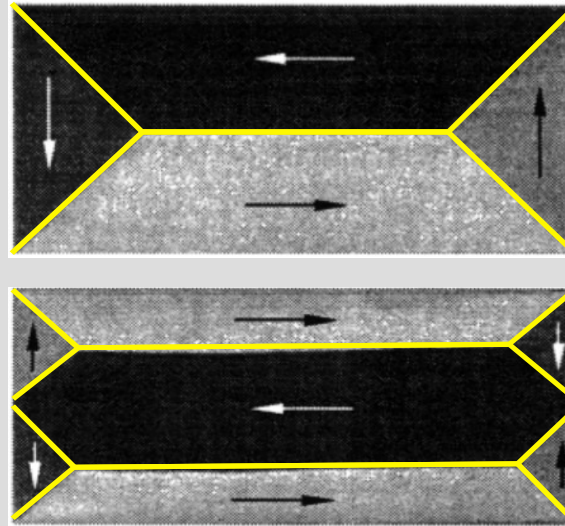
Numerous and complex magnetic domains



Co(1000) crystal – SEMPA
A. Hubert, Magnetic domains

Mesoscopic scale

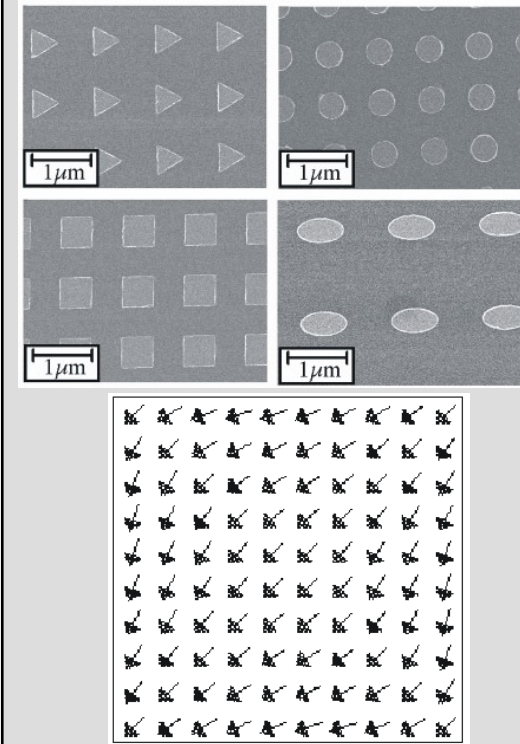
Small number of domains, simple shape



Microfabricated dots
Kerr magnetic imaging
A. Hubert, Magnetic domains

Nanometric scale

Magnetic single-domain



R.P. Cowburn,
J.Phys.D:Appl.Phys.33,
R1 (2000)

Nanomagnetism ~ mesoscopic magnetism



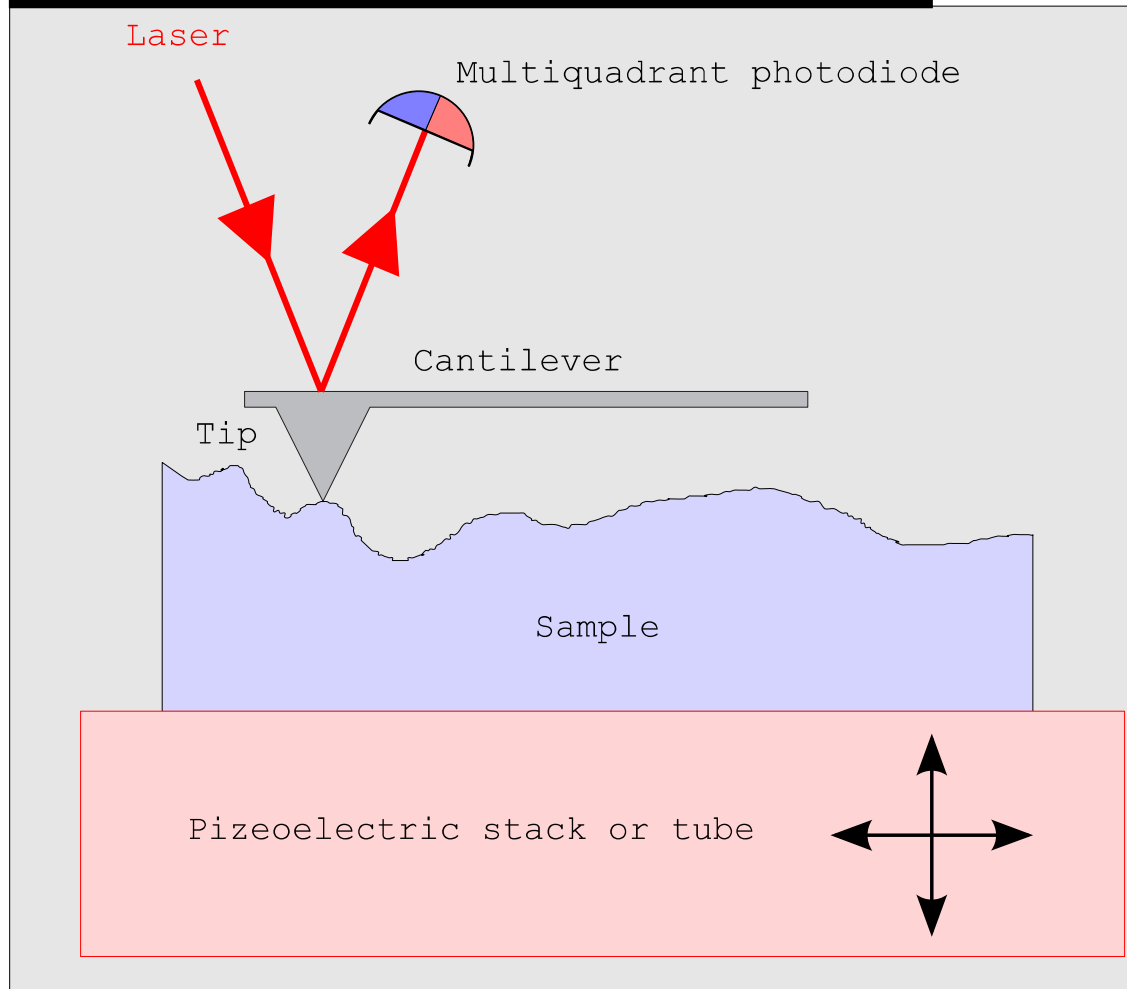
What information may be sought

- ⇒ Distribution of magnetization in sample
- ⇒ Direction & magnitude
- ⇒ Depth resolution
- ⇒ Elemental resolution
- ⇒ Lateral resolution
- ⇒ Time resolution

Conditions and environment

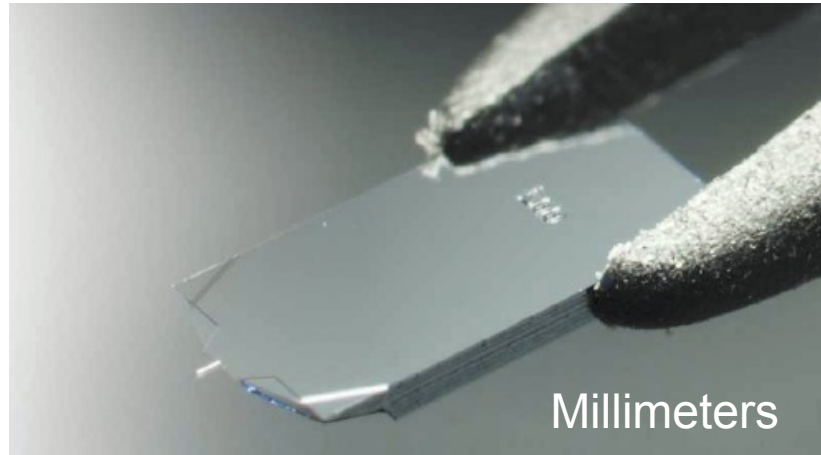
- ⇒ Temperature
- ⇒ Magnetic field
- ⇒ Electrical current, light etc.
- ⇒ Additional microscopies

Key elements of an Atomic Force Microscope (AFM)

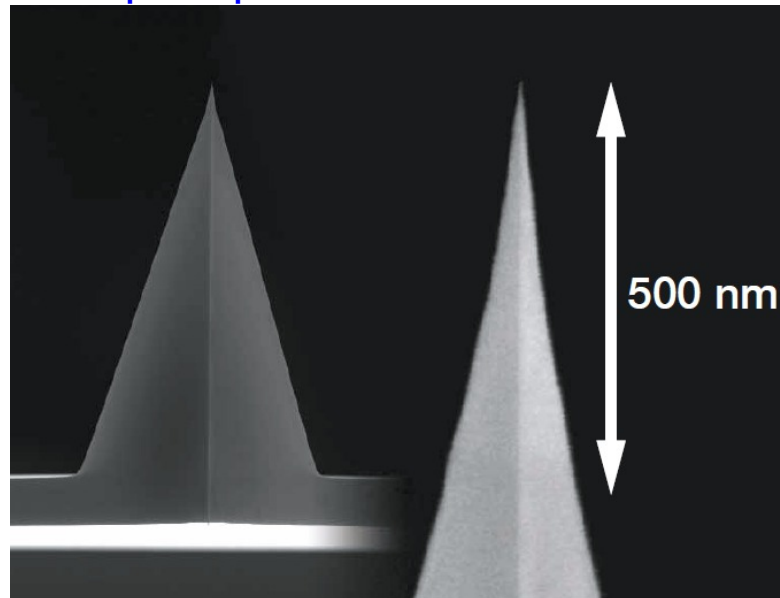


⇒ Measures forces (vertical and lateral) between sample and tip

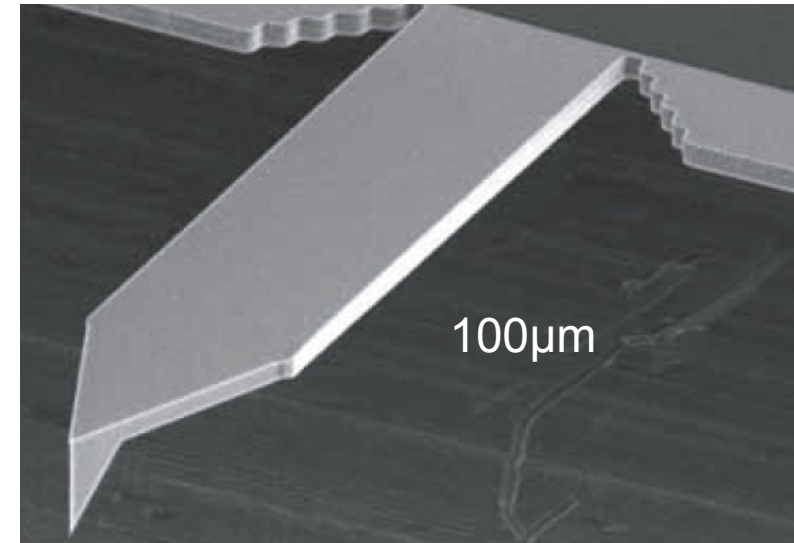
Chip – Batch fabrication



Full tip + apex



Cantilever



⇒ Price 10-200€/tip

⇒ Radius of curvature $\approx 5\text{nm}$

Images : Olympus catalog (<http://www.olympus.co.jp/probe>)



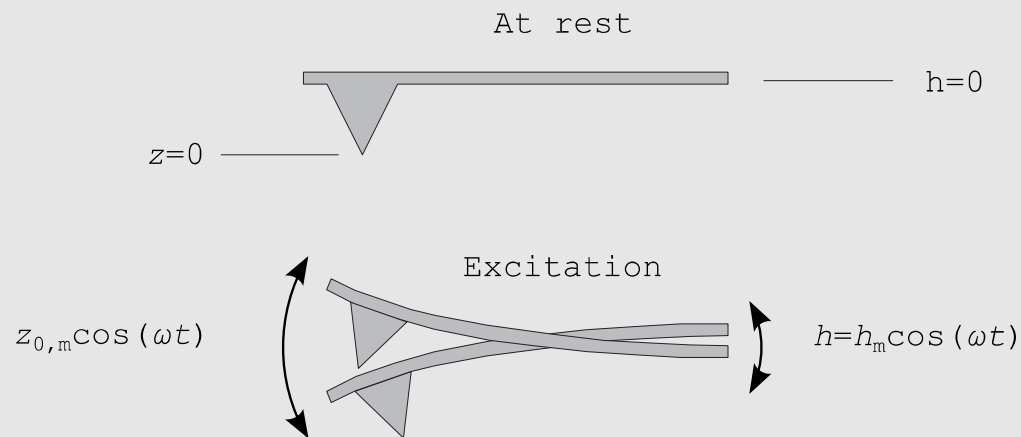
Measures

- ⇒ Topography
- ⇒ Mechanical properties
- ⇒ Electric properties
- ⇒ Piezoelectric properties
- ⇒ Long-range forces
(electrostatic, magnetic)
- ⇒ Micromanipulation &
fabrication

Modes of operation

- ⇒ Static (deflection)
 - When contact is needed : electric, friction etc.
- ⇒ Dynamic (cantilever oscillation)
 - Less damage to sample and tip
 - More sensitive

Mechanical excitation of cantilevers



$$m \ddot{z} + \Gamma \dot{z} + k z = F(z, t)$$

m	Inertia
Γ	Damping
k	Spring
$F(z, t)$	External force

Notations

Seek solutions for $F=0$

$$z(t) = z_0 e^{j\omega t}$$

Reference angular velocity

$$\omega_0 = \sqrt{\frac{k}{m}}$$

Quality factor

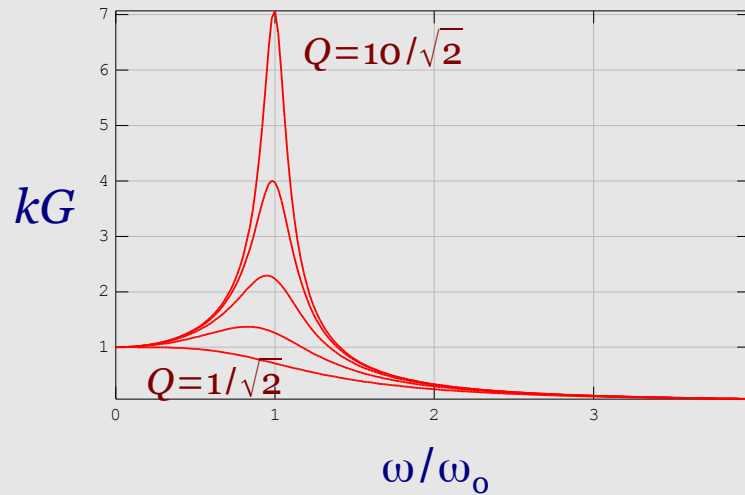
$$Q = \frac{\sqrt{k m}}{\Gamma}$$

⇒ Transfert function

$$H = \frac{z}{F} = \frac{1}{k} \frac{1}{-\left(\frac{\omega}{\omega_0}\right)^2 + \frac{j}{Q} \left(\frac{\omega}{\omega_0}\right) + 1}$$



Gain

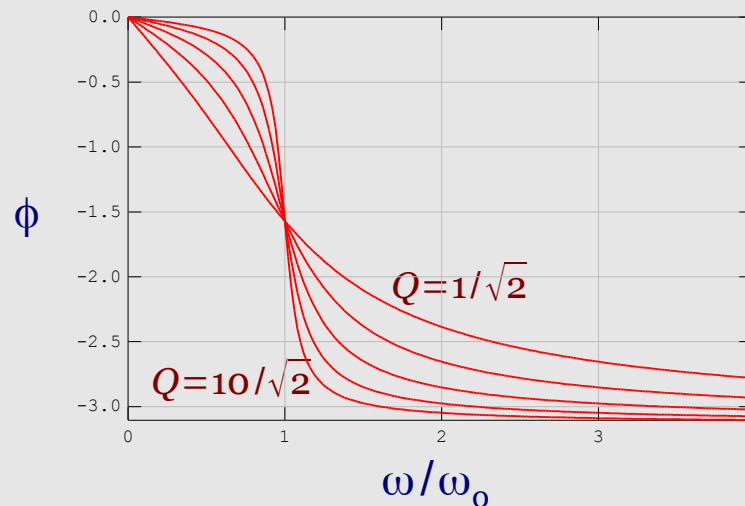


$$G = |H| = \frac{1}{k} \frac{1}{\sqrt{\left[1 - \left(\frac{\omega}{\omega_0}\right)^2\right]^2 + \frac{1}{Q^2} \left(\frac{\omega}{\omega_0}\right)^2}}$$

Peak at : $\omega_r = \omega_0 \sqrt{1 - \frac{1}{2Q^2}}$

$$\begin{cases} kG(0) = 1 \\ kG(\omega_r) = Q \\ kG(\infty) = 0 \end{cases}$$

Dephasing



$$\cos \phi = \frac{1 - \left(\frac{\omega}{\omega_0}\right)^2}{\sqrt{\left[1 - \left(\frac{\omega}{\omega_0}\right)^2\right]^2 + \frac{1}{Q^2} \left(\frac{\omega}{\omega_0}\right)^2}}$$

$$\phi(0) = 0$$

$$\phi(\infty) = -\pi$$

$Q \gg 1$

$$\omega_r \approx \omega_0$$

$$\phi(\omega_r) \approx -\pi/2$$

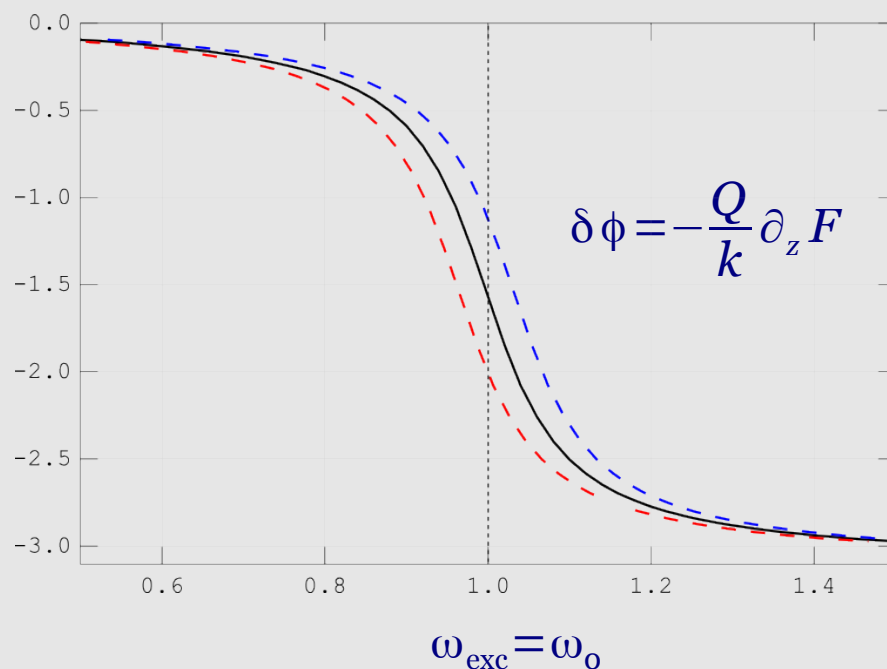
$$\frac{\Delta \omega_r}{\omega_0} \approx \frac{\sqrt{3}}{Q}$$

Tip-sample interaction treated as perturbation

$$m \ddot{z} + \Gamma \dot{z} + k z = F(z) \quad \text{with} \quad F(z) = F(z_0) + (z - z_0) \partial_z F$$

⇒ Mere renormalization : $\omega_{\text{o,eff}} = \omega_0 \left(1 - \frac{1}{2k} \partial_z F \right)$

Phase shift



Attractive force

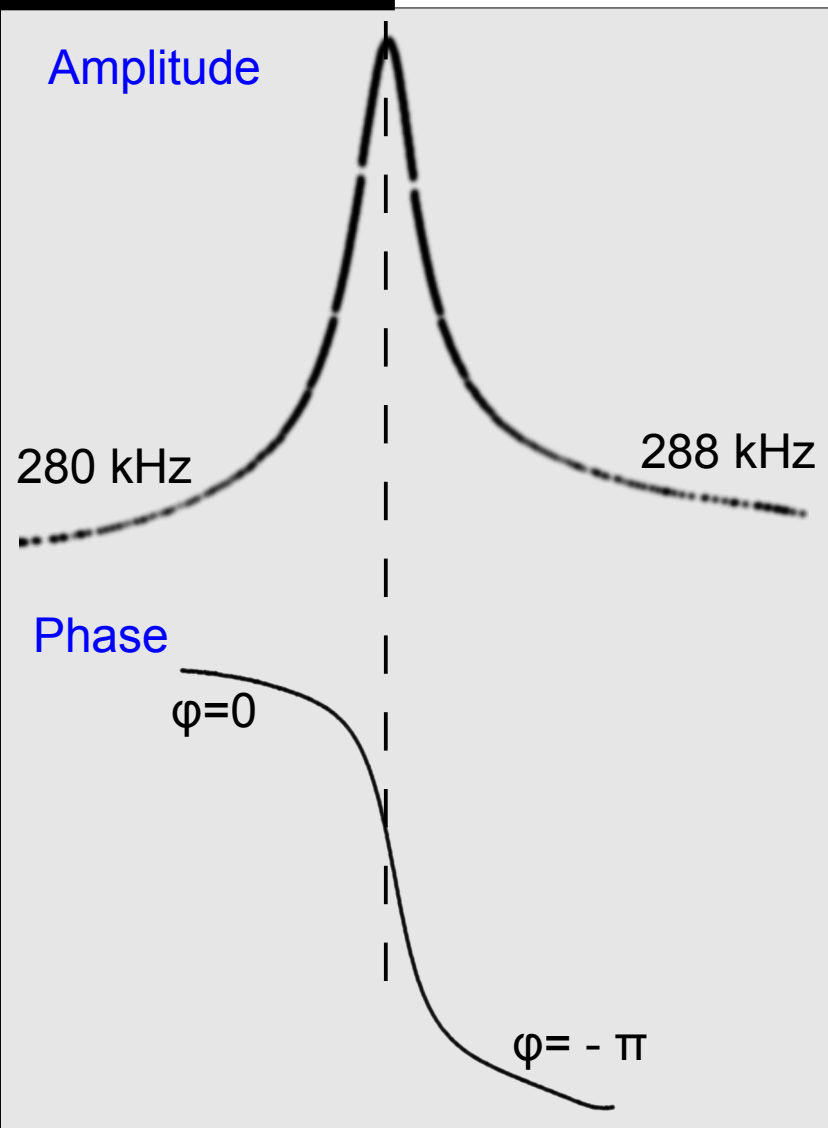
⇒ Red shift

Repulsive force

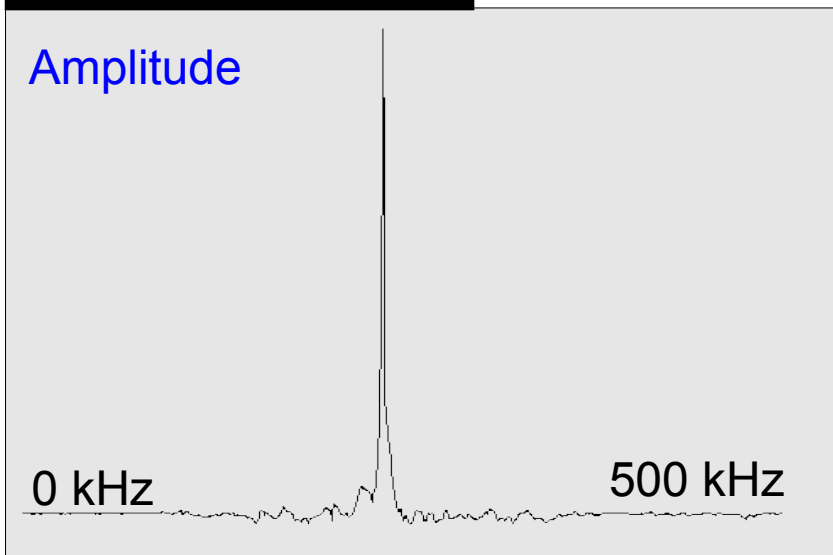
⇒ Blue shift

⇒ Forces monitored through phase shift

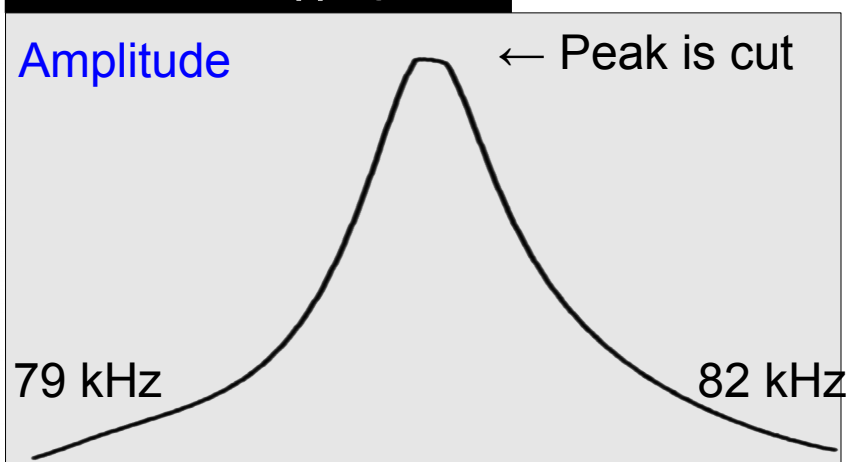
Resonance spectrum



Full resonance spectrum

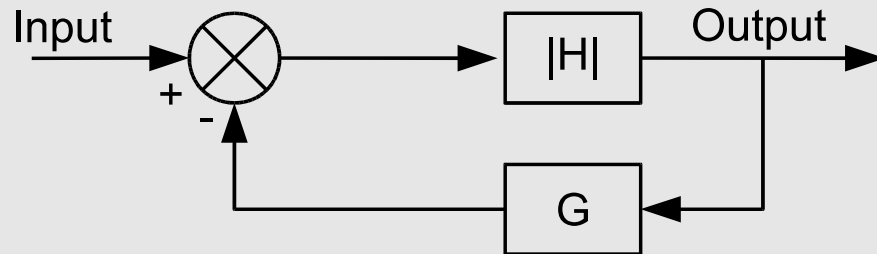


Resonance in tapping mode

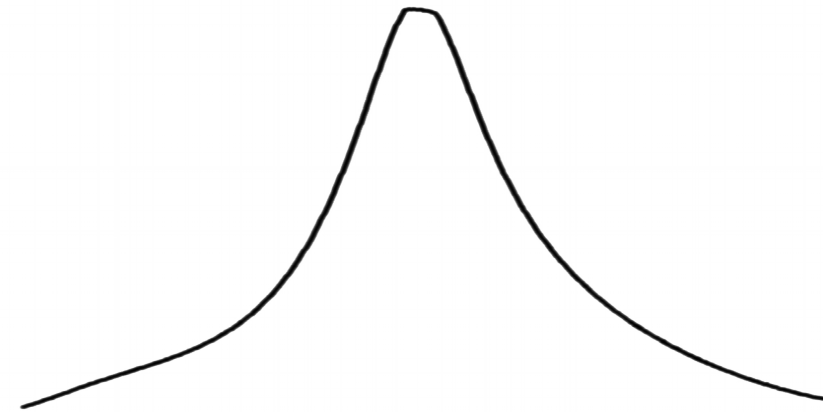


Close-loop operation

Feedback signal and setpoint: amplitude

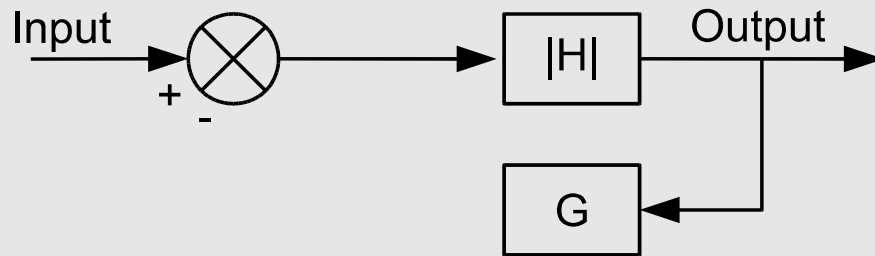


⇒ Map at constant force

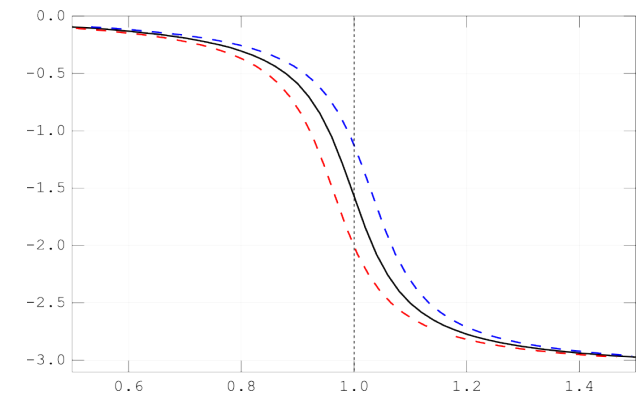


⇒ Ex : map = topography with setpoint on the amplitude

Open-loop operation



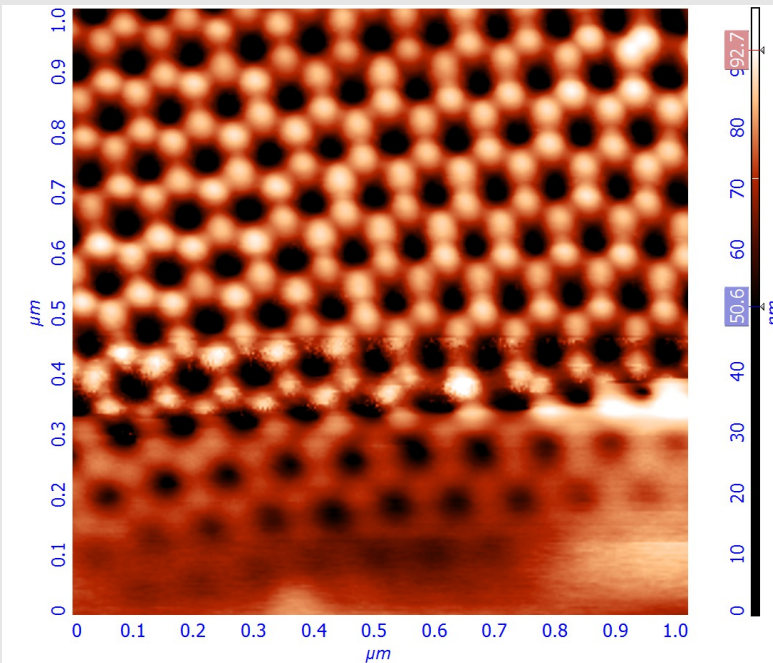
⇒ Map The force along a predefined trajectory (plane, lift-height etc.)



⇒ Ex : map = magnetic stray field above sample

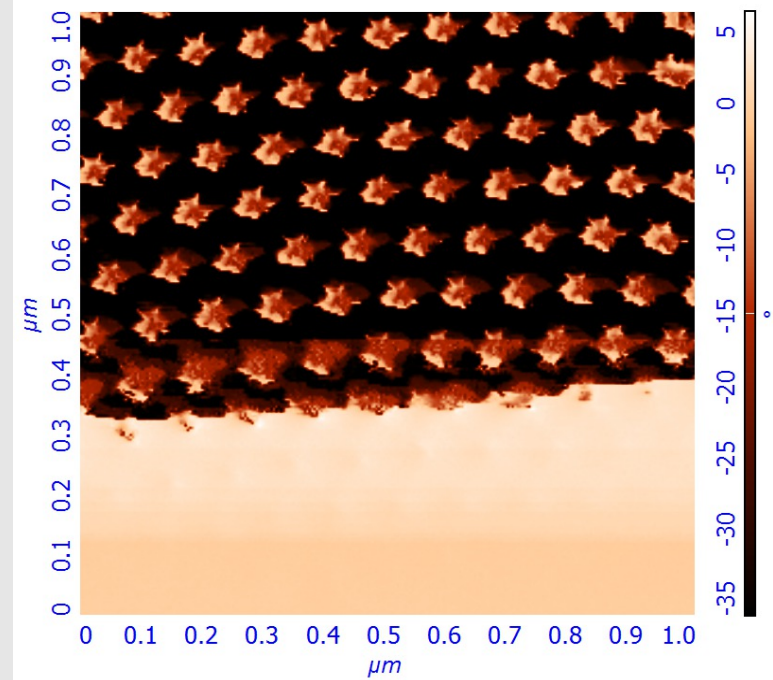
Images

Height image (topography)



Increasing pressure

Phase image

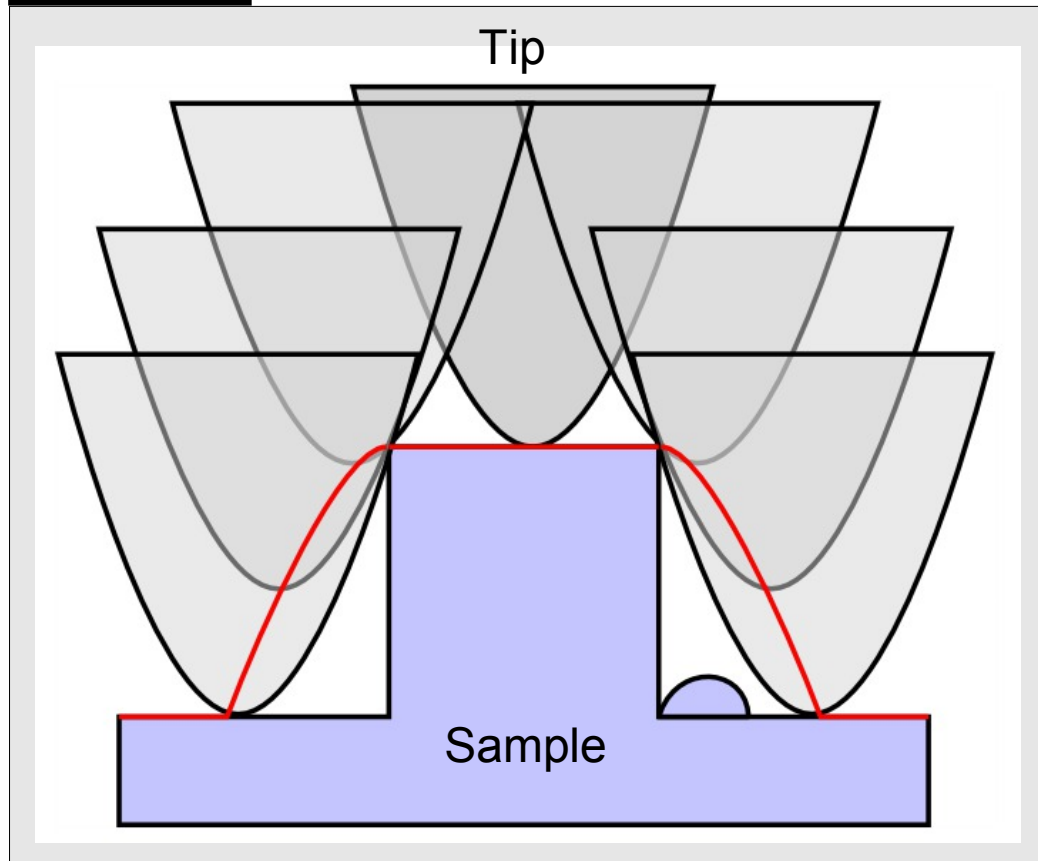


To notice

- ⇒ Non-contact part (bottom of image)
- ⇒ Phase does not reflect topography
- ⇒ Noise and phase depend on set point

**Sample : self-organized Anodized Alumina
(synthesis L. Cagnon, Institut Néel)**

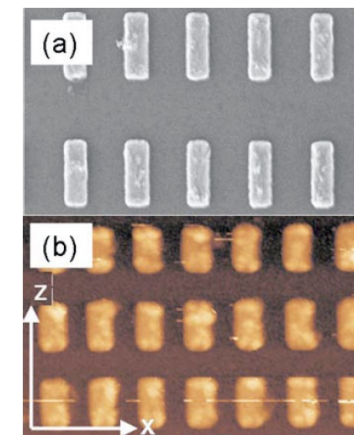
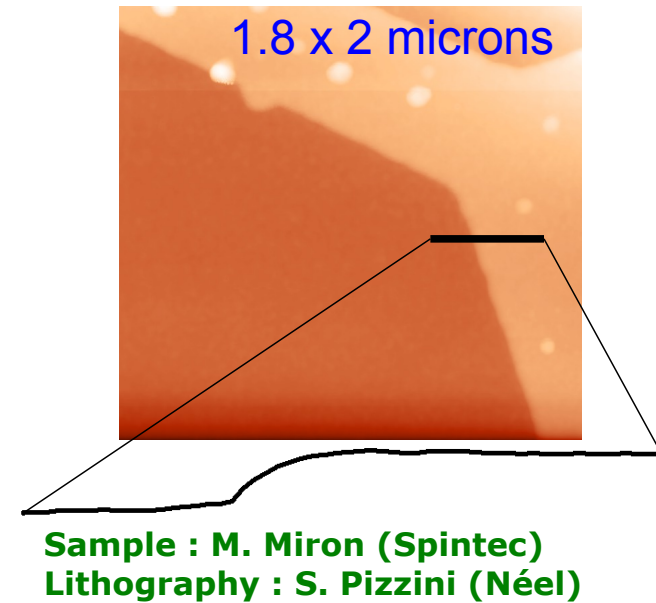
Schematics



Notice

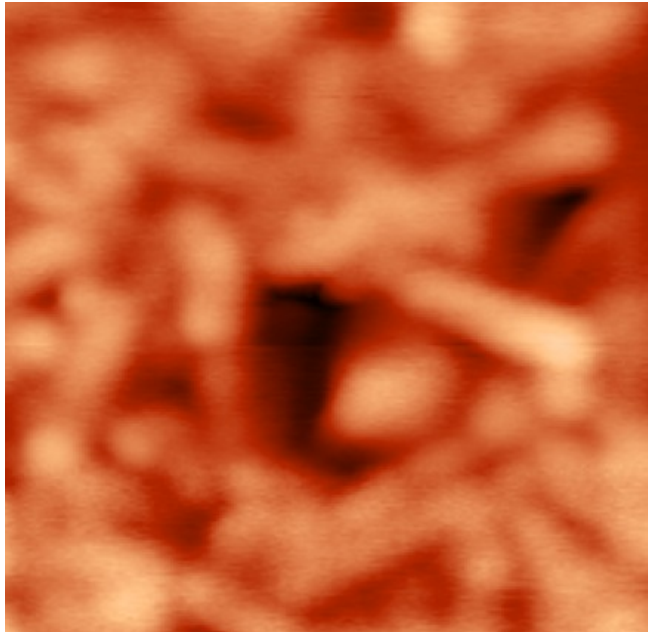
- ↪ Lateral (base) size is over-estimated with AFM
- ↪ Shading, not convolution (no true retrieval possible)
- ↪ Tips are less sharp for MFM due to magnetic coating

Examples

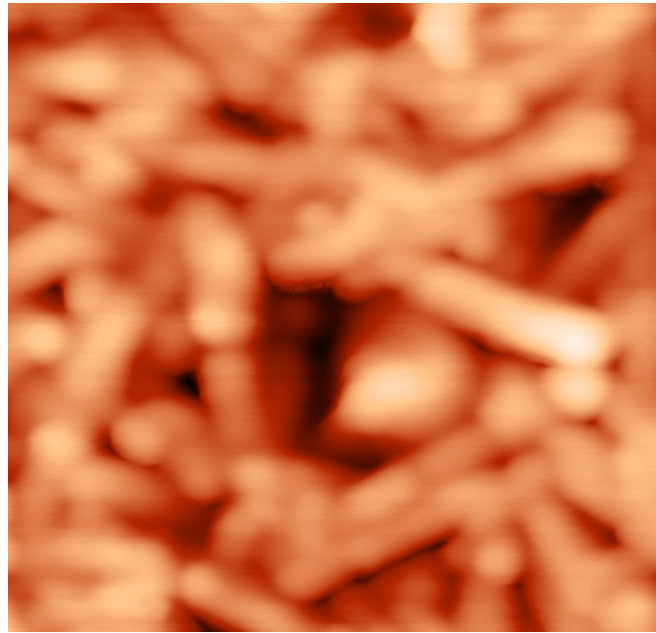


**S. Y. Suck et al.,
 APL95, 162503
 (2009)**

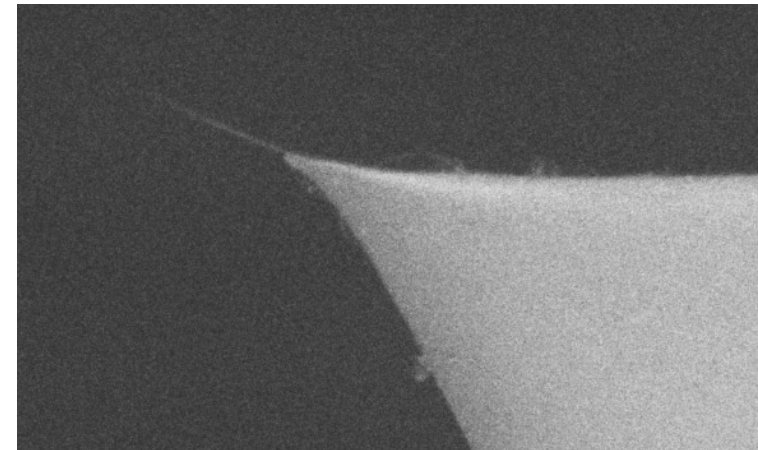
ZIP disk, 400x400 nm



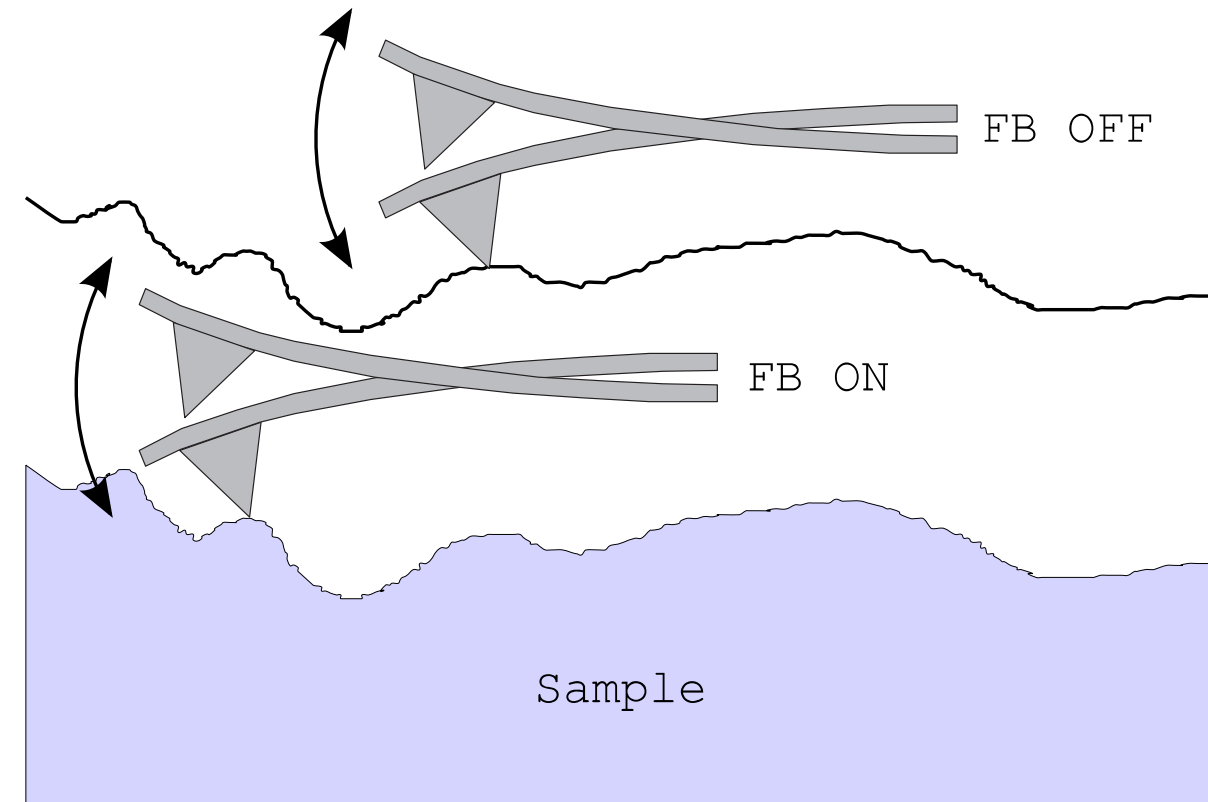
Usual tip



SWCNT tip

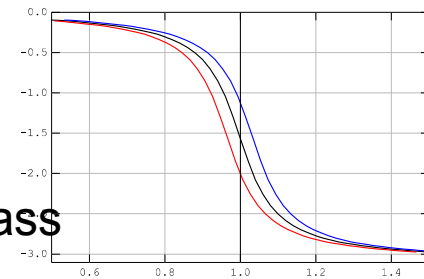


Tip : A. M. Bonnot (Institut Néel)



Second pass

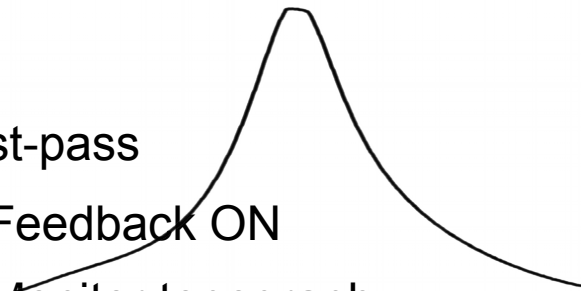
⇒ Monitor long-range forces (magnetic, electrostatic)



First-pass

⇒ Feedback ON

⇒ Monitor topography (height) and any other signal (phase etc.)



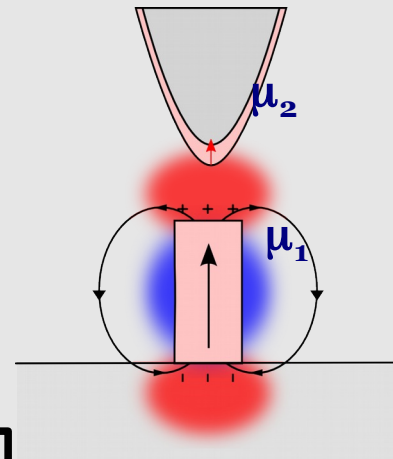
Calculate energy with magnetic dipoles

Magnetic field arising from a magnetic dipole

$$\mathbf{H}_d(\mathbf{r}) = \frac{\mu_0}{4\pi r^3} \left[\frac{3(\boldsymbol{\mu}_1 \cdot \mathbf{r})\mathbf{r}}{r^2} - \boldsymbol{\mu}_1 \right]$$

$$\Rightarrow \mathbf{F}_2(\mathbf{r}) = -\nabla E_{1,2} = \mu_0 \nabla (\mathbf{H}_d \cdot \boldsymbol{\mu}_2)$$

$$\mathbf{F}_2(\mathbf{r}) = -\nabla \mathcal{E}_{1,2} \quad \text{with} \quad \boxed{\mathcal{E}_{1,2} = -\mu_0 \boldsymbol{\mu}_2 \cdot \mathbf{H}_d}$$



Calculate energy with magnetic dipoles

Analogy with electrostatics thanks to $\text{div}(\mathbf{H}_d) = -\text{div}(\mathbf{M})$

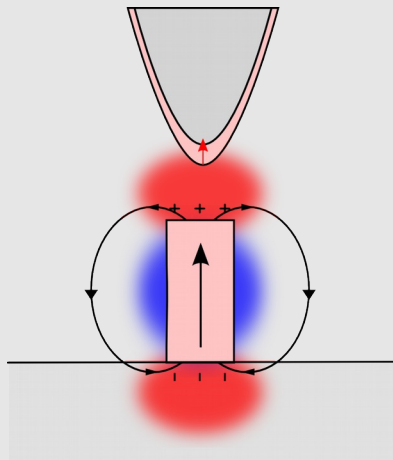
$$\mathbf{H}_d(\mathbf{r}) = M_s \left(-\iiint_{\text{space}} \frac{\text{div}[\mathbf{m}(\mathbf{r}')] \cdot (\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^3 r' + \iint_{\text{sample}} \frac{[\mathbf{m}(\mathbf{r}') \cdot \mathbf{n}(\mathbf{r}')] \cdot (\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 r' \right)$$

$$\rho(\mathbf{r}) = -M_s \text{div}[\mathbf{m}(\mathbf{r})] \quad \text{Volume charges}$$

$$\sigma(\mathbf{r}) = M_s \mathbf{m}(\mathbf{r}) \cdot \mathbf{n}(\mathbf{r}) \quad \text{Surface charges}$$

$$\boxed{\mathcal{E}_{1,2} = \mu_0 \sigma \cdot \varphi} \quad \text{with} \quad \mathbf{H}_d = -\nabla \varphi$$

Tip is a dipole

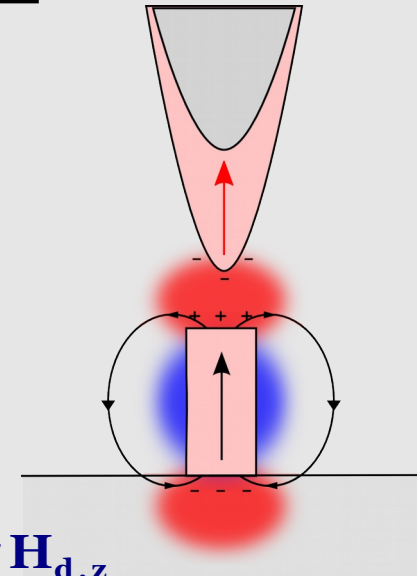


$$\mathcal{E}_{1,2} = -\mu_0 \mu_2 \cdot \mathbf{H}_d$$

$$\mathcal{E}_{1,2} = -\mu_0 (\mu_x \cdot H_{d,x} + \mu_y \cdot H_{d,y} + \mu_z \cdot H_{d,z})$$

$$\Rightarrow \delta\phi = \frac{Q}{k} \mu_0 \mu_i \partial_z^2 H_{d,i}$$

Tip is a monopole



$$\mathcal{E}_{1,2} = \mu_0 \sigma \cdot \varphi$$

$$\mathbf{F}_z = -\mu_0 \sigma \mathbf{H}_{d,z}$$

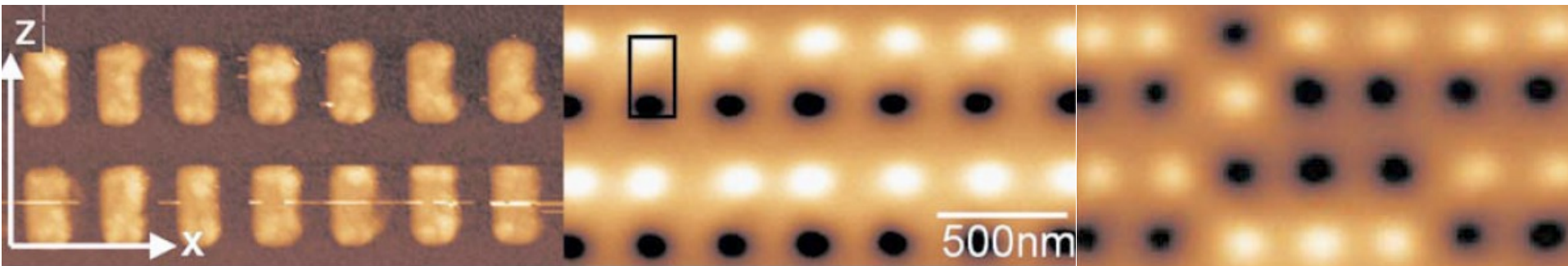
$$\Rightarrow \delta\phi = \frac{Q}{k} \mu_0 \sigma \partial_z H_{d,z}$$

- ↪ In practice, a combination of both models is best suited (dipole is more important)
- ↪ MFM is sensitive to some derivative(s) of the stray field from the sample
- ↪ MFM may be sensitive to in-plane field, depending on the tip moment.

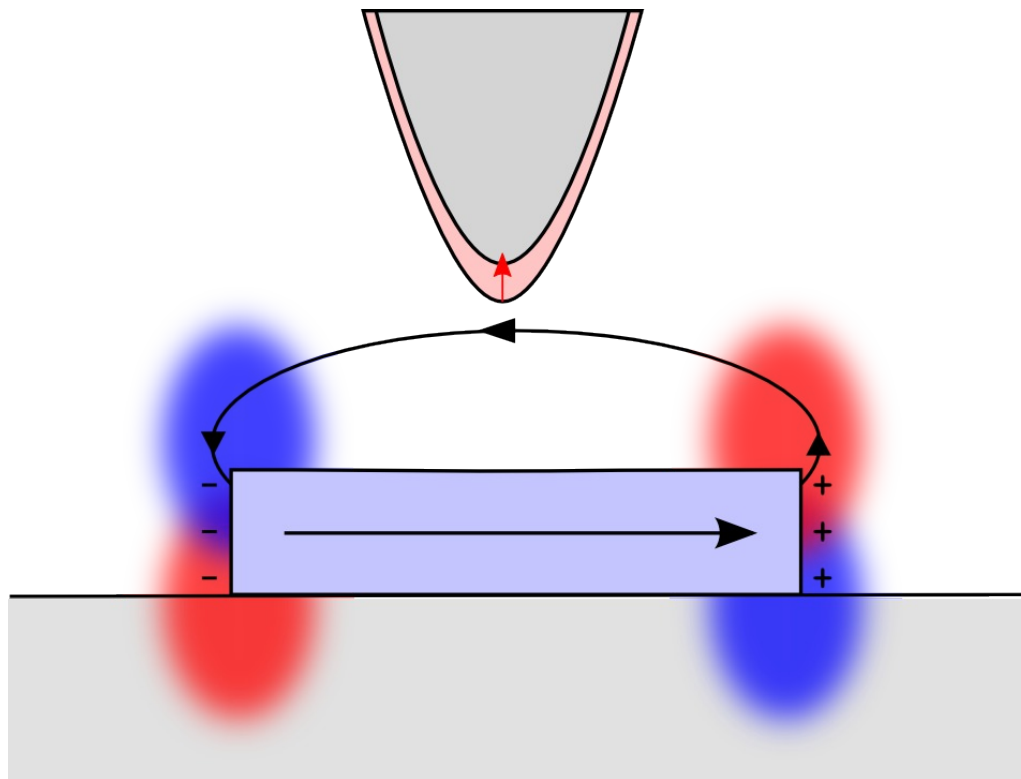
Topography

MFM, saturated

MFM, partly reversed



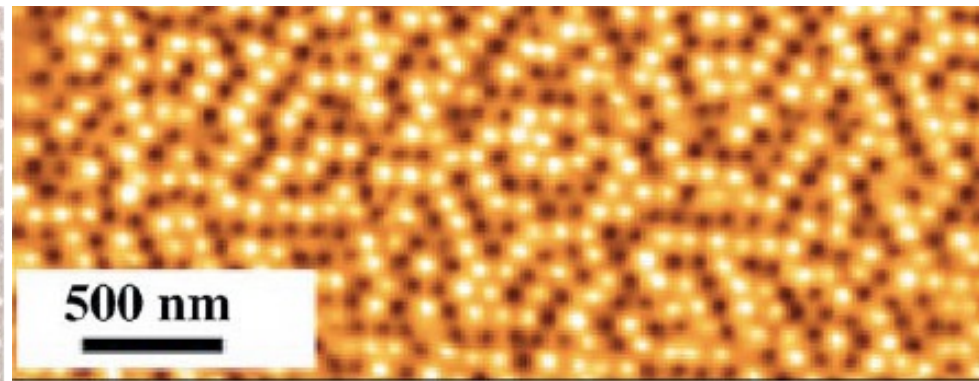
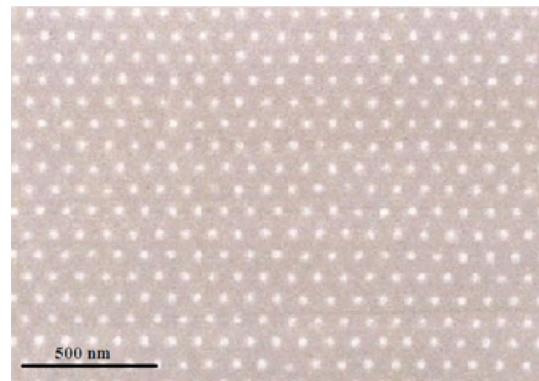
S. Y. Suck et al., APL95, 162503 (2009)



Single-domain in-plane magnetized dots appear as dipoles

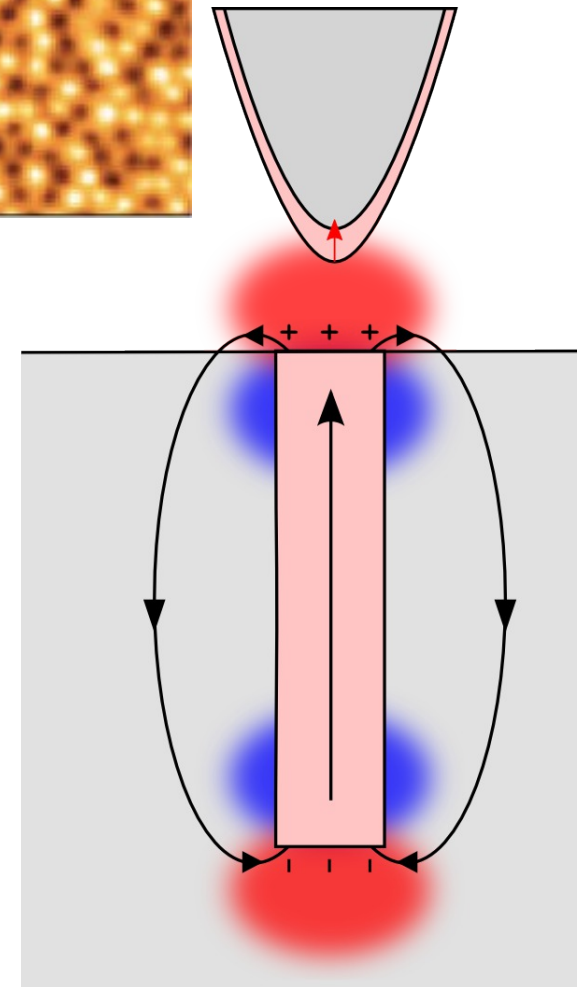
Structure (SEM)

MFM, partly reversed

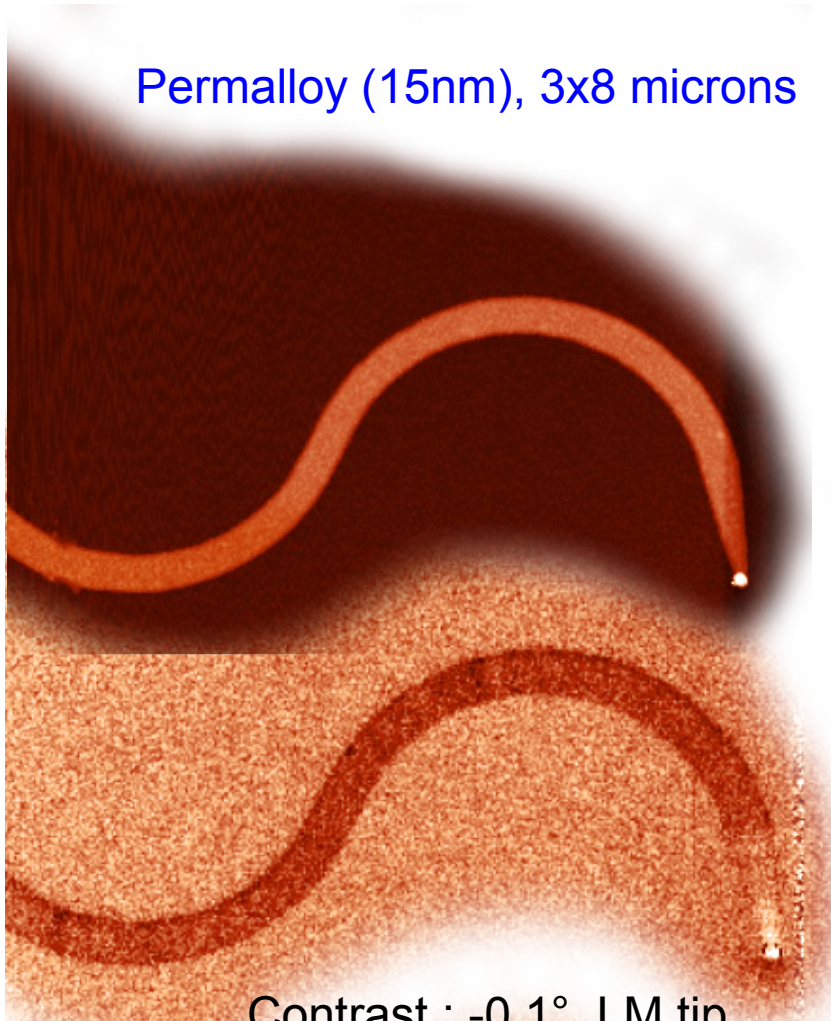


T. Wang et al., APL 92, 192504 (2008)

Single-domain out-of-plane magnetized dots appear as monopoles

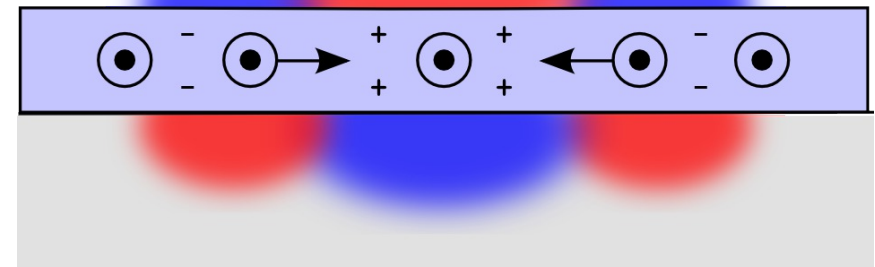
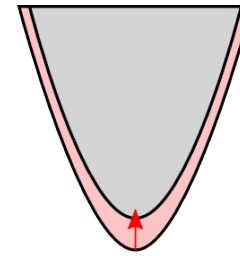


Permalloy (15nm), 3x8 microns



Contrast : -0.1° , LM tip

Lithography : S. Pizzini (Institut Néel)
Imaging : Z. Ishaque (Institut Néel)

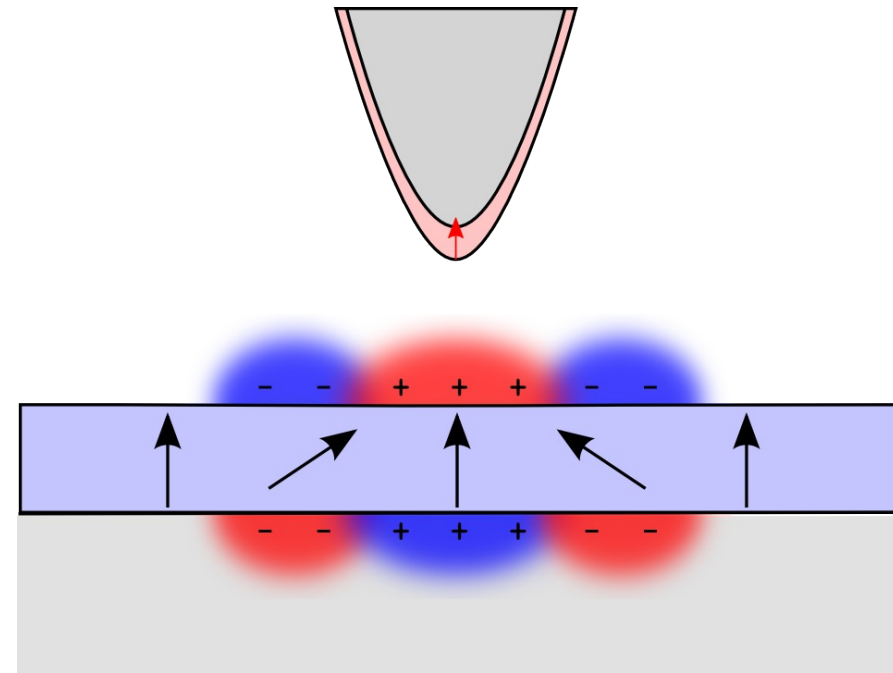
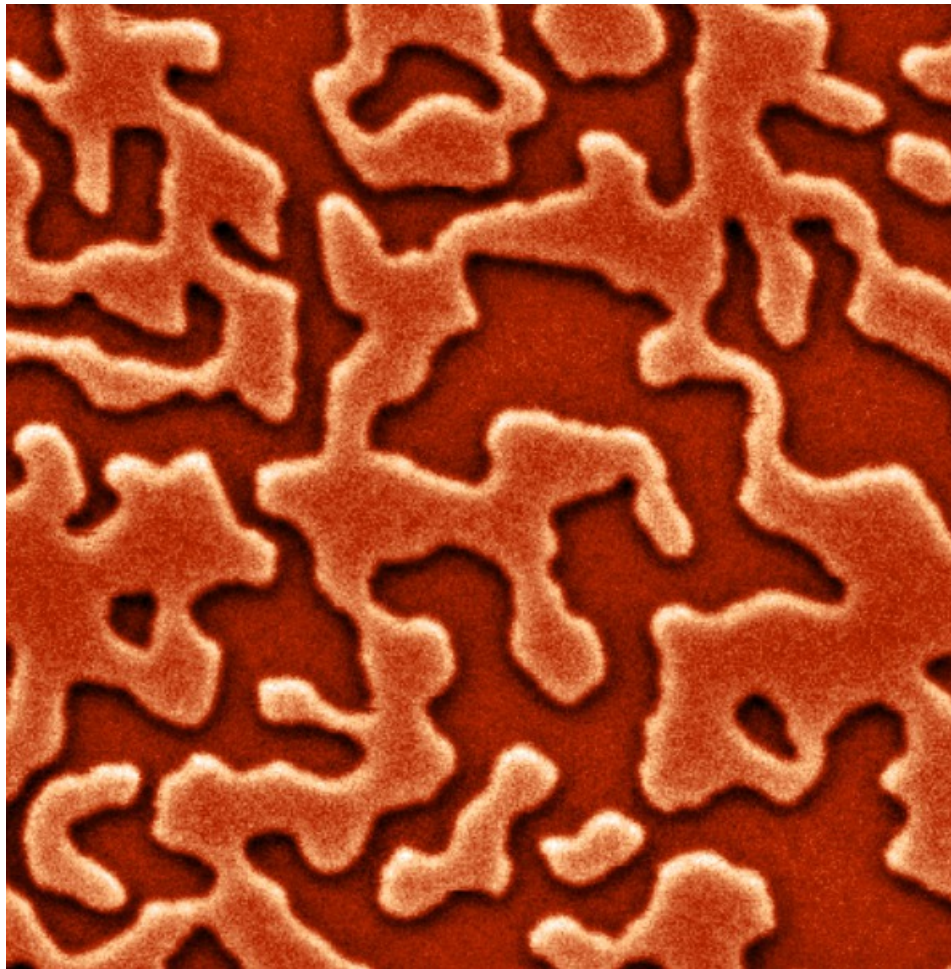


Principle :

1. Stray field magnetizes sample
2. Sample is non-uniform $\rightarrow$ stray field
3. Tip measures sample's stray field

It is a DOMAIN contrast
 Interaction is ALWAYS attractive : red shift
 Contrast is proportionnal to the square of the tip moment

FePt (4nm), 5x5 microns



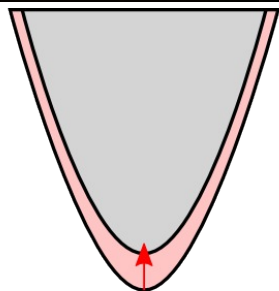
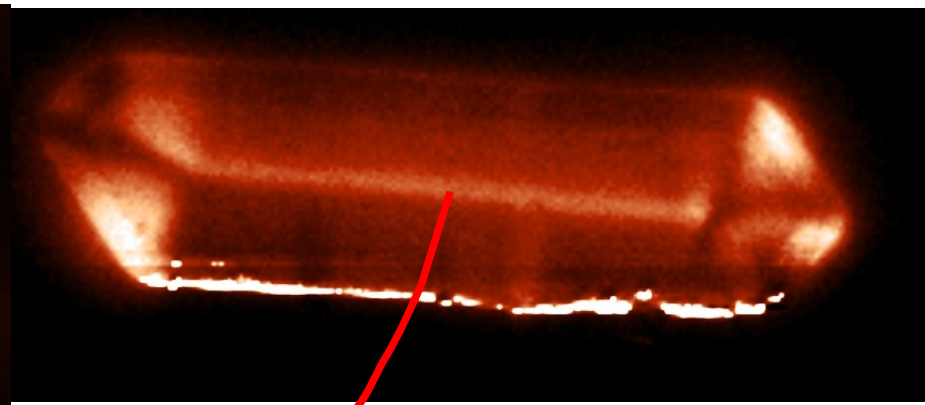
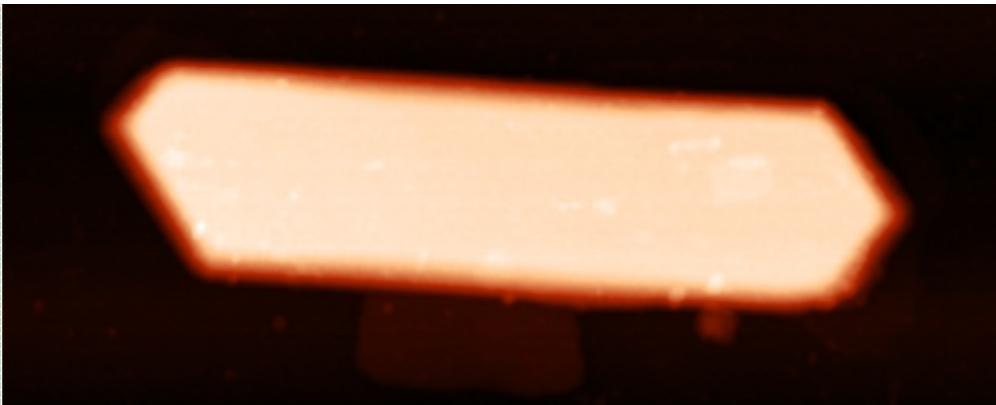
↻ It is a DOMAIN contrast
↻ The direction of magnetization is deduced

Sample : A. Marty (CEA-Grenoble)
Imaging : M. Darques (Institut Néel)

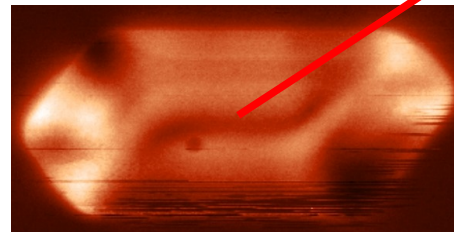
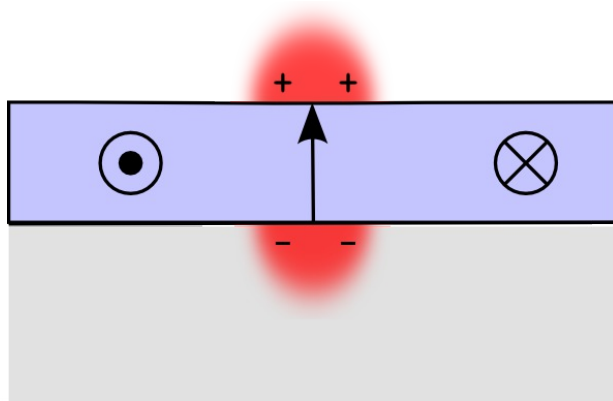
Contrast : $\pm 0.4^\circ$, LM tip

Quantitative analysis :
L. Belliard et al., J. Appl. Phys. 81,
3849 (1997)

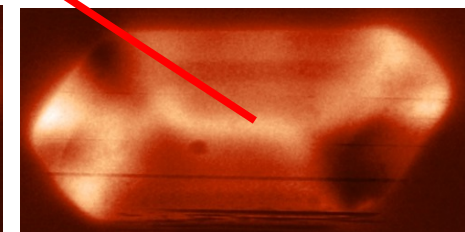
Fe dot (25nm), 2.5x1 microns



↪ Contrast is **MONOPOLAR**
↪ Informs about the polarity of the wall core

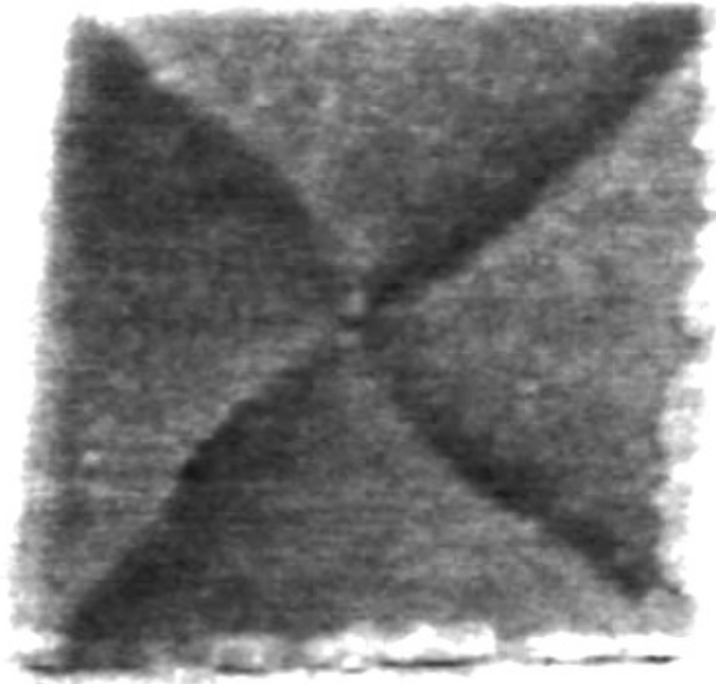


Down core



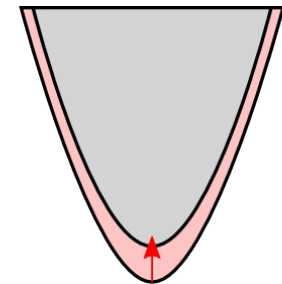
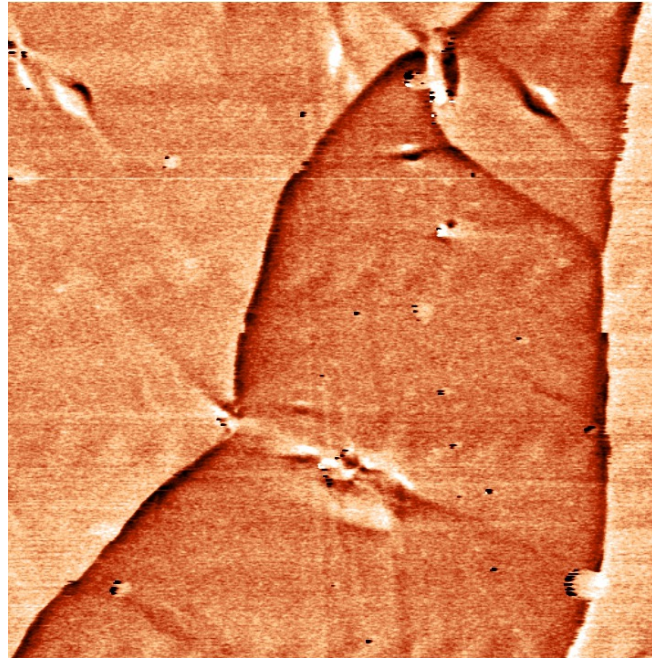
Up core

Permalloy dot (16nm)
2x2 microns

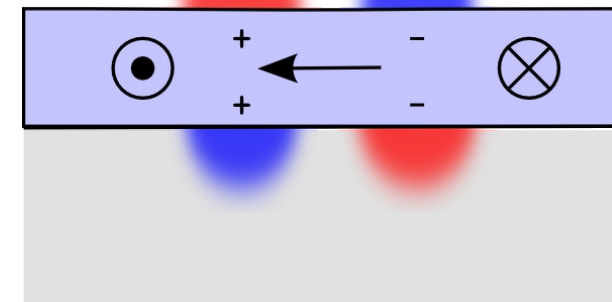


J. M. Garcia et al., APL 79, 656 (2001)

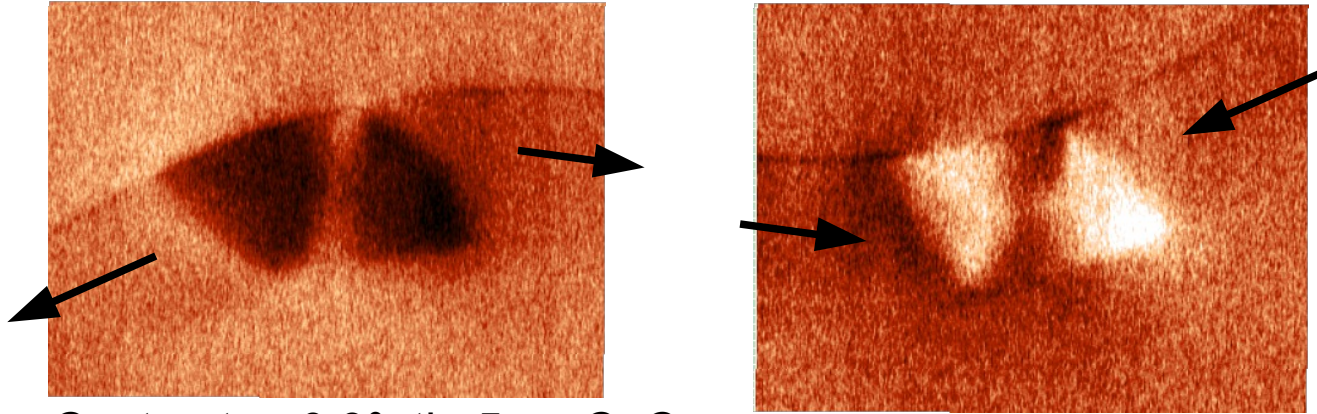
Permalloy film (20nm)
10x10 microns



⇒ Néel wall give rise to DIPOLAR contrast
⇒ Informs about the chirality of the wall core

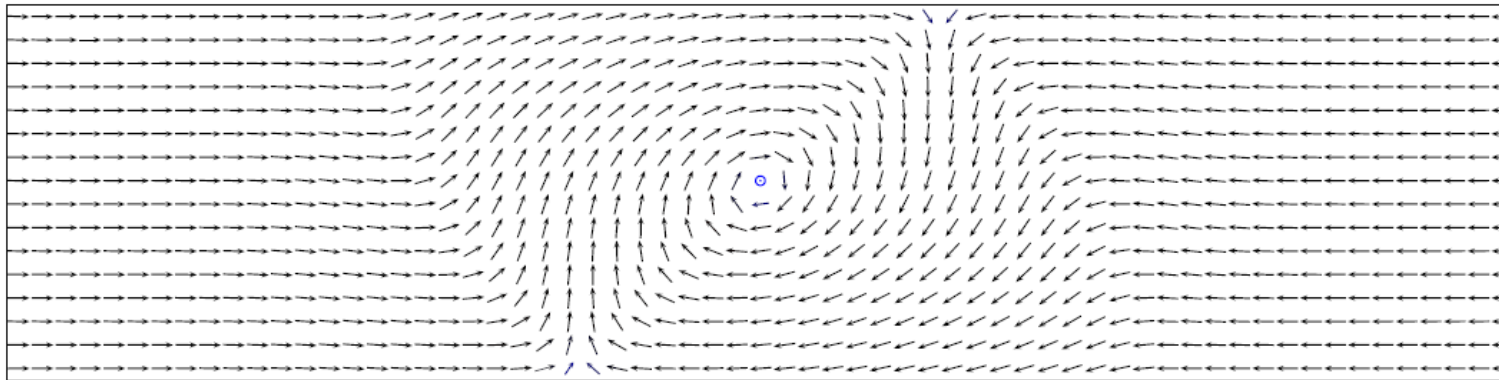


Permalloy stripes (15nm), 250nm wide



Contrast : $\pm 0.3^\circ$, tip 5nm CoCr

Known as vortex domain-wall

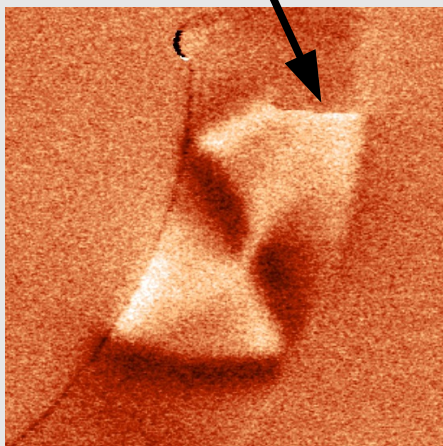


R. McMichael and M. Donahue, IEEE Trans. Magn. 33, 4167 (1997)

↻ Walls in in-plane magnetized stripes → MONOPOLAR
↻ Contrast informs about head-to-head or tail-to-tail

Moderate

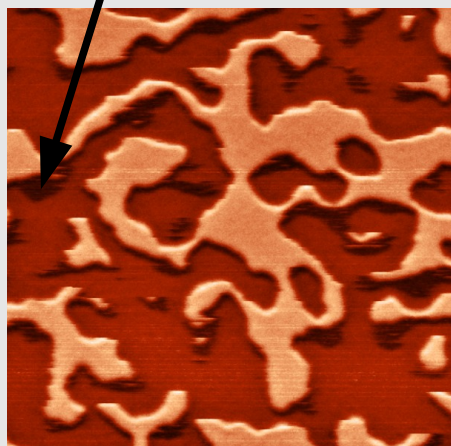
Repulsion



Permalloy (15nm)
500nm wide

Sample : S. Pizzini
Imaging : Z. Ishaque

Attraction



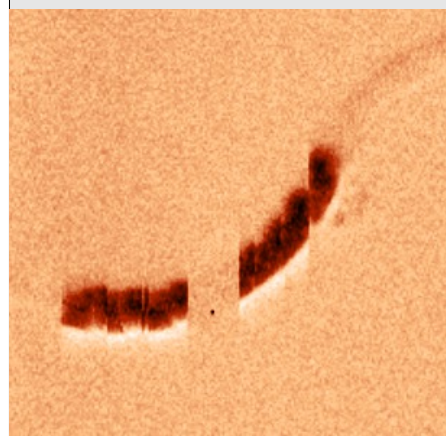
FePt (4nm)
Image 5 microns

Sample : A. Marty
Imaging : M. Darques

Moderate

Repulsion

Attraction

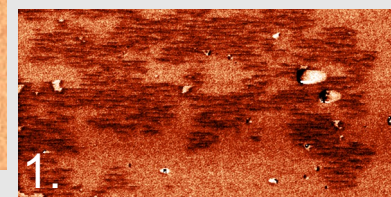
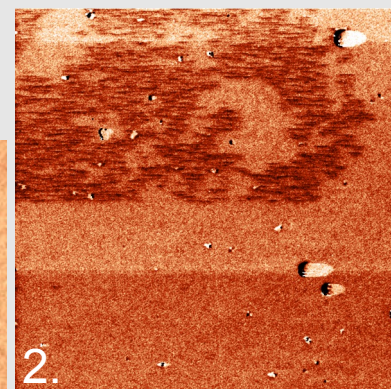


Permalloy (15nm)
500nm stripes

Sample : S. Pizzini
Imaging : Z. Ishaque

2.

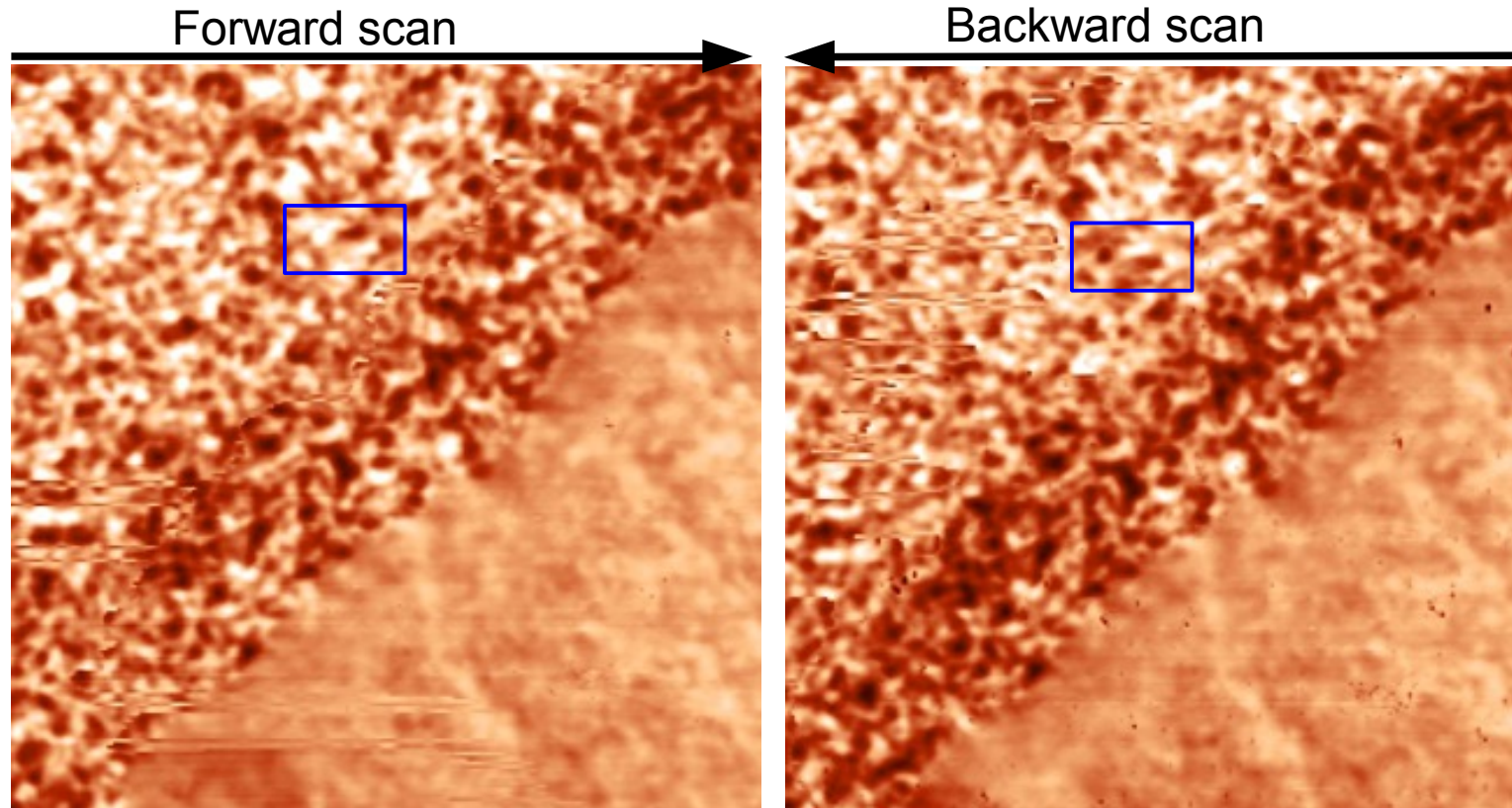
1.



Co (0.6nm)/
graphene (20 mic)

C. Dieudonné

- ↪ Repeat measurement and/or change scanning direction
- ↪ Low-coercive samples require low-moment tips
- ↪ Commercial 'low-moment' may not be low enough

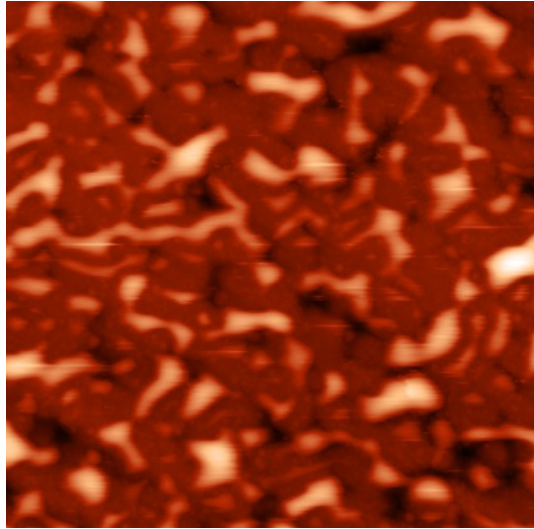


FePt thick film

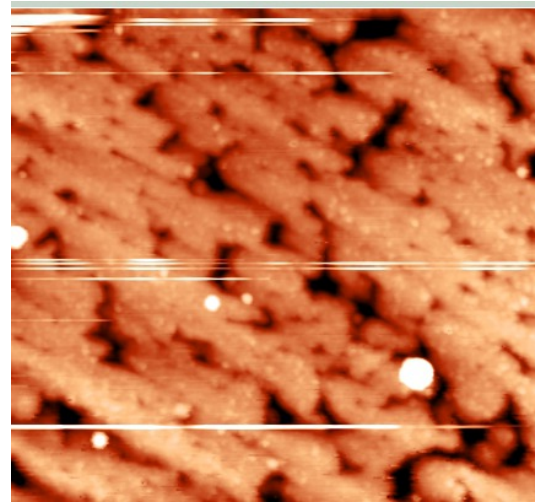
G. Ciuta (Institut néel)

- ↪ Moment of tip reverses during scan
- ↪ Permanent magnet → Choose high-coercivity tips (eg Asylum)

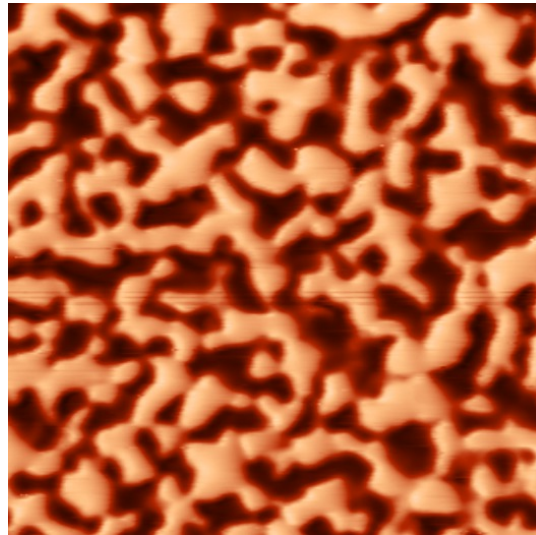
Soft cantilever (70kHz)



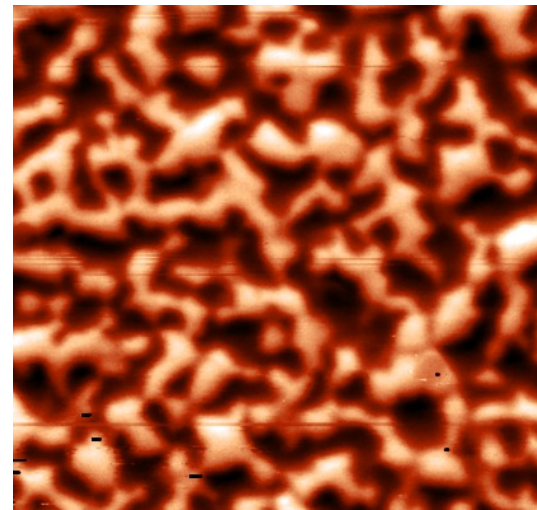
Stiff cantilever (300kHz)



- ↪ Cantilever repelled for tip and sample opposite
- ↪ 'Attractive' domains are over-dominant in the image
- ↪ 'Repulsive' domains lack of resolution
- ↪ Use stiff cantilever for permanent magnets



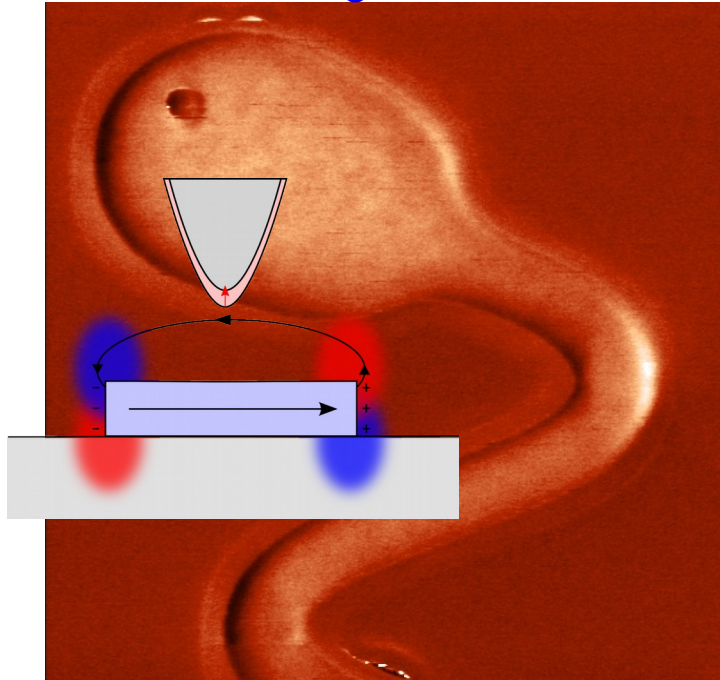
Contrast : $\pm 20^\circ$



Contrast : $\pm 0.5^\circ$

Sample : G. Ciuta (Institut néel)

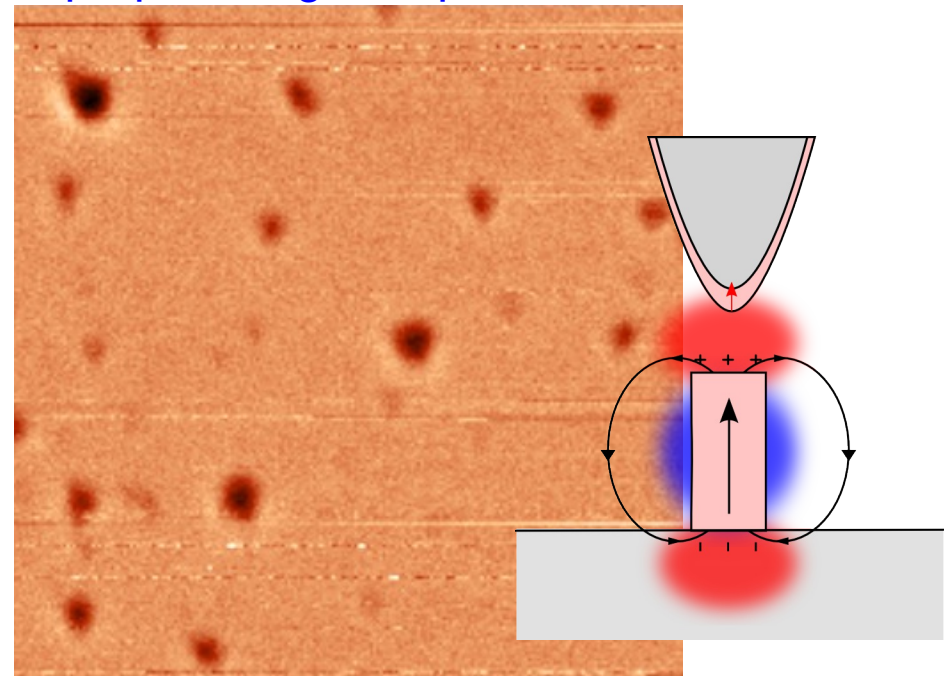
Co(5)\Cu(5)\Py(15nm)
5 microns image



In-plane field (30mT)

Sample : A. Masseboeuf (CEA-Grenoble)

Agglomerated Fe₃O₄
superparamagnetic particles



Out-of-plane field (400mT)

Sample : K. Aissou (LCPO , Bordeaux)

↪ Coercive field of usual tips of the order of 50mT

Moment

Normal moment for most samples
(30-50nm CoCr)

Low moment, or even :

Superparamagnetic or ultra-low moment

⇒ Low-coercivity samples

⇒ Increased resolution

⇒ At the expense of sensitivity

Cantilever

Normal stiffness ('force modulation')
→ resonance at 70kHz

Large stiffness

⇒ High stray-field samples
(typically permanent magnets)

⇒ At the expense of sensitivity

Tip sharpness

Normal resolution (50nm)

Sharp tips (resolution 25nm), expense :

⇒ Commercial and/or spacial
fabrication (FIB etc.)

⇒ Loss of sensitivity

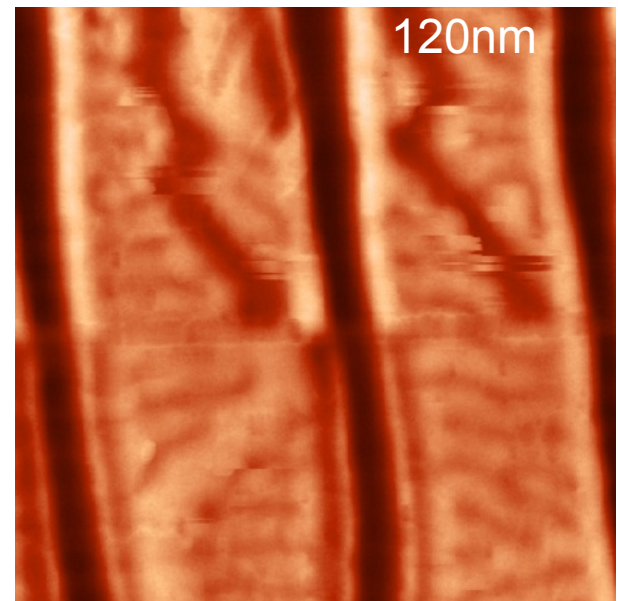
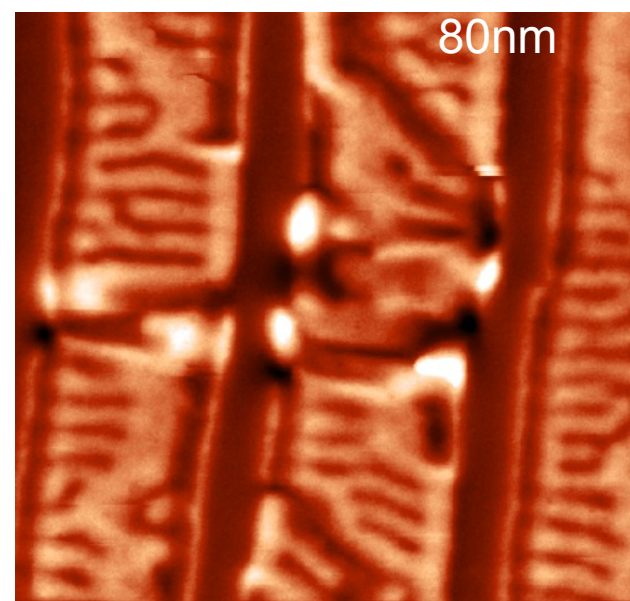
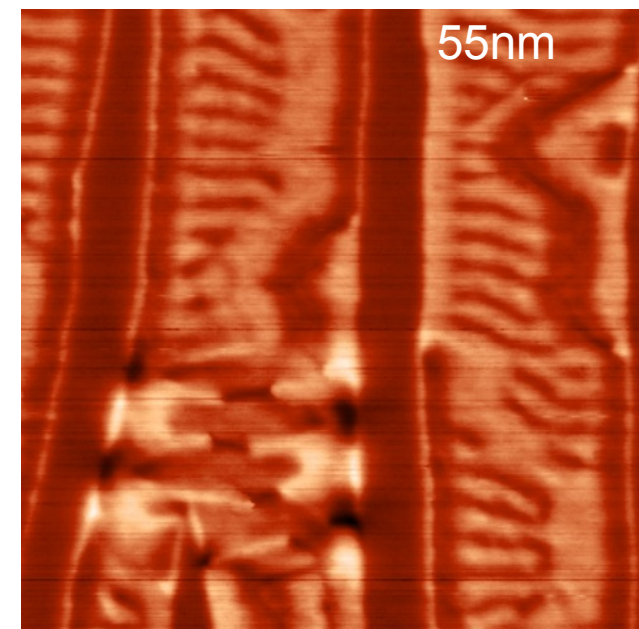
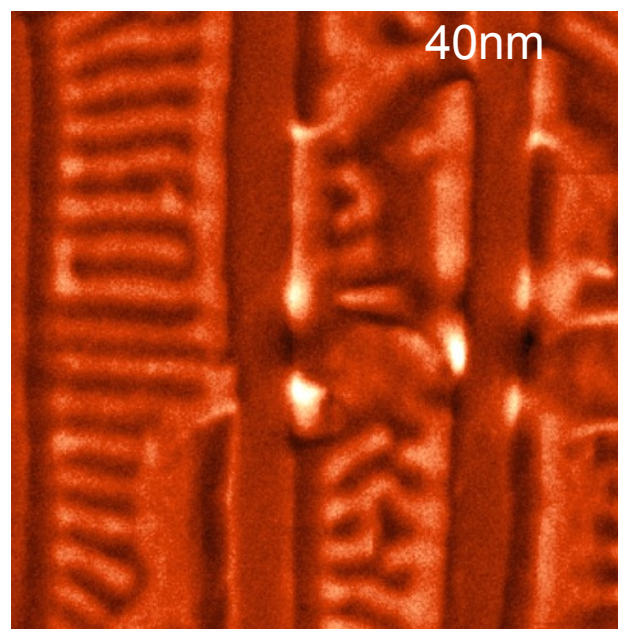
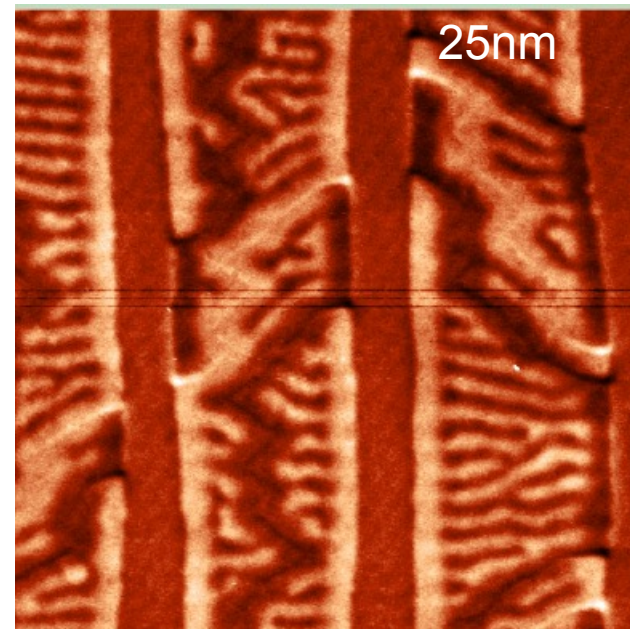
Coercivity

Normal (30-70mT)

High coercivity (eg Asylum)

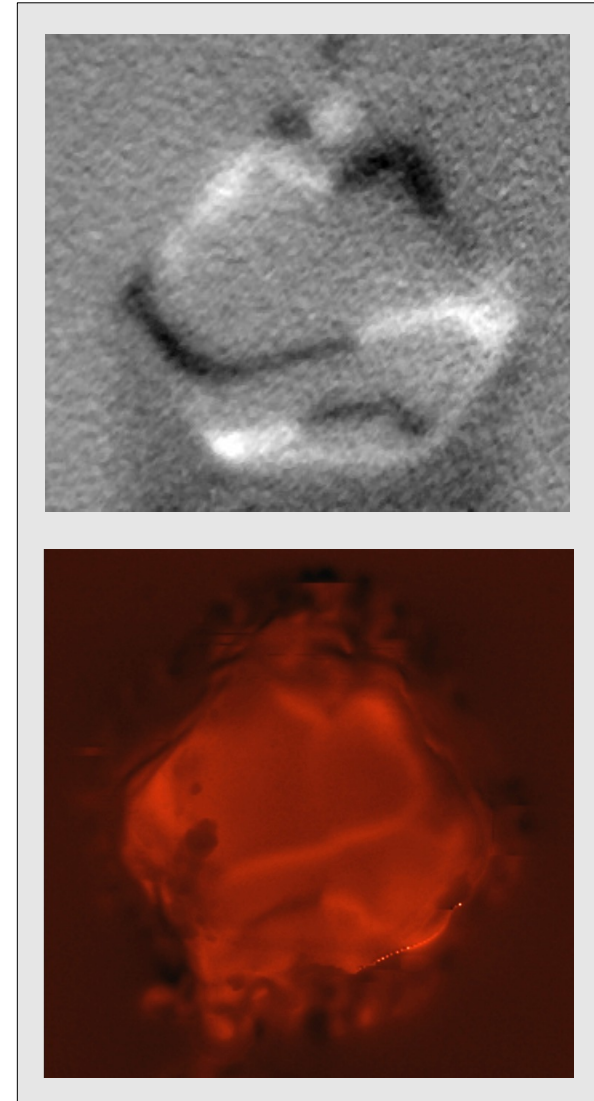
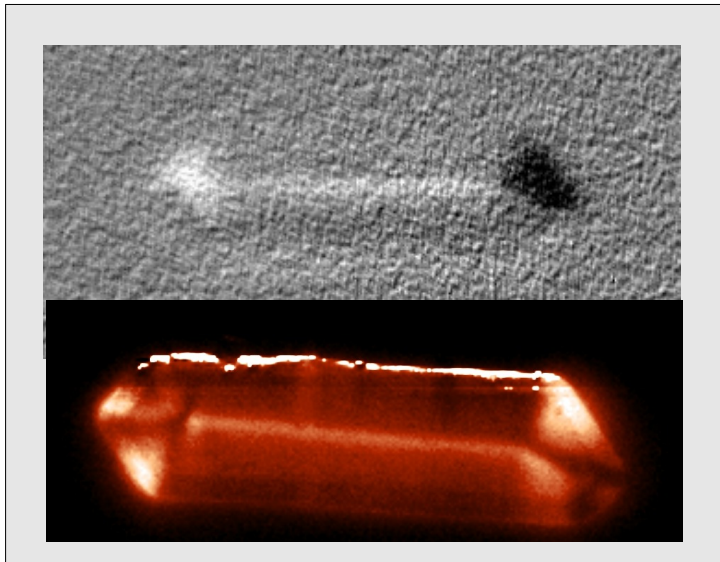
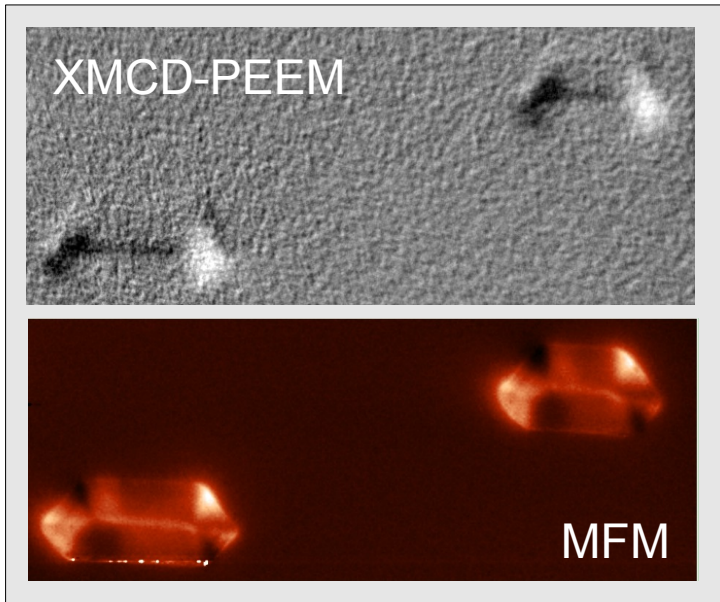
⇒ High stray-field samples
(typically permanent magnets)

⇒ At the expense of cost

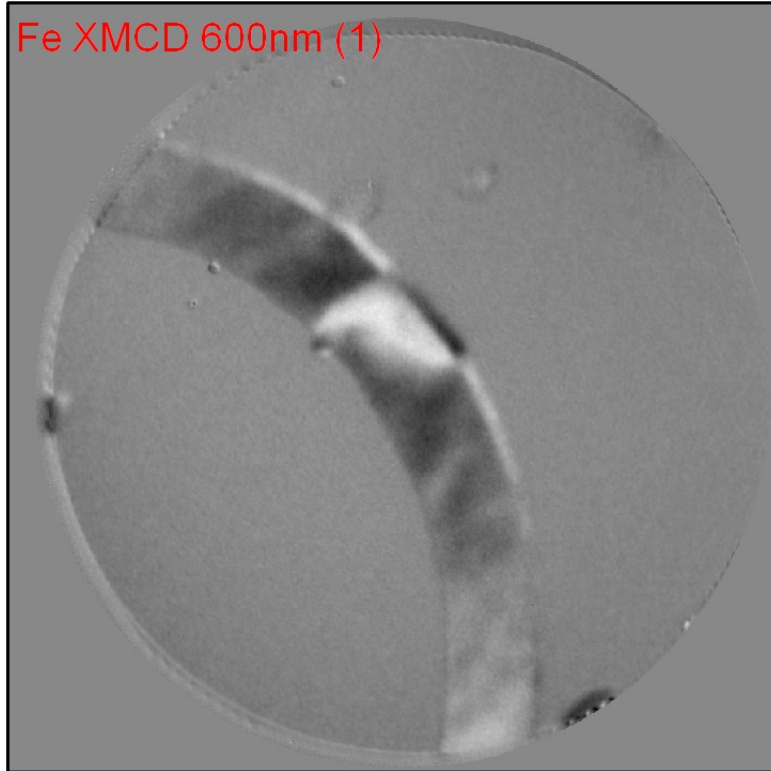


↪ Compare tips !
↪ Use identical sample and
imaging parameters

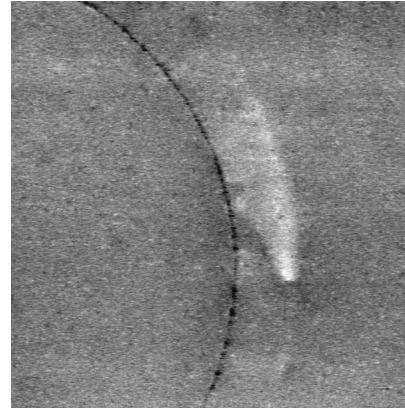
Sample : MnAs(001)
R. Belkhou (Soleil)



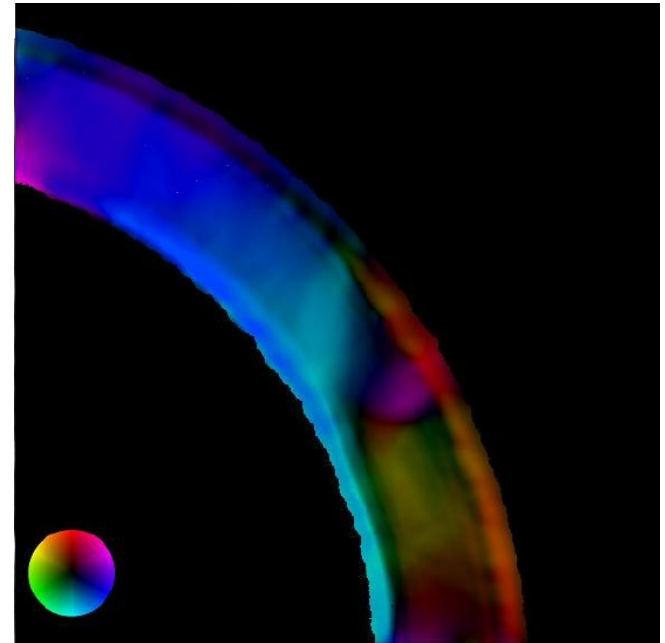
XMCD-PEEM



MFM



Lorentz



Some references

Y. Zhu Ed., Modern techniques for characterizing magnetic materials, Springer (2005)

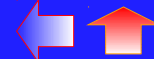
A. Schwartz et al., Scanning probe techniques: MFM and SP-STM, in : series Handbook of magnetism and advanced magnetic materials, Novel techniques for characterizing and preparing samples (vol.3), H. Kronmüller, S. Parkin Ed. (2007)

A. Hubert, R. Schäfer, Magnetic domains, Springer (1999)

**Repository of the European School on Magnetism : <http://esm.neel.cnrs.fr>
See 2005 School : « New experimental approaches to Magnetism »**

Why we DO need 'SOLEIL'





Aug 22nd - Sep. 2nd
2011
Targoviste - Romania

EUROPEAN SCHOOL ON MAGNETISM

2011

TIME-DEPENDENT PHENOMENA IN MAGNETISM

$$+ \sum_{\vec{r}, \vec{r}'} \frac{J_{\vec{r}, \vec{r}'}}{|\vec{r} - \vec{r}'|} \vec{S}_{\vec{r}} \cdot \vec{S}_{\vec{r}'} - J_H S_z^2 - J_H (\vec{\mu}_B \cdot \vec{S}_i)$$

$$M_S = (n_{\uparrow} - n_{\downarrow}) \mu_B$$

$$\leq n \mu_B$$

$i = \vec{r}$



<http://esm.neel.cnrs.fr>

Organizers

Jan VOGEL (chair), Grenoble
Olivier FRUCHART, Grenoble
Olivier ISNARD, Grenoble
Claudine LACROIX, Grenoble
Ioan CUCIU, Targoviste
Calin OROS, Targoviste
Laura M. GORCHILL, Targoviste

Scope

The European School on Magnetism (ESM) is a joint action of the European Community of Magnetism, organized in cooperation with JEMS conference (Joint European Magnetic Symposia). ESM aims at providing young scientists with a thorough insight in the fundamentals of magnetism up to its most modern aspects.

Like previous editions of ESM, the 2011 School is based on a broad series of fundamental lectures, before focusing on a special topic. The topic selected for 2011, time-dependent phenomena in magnetism, covers a wide range of phenomena from